

***NRL Multivariate Ocean Data Assimilation  
System Overview***

***Jim Cummings***



# ***NRL Multivariate Ocean Data Assimilation***

## **DA Technique Based on Optimal Estimation Theory**

- oceanographic version of MVOI method widely used in NWP systems (Daley, 1991)
- simultaneous analysis of five ocean variables: temperature, salinity, geopotential, and u-v velocity components (T, S,  $\Phi$ , u, v)
- multivariate in mass and velocity

## **Observation Space Formulation**

$$\mathbf{x}_a = \mathbf{x}_b + \mathbf{P}_b \mathbf{H}^T (\mathbf{H} \mathbf{P}_b \mathbf{H}^T + \mathbf{R})^{-1} [\mathbf{y} - \mathbf{H}(\mathbf{x}_b)]$$

where  $\mathbf{x}_a$  = analysis,  $\mathbf{x}_b$  = background

$\mathbf{P}_b$  = background error covariance,  $\mathbf{R}$  = observation error covariance

$\mathbf{H}$  = forward operator (spatial interpolation in 3 dimensions)

$(\mathbf{x}_a - \mathbf{x}_b)$  = analyzed increment

$[\mathbf{y} - \mathbf{H}(\mathbf{x}_b)]$  = innovation vector (synoptic T, S, u, v observations)



# ***NRL Multivariate Ocean Data Assimilation***

## **Flexible System**

- global or regional applications
- supports re-locatable, multi-scale analyses on nested, successively higher resolution grids
- used to initialize/update ocean forecast model or run stand-alone
- interfaced to multiple ocean forecast models
  - Hybrid Coordinate Ocean Model (HYCOM)
  - Navy Coastal Ocean Model (NCOM)
  - Wavewatch III wave forecast model (WW3)

## **Designed as Complete End-to-End Analysis System**

- fully automated ocean data quality control
- multivariate analysis
- performance diagnostics package



# ***NRL Multivariate Ocean Data Assimilation***

## **Operational Applications**

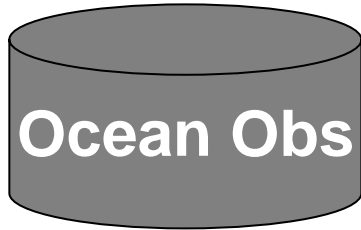
- SST and sea ice analyses as LBCs for COAMPS and NOGAPS NWP models at FNMOC
- global and regional 3D analysis-only runs at FNMOC and NAVOCEANO

## **Pre-Operational Applications**

- MVOI cycling with global HYCOM (NOPP/GODAE project)
- MVOI cycling with regional HYCOM and NCOM (various NRL and NOPP/CODAE projects)
- ensemble-based adaptive sampling project with ocean gliders
- assimilation altimeter SWH in global Wavewatch III at FNMOC

# NRL Ocean Data Assimilation

Sequential Incremental Update Cycle  
Analysis-Forecast-Analysis



**SST:** Ship, Buoy, AVHRR (GAC/LAC), GOES, AMSR-E, AATSR, MSG

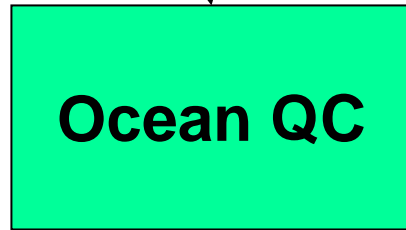
**SSS:** TSG

**Temp/Salt Profiles:** XBT, CTD, Argo Float, Buoy (Fixed/Drifting), Glider

**SSH:** Altimeters (Jason, Envisat, GFO), *in situ* Temp/Salt profiles

**SWH:** Altimeters, Buoys

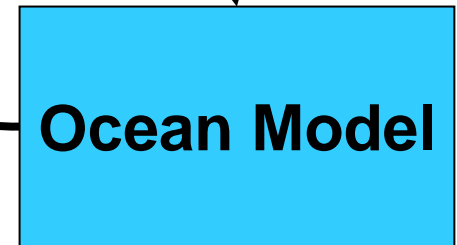
**Sea Ice:** SSM/I



Innovations



Increments



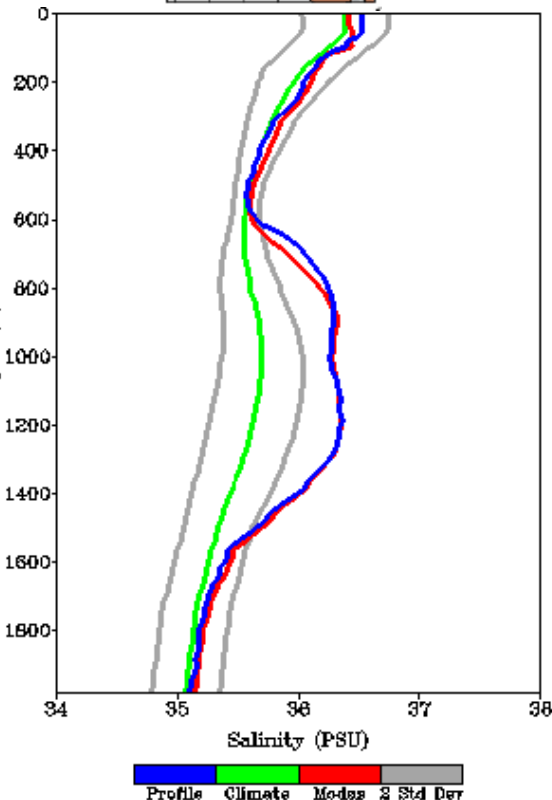
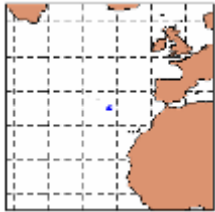
First Guess

Forecast Fields  
Prediction Errors

Model forecast fields and prediction errors are being evaluated for use in the QC of newly received ocean observations



# Salinity Observation Data Sources



- observed salinity (Argo, CTD) is directly assimilated
- salinity is derived for temperature-only profiles using MODAS historical TS relationships (bi-monthly, global)

$$S_{i,k}(T) = \bar{S}_{i,k} + \alpha_{i,k}(T - \bar{T}_{i,k})$$

$$\alpha_{i,k} = \frac{\sum b_{i,j}(T_{j,k} - \bar{T}_{i,k})(S_{j,k} - \bar{S}_{i,k})}{\sum b_{i,j}(T_{j,k} - \bar{T}_{i,k})^2}$$

$$b_{i,j} = \exp(-((x_j - x_i)/L_x)^2 - ((y_j - y_i)/L_y)^2 - ((t_j - t_i)/L_t)^2)$$

- derived salinity values are put through the automated QC procedures in same way as an observed salinity

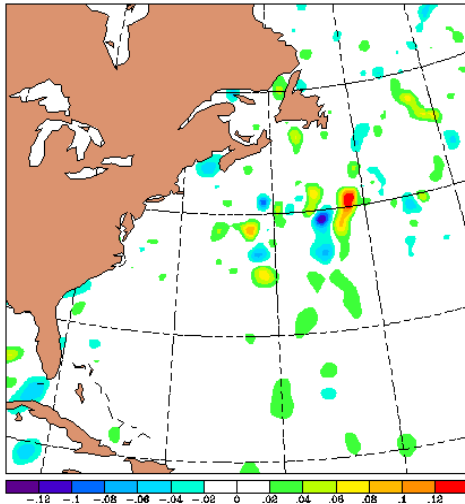
MODAS salt profile derived from Argo float temperature in MEDDY (red) - verifying Argo salt profile in blue – MODAS does a good job predicting MEDDY salinities



# Altimeter SSH Assimilation

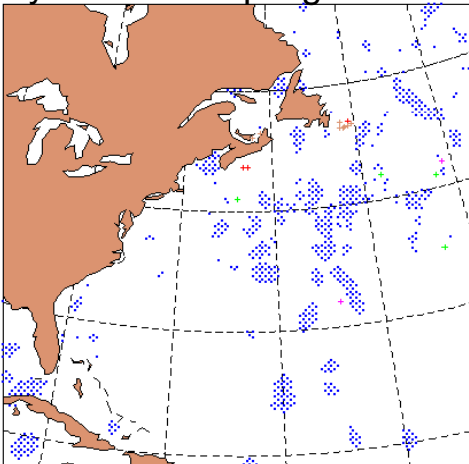
**Synthetic T/S profiles generated using one of two approaches:  
Synthetics are assimilated in the MVOI as an observing system**

SSH Increments



1. Direct method (modified form of Cooper Haines)
  - adjusts model density profile to be consistent with measured change in model forecast SSH (creates T/S innovations)
  - observation errors set to forecast error variance plus residual error from iterative fit of density adjustment
2. MODAS synthetic BT method
  - computes temperature at depth from SSHA using stored regressions of climate anomalies of temperature and dynamic height
  - salinity is then computed from synthetic temperatures
  - observation errors are set to stored regression residuals

Synthetic Sampling Locations



**synthetic profiles are generated where analyzed change in SSH exceeds altimeter measurement errors (~2 cm)**

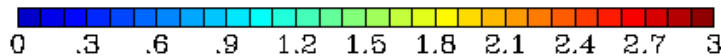
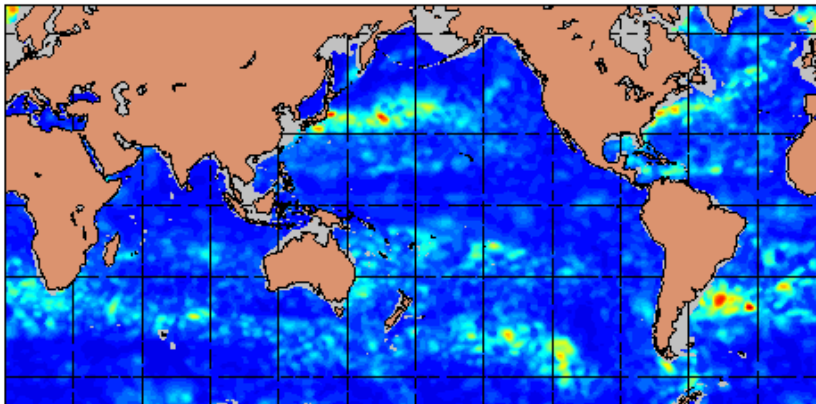


# Background Error Covariances

**Separable formulation: product of a variance and a correlation**

## Error Variances

- vary by position, depth and analysis variable
- evolve with time, updated continuously using analyzed increment fields
- error growth parameterization used in long term absence of observations
  - function of age of data on grid and innovation temporal autocorrelations
  - evolves to climate or free running model errors in limit of no data



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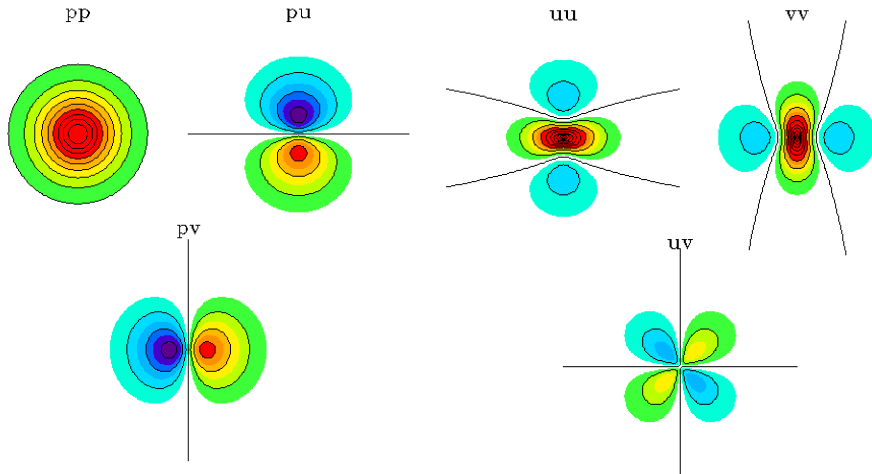
400 M temperature background error standard deviation (°C) from FNMOC global analysis





# Background Error Correlations

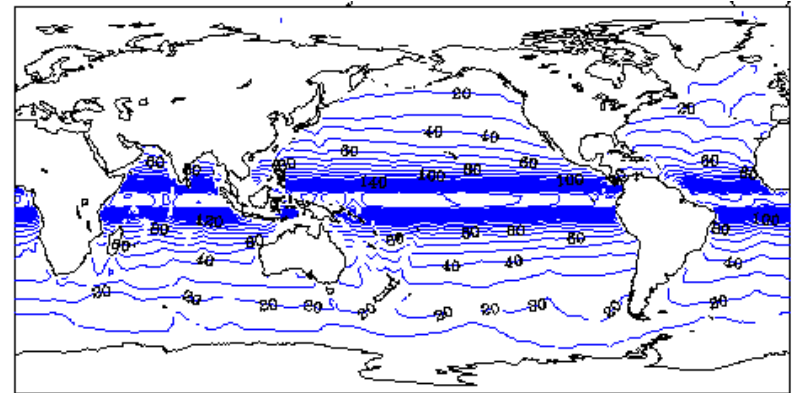
**Separable formulation: product of a horizontal and a vertical correlation**



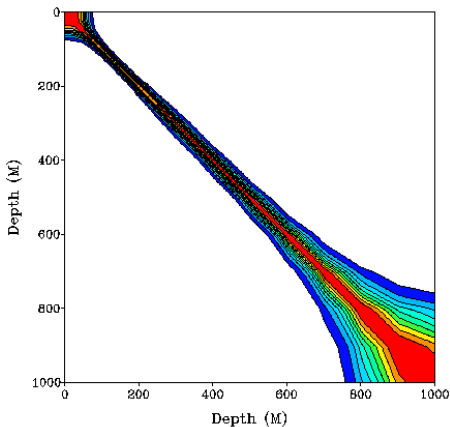
**geopotential and velocity**

**u,v velocity**

Horizontal correlations are multivariate in velocity and geopotential - length scales depend on location (default is Rossby radius)



**Rossby Radius Deformation (km)**



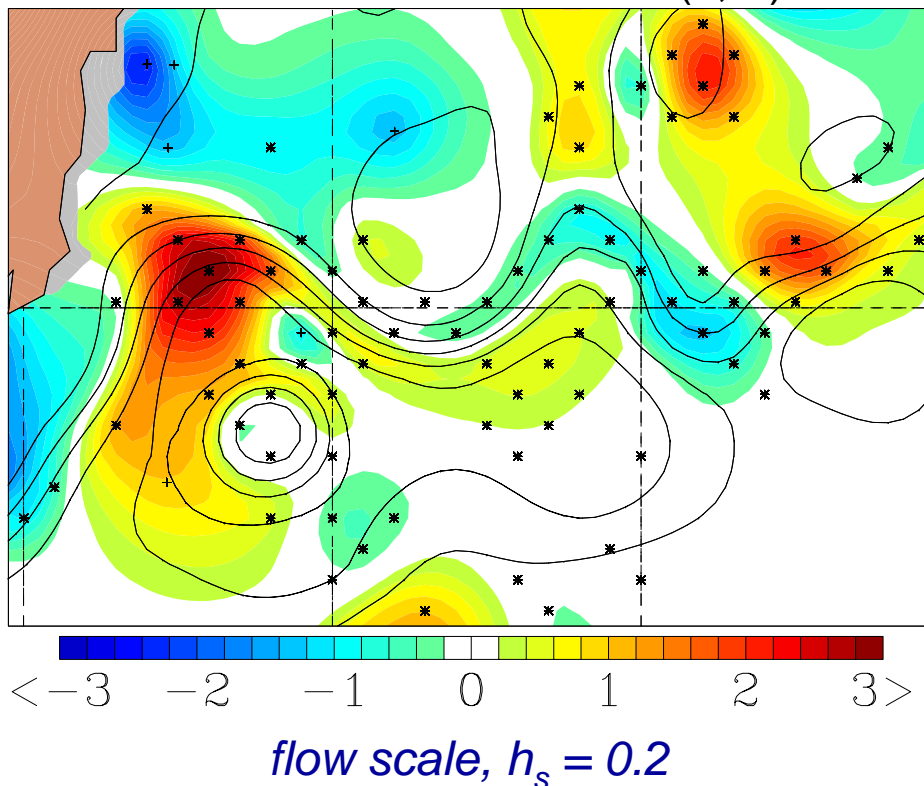
Vertical correlation length scales are computed from background vertical density gradients - correlations evolve with time but do not vary with location

scales are large (small) when stratification is weak (strong)



# Flow Dependent Error Correlations

Temperature Increments at 100 M (color)  
Forecast Surface Height (lines)  
Observation Locations (\*, +)



MVOI correlations modified to incorporate flow dependence from forecast surface height.

$$C = C_h C_v C_f$$

$C_h$  – horizontal correlation

$C_v$  – vertical correlation

$C_f$  – flow dependent correlation

Small (large) values of flow dependence scalar ( $h_s$ ) produces strong (weak) flow dependence

Note increments stretched along Kuroshio front and decorrelation in cold eddy south of the Kuroshio



# Observation Error Variances

- sum of measurement error ( $\varepsilon_i$ ), representation error ( $\varepsilon_r$ ), and data age error ( $\varepsilon_\tau$ )
- measurement errors are from data provider or table look-up
  - satellite SST measurement errors computed from buoy match-ups
  - *in situ* measurement errors function of instrument type
- satellite representation error function of resolution of model ( $r_g$ ), resolution of observing system ( $r_o$ ), and background horizontal gradient ( $\nabla_b$ )

$$\varepsilon_r = \nabla_b \cdot (r_o / r_g) \quad r_o > r_g$$

- profile representation error function of mesoscale variance ( $\sigma_t$ ) and uncertainty associated with internal wave activity (vertical gradient used as proxy)

$$\varepsilon_r = \kappa_t \sigma_t + \lambda_t \cdot (dT \cdot dz^{-1})$$

- $\kappa_t$  and  $\lambda_t$  are determined empirically for temperature and salinity
- data age error a function of observation time ( $\tau_o$ ), time correlation scale ( $\tau_c$ ), and observation depth ( $z_o$ ) relative to maximum depth of time correlation ( $z_c$ )

$$\varepsilon_\tau = \varepsilon_i \cdot (\tau_o \cdot \delta) / \tau_c$$
$$\delta = 1 - z_o / (z_o + z_c)$$

- observation error variances tuned based on  $J_{\min}$  statistics

$J_{\min} \ll 1$  variances too large,  $J_{\min} \gg 1$  variances too small (or bad data)

***Projects Underway and  
Present Developments***

# Projects Underway – Present Developments

- **Conversion to 3D-Var assimilation system based on NAVDAS**
  - natural development pathway from MVOI
  - global solution, no data selection
  - direct assimilation of observations with (weak) nonlinearities in the observation operator
  - non-separable covariances (horizontal and vertical)
  - vertical flow dependence (isopycnal coordinates)
  - new balance operators (based on Anthony Weaver's work)
- **Development of 4D-Var assimilation based on NAVDAS-AR**
  - focus on Navy Coastal Ocean Model (NCOM) in limited domains
- **Adaptive Sampling**
  - incorporation of ensemble covariances in assimilation (so called hybrid approach)

# Projects Underway – Present Developments

- Assimilation of new observing systems
  - glider T/S data and METOP, MSG, AMSR-E and MTSAT SST
- Diagnostics and automated tuning of error covariances
- Wave Model assimilation of altimeter SWH
  - Global and regional Wavewatch III assimilation at FNMOC
  - evaluation of alternative wave model updating strategies
- Global and regional HYCOM/NCODA NOPP/GODAE transitions
  - real-time demonstration later this year (2007)
- Development and implementation of adaptive QC methods
- Improvement in pre-processing functions
  - adaptive data thinning to handle large amounts of satellite observations
  - bias detection/correction

**END**