

Lecture 3B

The Community Radiative Transfer Model (CRTM)

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Contents

- General requirements on forward operators
- Vertical stratification and approximation methods to calculate transmittance
- Gaseous absorption and fast transmittance models (ODAS, ODPS, SSU, Zeeman, NLTE) in CRTM
- Aerosol and cloud absorption and scattering models
- Radiative transfer solution in a vertically stratified atmosphere (ADA)
- Surface emissivity models
- References

Satellite Data Assimilation Principle

$$J = \frac{1}{2} (\mathbf{x} - \mathbf{x}^b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}^b) + \frac{1}{2} [\mathbf{I}(\mathbf{x}) - \mathbf{I}^o]^T (\mathbf{E} + \mathbf{F})^{-1} [\mathbf{I}(\mathbf{x}) - \mathbf{I}^o]$$

where

\mathbf{x} is a state vector including all possible atmospheric and surface parameters.

\mathbf{I} is the radiance vector

\mathbf{B} is the error covariance matrix of background

\mathbf{E} is the observation error covariance matrix

\mathbf{F} is the radiative transfer model error matrix

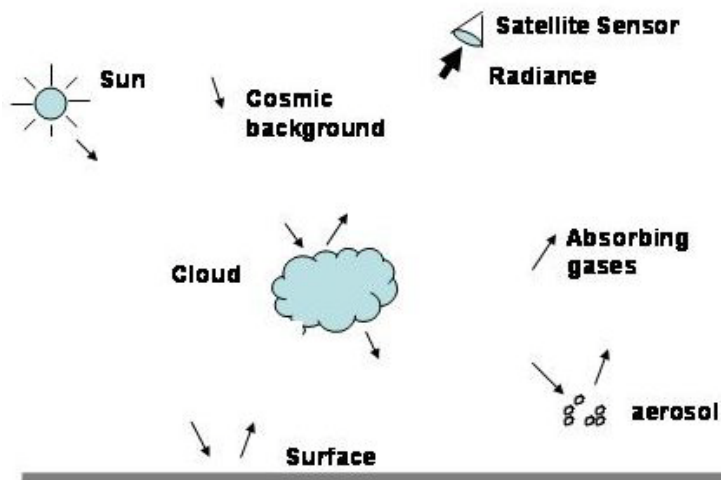
- Forward models and its Jacobians
- Error covariance matrices
 - Background
 - Forward model
 - Observations
- Bias corrections
 - Background
 - Forward model
 - Observations

Requirements on Radiative Transfer Models for Data Assimilation

- Fast and accurate in forward, tangent linear/adjoint models
 - All weather conditions
 - Surface and atmospheric spectroscopy
- Flexible interface with different NWP models
 - Global forecast system, GFS, NOGAPS, etc.
 - Regional forecast model: e.g. WRF
- Expansion for broader applications
 - satellite calibration/validation and climate reanalysis
 - Solar insolation (direct/diffuse) for renewable energy

What CRTM Does?

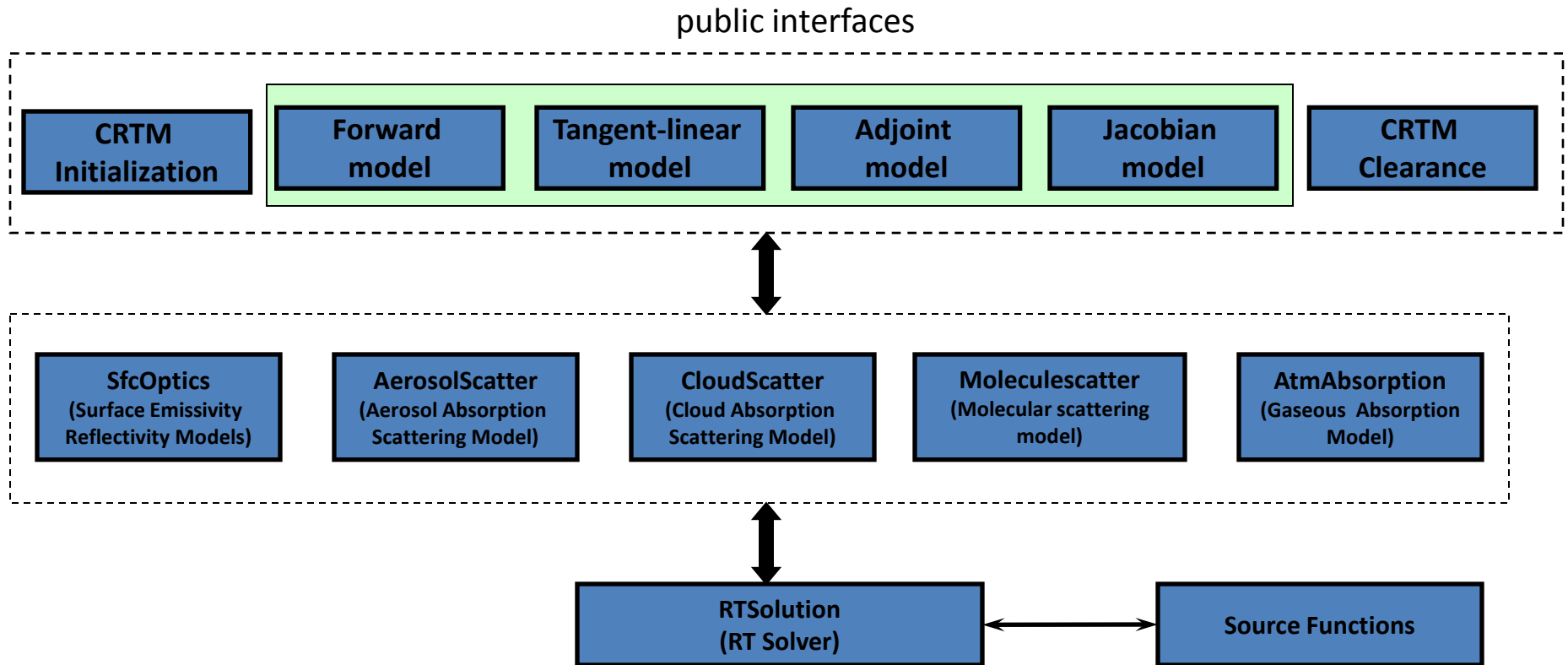
- Perform fast and accurate satellite radiance simulations (Forward model)
- Compute radiance sensitivities and derivatives (Tangent-linear, Adjoint and Jacobian models)
- Support IR, MW, Visible and UV sensors
- Work under all atmospheric and surface conditions



CRTM supports more than 100 Sensors

- GOES-R ABI
- NPP/JPSS CrIS/ATMS/VIIRS
- Metop A and B IASI/HIRS/AVHRR/AMSU/MHS
- TIROS-N to NOAA-19 AVHRR
- TIROS-N to NOAA-19 HIRS
- GOES-8 to 15 Imager
- GOES-8 to 15 sounder IR and VIS
- Terra/Aqua MODIS
- MSG SEVIRI
- Aqua AIRS, AMSR-E, AMSU-A,HSB
- NOAA-15 to 19 AMSU-A
- NOAA-15 to 17 AMSU-B
- NOAA-18/19 MHS
- TIROS-N to NOAA-14 MSU
- DMSP F8, F10, F11, and 13 to15 SSM/I
- DMSP F13,15 SSM/T1
- DMSP F14,15 SSM/T2
- DMSP F16-20 SSMIS
- Coriolis Windsat
- TIROS-NOAA-14 SSU
- FY-3 A and B IRAS, MERSI, MWTS,MWHS,MWRI
- COMS MI
- GPM GMI
- TRMM TMI
- MT MADRAS/SAPHIR

CRTM Major Modules



- Input profiles: pressure, temperature, water vapor and ozone profiles at user defined layers, and optionally, water content and mean particle size profiles with up to 6 cloud types; 8 types of aerosols.
- Surface emissivity: computed internally or supplied by user.
- Frequency coverage: MW, IR, and Visible/UV.

K-Matrix Model

Forward model: $R = F(x)$

Tangent-linear (TL) model: $R_{TL} = \mathbf{H} x_{TL}$

The matrix \mathbf{H} contains the Jacobian element, $\frac{\partial R_i}{\partial x_j}$

Adjoint (AD) model: $x_{AD} = \mathbf{H}^T R_{AD}$

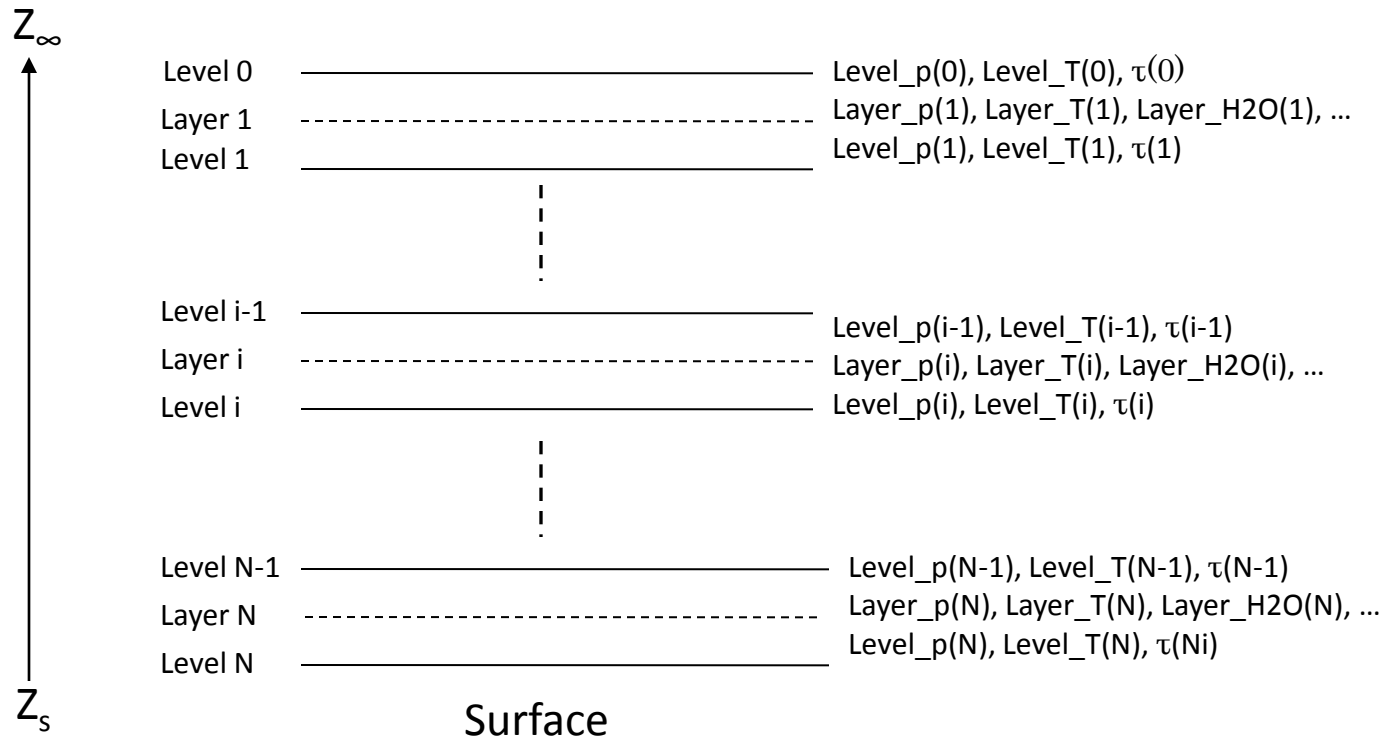
K-matrix (K) model: $x_K = [h_1 R_{K,1}, h_2 R_{K,2}, \dots, h_m R_{K,m}]$

$$h_i = \left[\frac{\partial R_i}{\partial x_1}, \frac{\partial R_i}{\partial x_2}, \dots, \frac{\partial R_i}{\partial x_n} \right]^T$$

Perturbation method:

$$\frac{\delta R}{\delta x} = \frac{F(x + \delta x / 2) - F(x - \delta x / 2)}{\delta x}.$$

Atmosphere Profile Layering Scheme



Example: AIRS science team level pressure definition (101 levels):

$$P_{lev}(i) = (Ai^2 + Bi + C)^{7/2}$$

$$P_{lev}(1) = 0.005 \quad P_{lev}(38) = 300.0 \quad P_{lev}(101) = 1100.0$$

$$A = -1.55 \times 10^{-4}, \quad B = -1.55 \times 10^{-4}, \quad \text{and} \quad C = 7.45$$

Layer pressure definition:

$$P_{layer}(1:N) = (P_{lev}(2:N) - P_{lev}(1:N-1)) / \log(P_{lev}(2:N) / P_{lev}(1:N-1))$$

General Radiative Transfer Equation for clear sky

$$R_\nu = \varepsilon_\nu B_s[\nu, T(z_s)]\tau(\nu, z_s) + (1 - \varepsilon_\nu)\tau(\nu, z_s) \int_1^{\tau(\nu, z_s)} B[\nu, T(z)] d\tau(\nu, z) \\ + \int_{\tau(\nu, z_s)}^1 B[\nu, T(z)] d\tau(\nu, z) + r\mu_0 F_* \tau(\nu, z_s, \mu_0)\tau(\nu, z_s, \mu) / \pi$$

If surface emissivity $\varepsilon_\nu = 1$

$$R_\nu = B_s[\nu, T(z_s)]\tau(\nu, z_s) + \int_{\tau(\nu, z_s)}^1 B[\nu, T(z)] d\tau(\nu, z)$$

Channel radiance received by the satellite sensor

$$R = \frac{\int_{\Delta\nu} \phi(\nu) B_s[\nu, T(z_s)]\tau(\nu, z_s) d\nu + \int_{\Delta\nu} \phi(\nu) \int_{\tau(\nu, z_s)}^1 B[\nu, T(z)] d\tau(\nu, z) d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu}$$

Line-by-Line Radiance

The radiance received by the satellite sensor is computed by convolving the monochromatic radiances with the instrument SRF:

$$R = \frac{\int_{\Delta\nu} \phi(\nu) B_s[\nu, T(z_s)] \tau(\nu, z_s) d\nu + \int_{\Delta\nu} \phi(\nu) \int_{\tau(\nu, z_s)}^1 B[\nu, T(z)] d\tau(\nu, z) d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu}$$

After discretion at z direction

$$R \approx \frac{\int_{\Delta\nu} \phi(\nu) B_s[\nu, T(z_s)] \tau(\nu, z_s) d\nu + \sum_{i=1}^N \int_{\Delta\nu} \phi(\nu) \overline{B[\nu, T_i]} (\tau(\nu, z_{i-1}) - \tau(\nu, z_i)) d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu},$$

Rearrange

$$\begin{aligned} R &= \frac{\int_{\Delta\nu} \phi(\nu) B_s[\nu, T(z_s)] d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu} \frac{\int_{\Delta\nu} \phi(\nu) B_s[\nu, T(z_s)] \tau(\nu, z_s) d\nu}{\int_{\Delta\nu} \phi(\nu) B_s[\nu, T(z_s)] d\nu} \\ &+ \sum_{i=1}^N \frac{\int_{\Delta\nu} \phi(\nu) \overline{B[\nu, T_i]} d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu} \left(\frac{\int_{\Delta\nu} \phi(\nu) \overline{B[\nu, T_i]} \tau(\nu, z_{i-1}) d\nu}{\int_{\Delta\nu} \phi(\nu) \overline{B[\nu, T_i]} d\nu} - \frac{\int_{\Delta\nu} \phi(\nu) \overline{B[\nu, T_i]} \tau(\nu, z_i) d\nu}{\int_{\Delta\nu} \phi(\nu) \overline{B[\nu, T_i]} d\nu} \right) \\ &\approx \frac{\int_{\Delta\nu} \phi(\nu) B_s[\nu, T(z_s)] d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu} \tau_s + \sum_{i=1}^N \frac{\int_{\Delta\nu} \phi(\nu) \overline{B[\nu, T_i]} d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu} (\tau_{i-1} - \tau_i) \end{aligned}$$

Fast Model Approximations

Approximation 1 (Ordinary Transmittance), the variation of the Planck radiances within the channel spectra is not considered when calculating channel transmittance:

$$\tau_i^{ORD} = \frac{\int \phi(\nu) \tau_i(\nu) d\nu}{\int \phi(\nu) d\nu}$$

Approximation 2 (PW1), the layer temperature is used to calculate the Planck-weighted channel transmittance

$$\tau_i^{PW1} = \frac{\int \phi(\nu) B[\nu, \bar{T}_i] \tau_i(\nu) d\nu}{\int \phi(\nu) B[\nu, \bar{T}_i] d\nu}$$

Approximation 3 (PW2), the level temperature is used to calculate the Planck-weighted channel transmittance

$$\tau_i^{PW2} = \frac{\int \phi(\nu) B[\nu, T_i] \tau_i(\nu) d\nu}{\int \phi(\nu) B[\nu, T_i] d\nu}$$

Sensor Channel Band Correction

Convert the channel radiance to channel Brightness Temperature (BT)

Channel central wavenumber ν_i

$$\nu_i = \frac{\int \phi(\nu) \nu d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu}$$

For each channel, the channel effective brightness temperature T_e at the center wavenumber ν_i is calculated for the blackbody temperature T over SRF

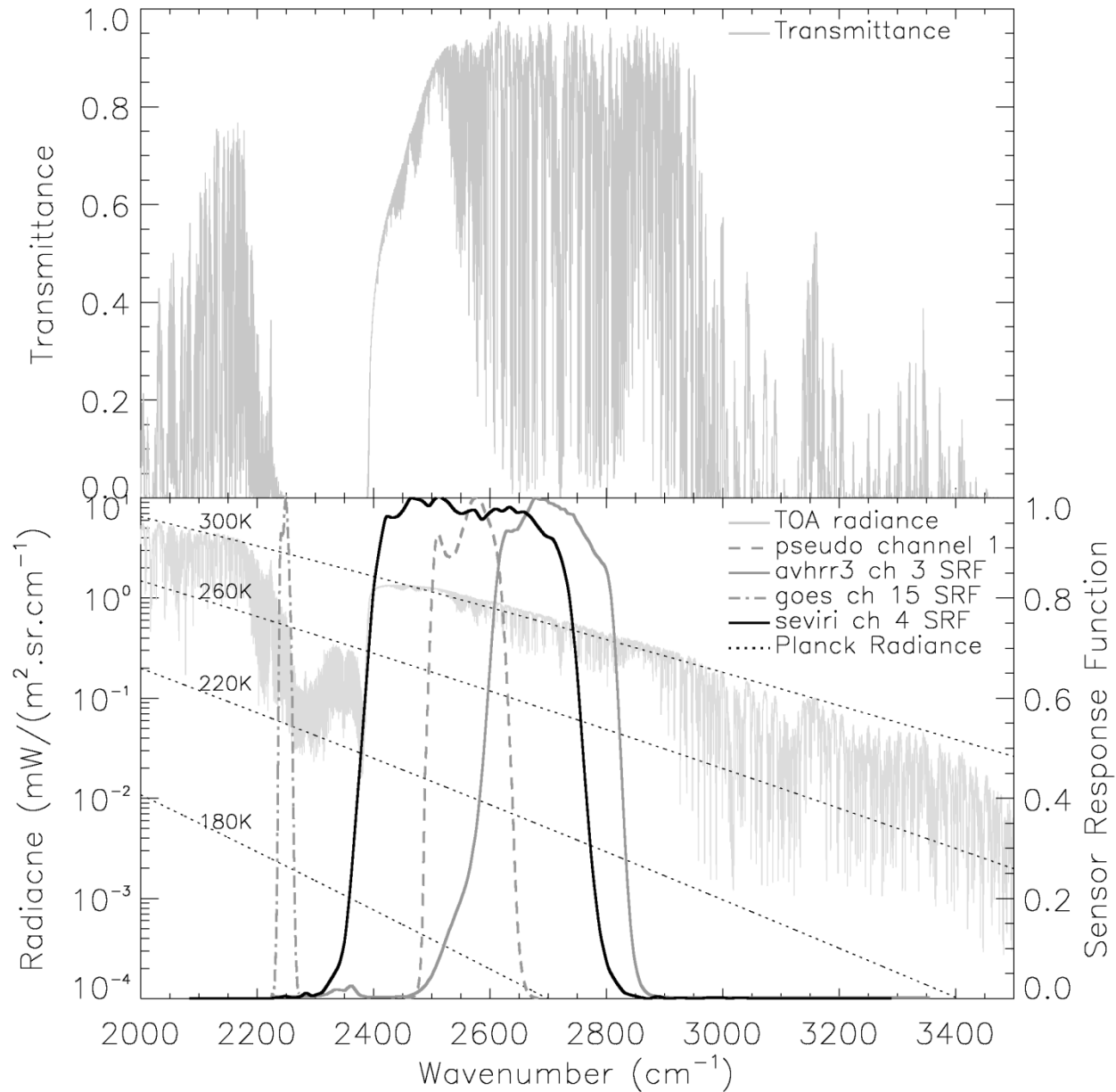
$$R = \frac{c_1 \nu_i^3}{e^{c_2 \nu_i / T_e} - 1} = \frac{\int \phi(\nu) B[\nu, T] d\nu}{\int_{\Delta\nu} \phi(\nu) d\nu}$$

A linear relationship between T and T_e is established by ranging T from 150 to 340 K

$$T_e = b + b_1 T$$

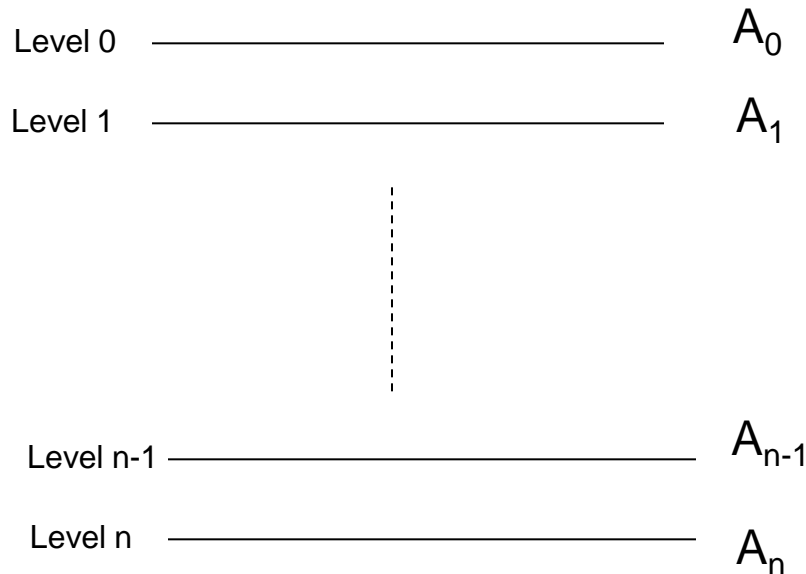
The band correction coefficient b is a very good indicator for Planck radiance variation across the channel SRF.

Atmosphere Radiance and Transmittance



Gaseous Transmittance Model 1 (AtmAbsorption)

Compact OPTRAN (ODAS)



$$A_i = \int_0^p \frac{r_i}{g \cos(\theta)} dp'$$

$$\ln(k_{ch}(A)) = c_0(A) + \sum_{j=1}^6 c_j(A) P_j(A)$$

$$c_j(A) = \sum_{m=0}^n a_{j,m} \ln(A)^m, \quad j = 0, 6, \quad n < 10$$

$$\tau_{ch} = \exp(-k_{ch} \delta A)$$

estimate layer
transmittance

$$\tau_{ch} := \int \tau_v \phi_v d\nu$$

Channel transmittance
definition

ϕ_v – spectral response function

K – absorption coefficient of an absorber

A – integrated absorber amount

P_j – predictors

a_j – constants obtained from regression

- Currently H₂O and O₃ are the only variable trace gases and other trace gases are “fixed”.
- The model provides good Jacobians and is very efficient in using computer memory

Gaseous Transmittance Model 2 (AtmAbsorption) ODPS (Optical Depth in Pressure Space)

Regression formulation:

$$d_i - d_{i-1} = \sum_{j=1}^{N_p} c_{i,j} X_{i,j},$$

$(d_i - d_{i-1})$ – the layer optical depth

d_i – the level to space optical depth from level i

N_p – the number of predictors at layer i

$c_{i,j}$ – the regression coefficients

$X_{i,j}$ – the predictors

The regression is actually performed in terms of its departure from a reference profile for all variable gases.

- Variable gases H₂O, CO₂, O₃, and can add absorbers N₂O, CO, and CH₄ for hyper-spectral IR sensors: IASI, AIRS, and CrIS.
- Other features:
 - (1) Water vapor line computed using ODAS (optional)
 - (2) Water vapor continua transmittance is treated separately from the water vapor line absorption.
 - (3) Have reference profile, and each absorber has associated min and max values.

Water Line Predictors in Different Transmittance Models

	ODPS	Optran	ODAS
Models	Method A ^b	Method B	Method C
Predictors	$\sec(\theta)W_r, \sec(\theta)W_r\delta T,$ $(\sec(\theta)W_r)^2, \sec(\theta)W_r\delta T \delta T ,$ $\sqrt[4]{\sec(\theta)W_r}, (\sec(\theta)W_r)^3,$ $\sqrt{\sec(\theta)W_r}, \sqrt{\sec(\theta)W_r\delta T},$ $(\sec(\theta)W_r)^4, W_r/W_{tw},$ $\sec(\theta)W_r^2/W_{tw},$ $(\sec(\theta)W_w)^2, \sec(\theta)W_w,$ $\sec(\theta), \sec(\theta)C_r$	$T_x, P_x, T_x^2, P_x^2, T_x P_x,$ $T_x^2 P_x, T_x P_x^2, T_x^2 P_x^2,$ $P_x^4, T_x^2 P_x^4, W, W/T_x^2,$ $T_x^* P_x^*, T_x^{**} P_x^{**}, P_x^{***} P_x^{***},$ $T_x^{***} P_x^{***}$	$T, P, T^2, P^2, TP,$ $T^2 P, TP^2, T^2 P^2,$ $\sqrt[4]{P}, W, W/T^2, T^*,$ $P^*, T^{**}, P^{**}, T^{***},$ P^{***}

^aWhere $T_x = T/100(K)$, $P_x = \sqrt[4]{P(\text{hPa})}$, W is water vapor mixing ratio (g/kg), T is temperature (K), and P is pressure (hPa).

$$T_x^*(l) = \sum_{i=1}^l [(T_x(i) + T_x(i-1))(A(i) - A(i-1))]/(2A^2(l)),$$

$$T_x^{**}(l) = \sum_{i=1}^l [(T_x(i)A(i) + T_x(i-1)A(i-1))(A(i) - A(i-1))]/(2A^2(l)),$$

$$T_x^{***}(l) = \sum_{i=1}^l [(T_x(i)A^2(i) + T_x(i-1)A^2(i-1))(A(i) - A(i-1))]/(2A^3(l)),$$

where $A(i)$ is the i th level integrated absorber amount for water vapor. The same equations applied to P_x^* , P_x^{**} , P_x^{***} , T^* , T^{**} , T^{***} , P^* , P^{**} , and P^{***} for methods B and C.

$$W_r(l) = W(l)/W^*(l),$$

$$C_r(l) = CO_2(l)/CO_2^*(l),$$

$$\delta T(l) = T(l) - T^*(l),$$

$$W_w(l) = \{\sum_{i=1}^l P(i)[P(i) - P(i-1)]W(i)\}/\{\sum_{i=1}^l P(i)[P(i) - P(i-1)]W^*(i)\},$$

$$W_{tw}(l) = \{\sum_{i=1}^l P(i)[P(i) - P(i-1)]W(i)T(i)\}/\{\sum_{i=1}^l P(i)[P(i) - P(i-1)]W^*(i)T^*(i)\}.$$

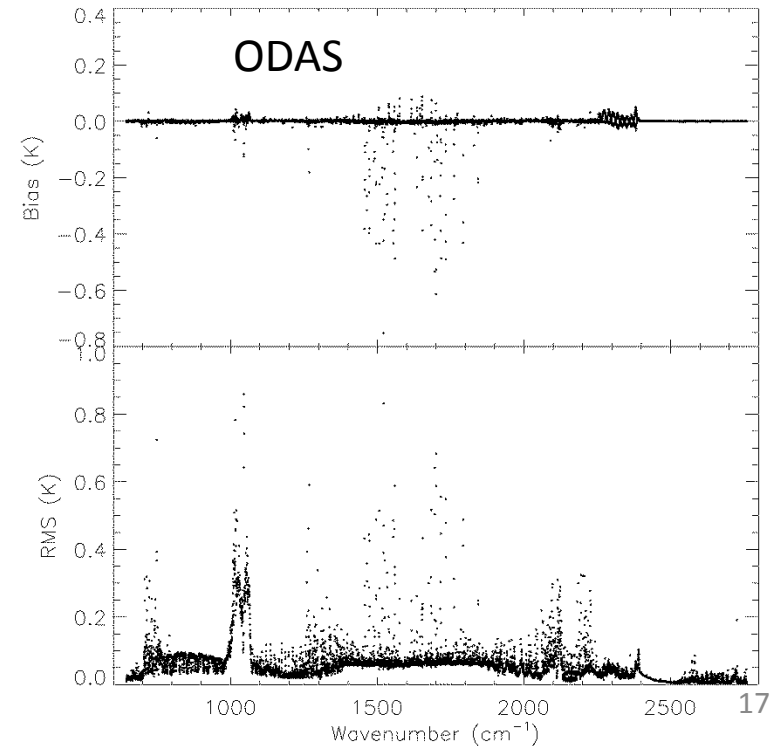
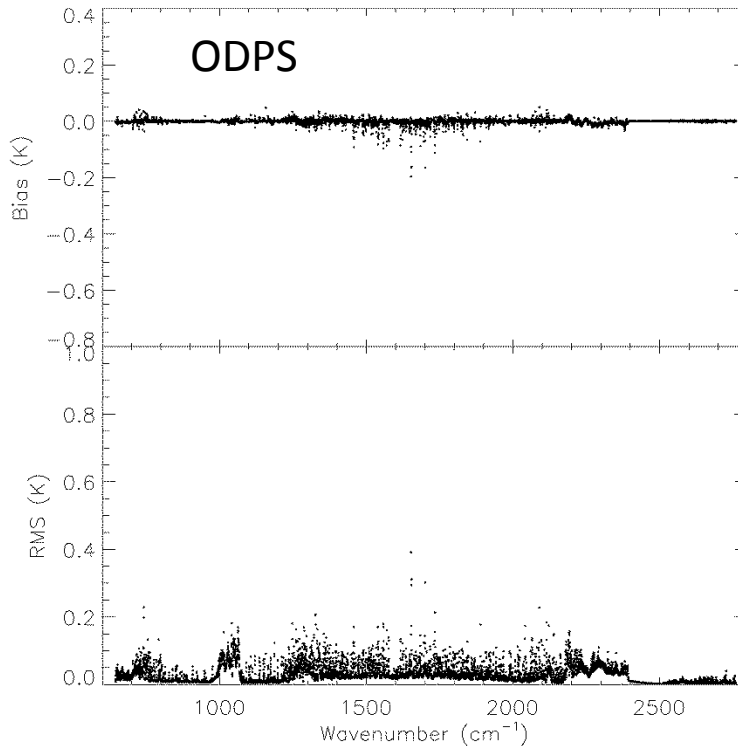
The asterisk refers to the value from reference profile for method A, and $\sec(\theta)$ is the secant of zenith angle.

^bData are from *Matricardi et al.* [2004].

ODPS vs ODAS

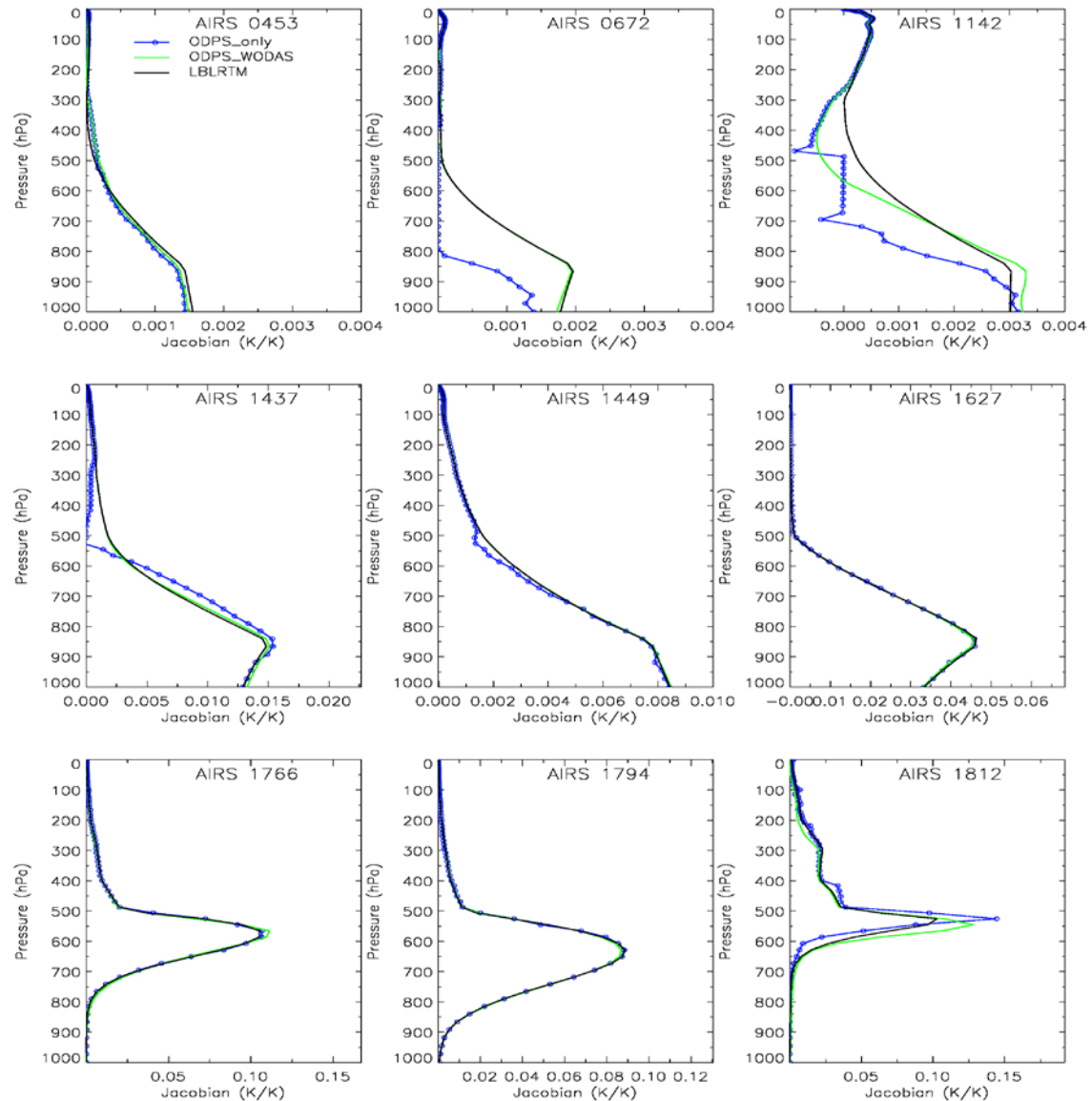
	ODPS (Optical Depth in Pressure Space)	ODAS (Optical Depth in Absorber Space) – CompactOPTRAN
Variable gases	H ₂ O, CO ₂ , O ₃ , and can add absorbers N ₂ O, CO, and CH ₄ for hyper-spectral IR sensors: IASI, AIRS, and CrIS.	Only H ₂ O, and O ₃
Other features	(1) Water vapor line computed using ODAS (optional) (2) Water vapor continua transmittance is treated separately from the water vapor line absorption. (3) Have reference profile, and each absorber has associated min and max values.	

Training accuracy for IASI



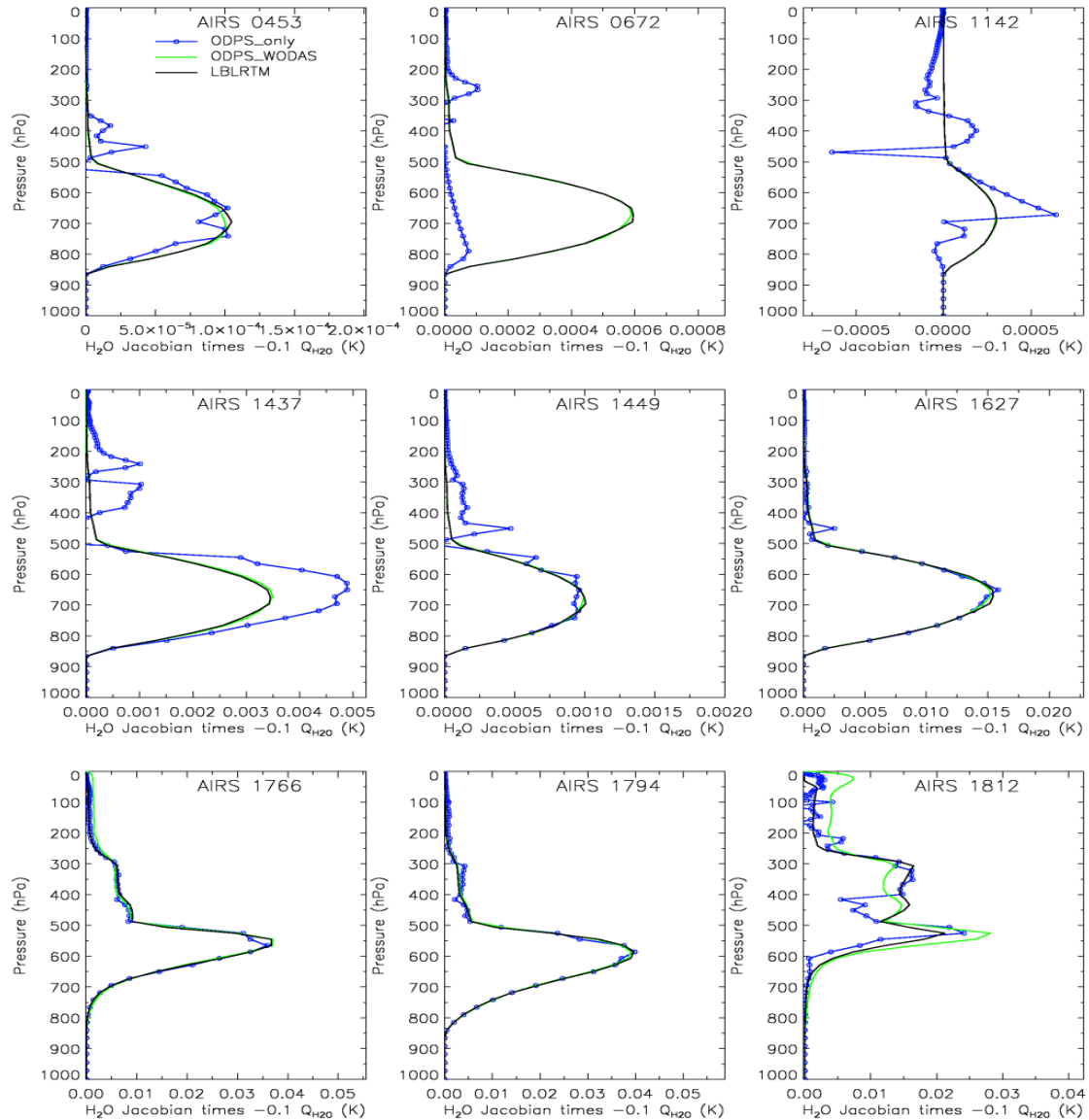
ODPS vs ODAS

- In the ODPS transmittance model, the ODAS (OPTRAN) algorithm is used (optional) to compute water vapor line transmittances since it can provide better forward results and Jacobians for many IR channels.
- Preliminary results have shown positive NWP impacts from temperature related fields when the ODPS plus ODAS for H₂O line is used, compared to the use of ODPS alone.



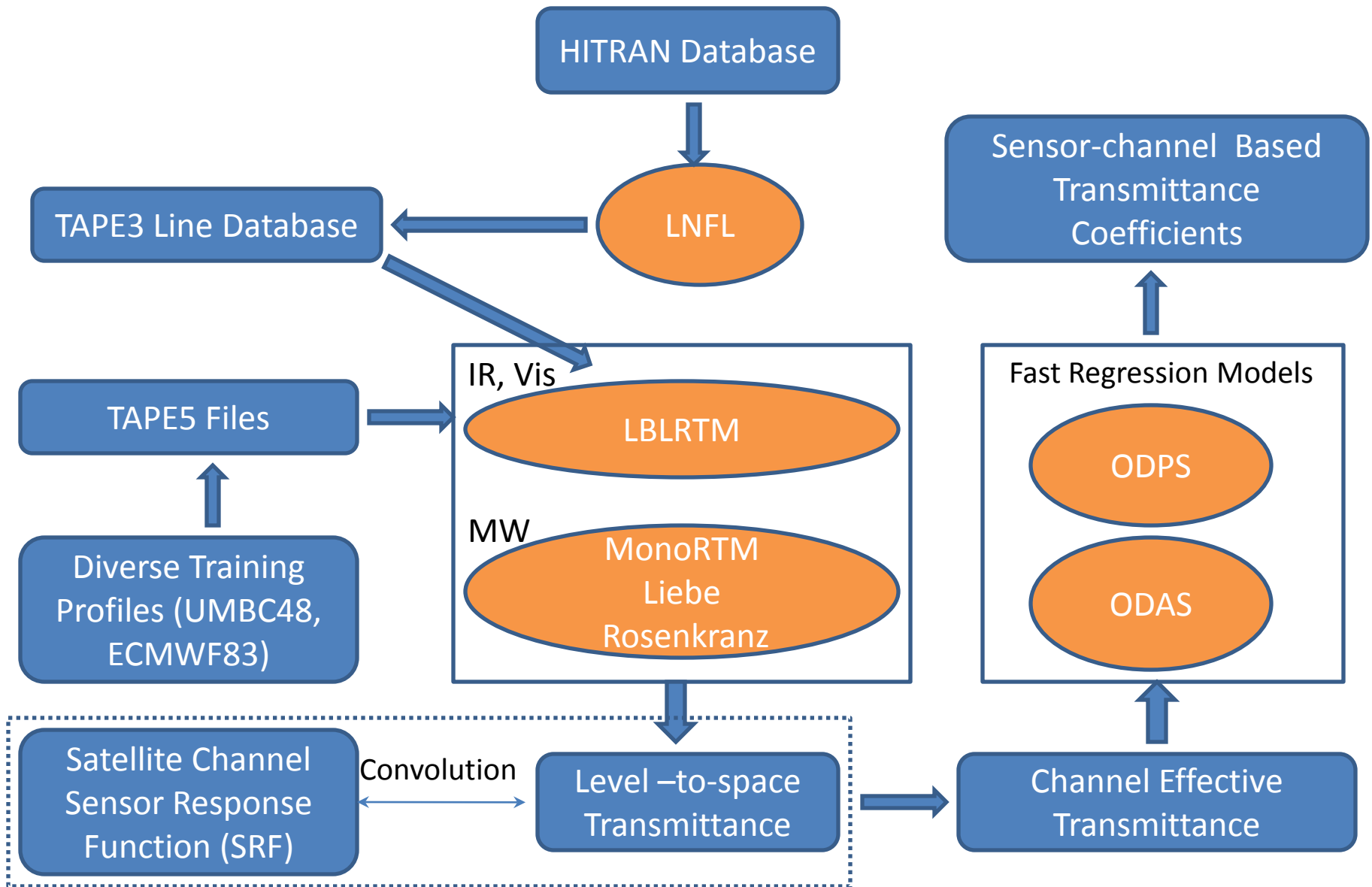
Temperature Jacobians

ODPS vs ODAS

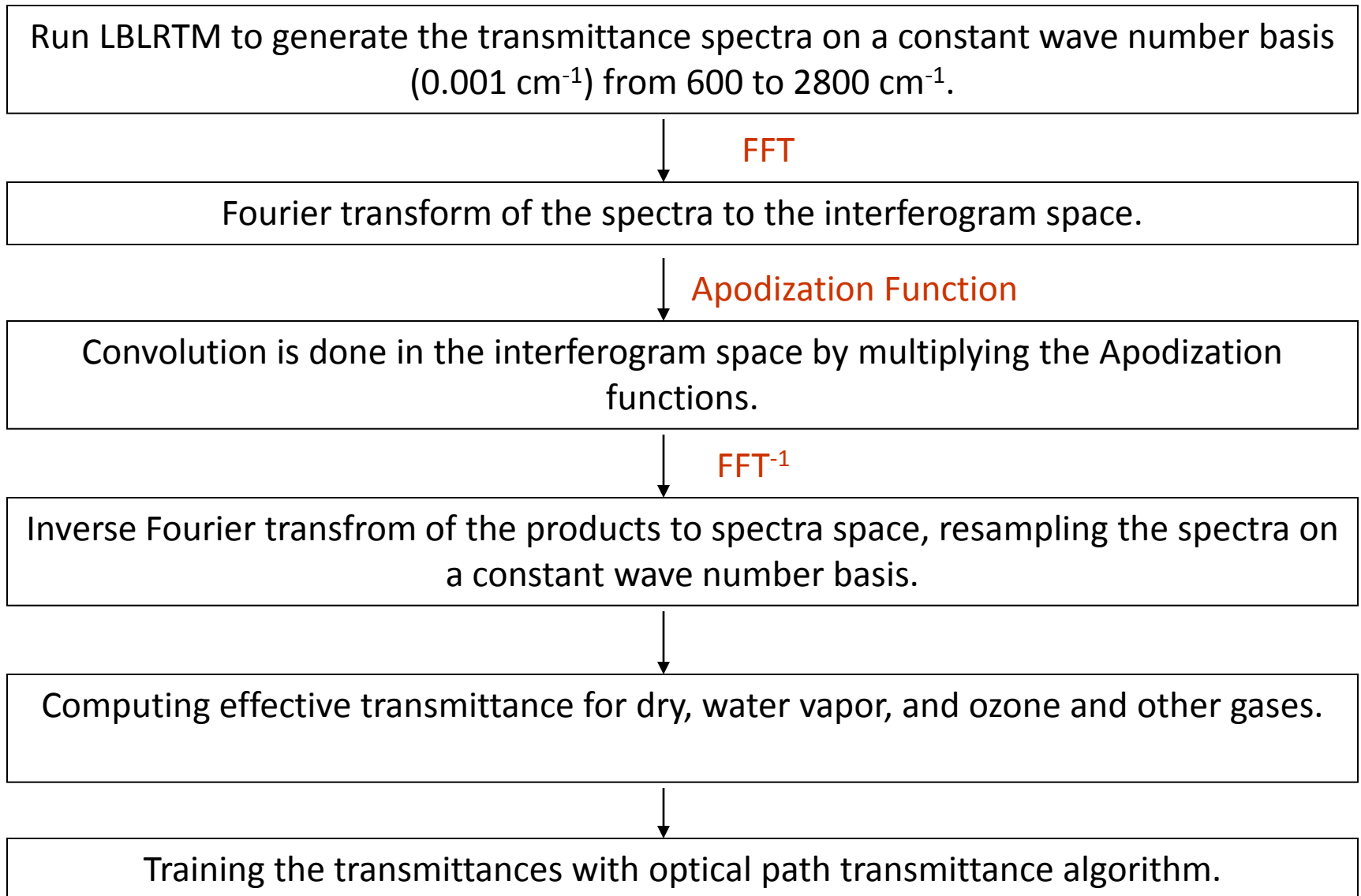


Water Vapor Jacobian

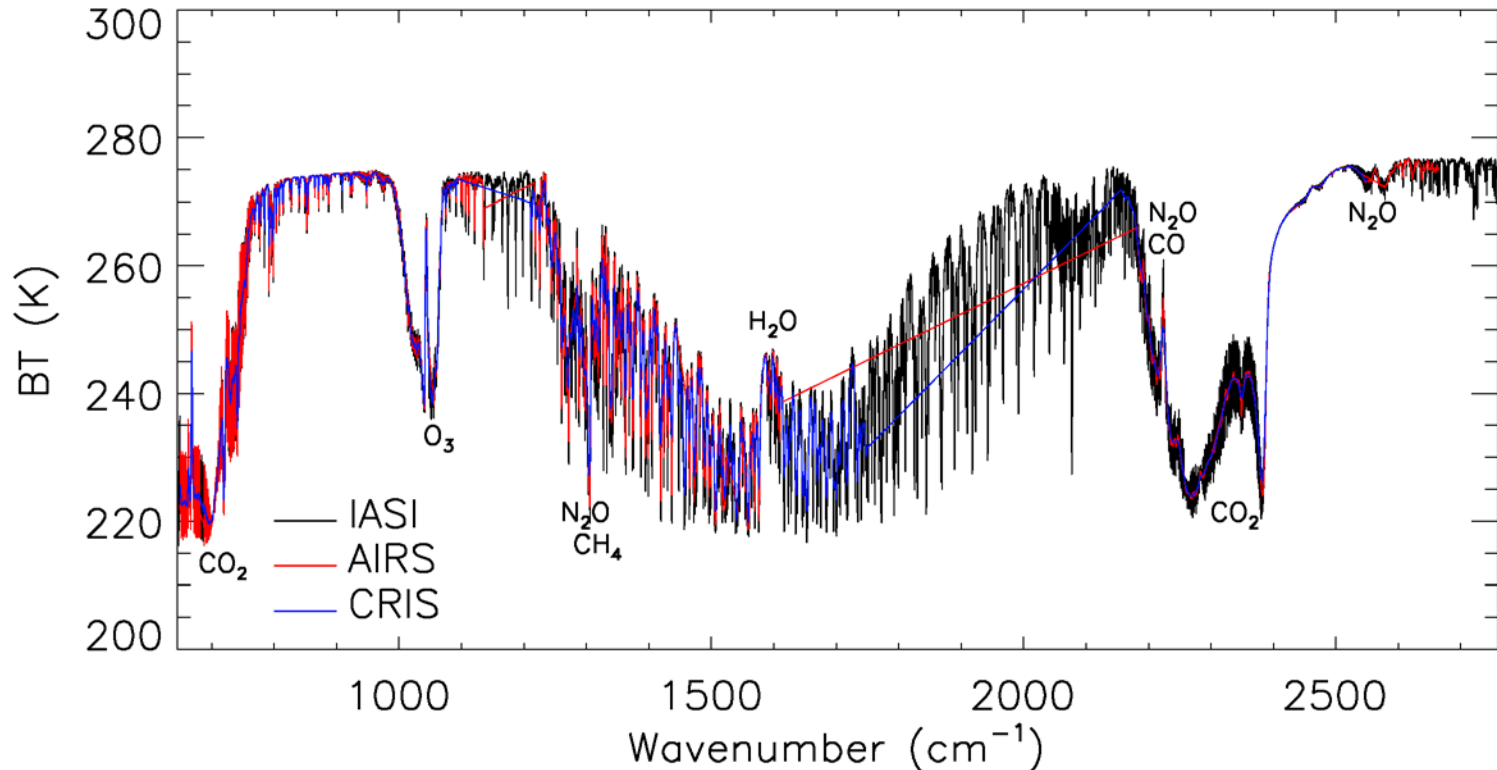
CRTM Coefficients Training Process



Process of generating fast model IASI, CrIS coefficients



CRTM Infrared Spectroscopy Corresponding to AIRS, IASI and CrIS



Variable gases: H_2O , CO_2 , O_3 , CO , CH_4 , and N_2O , **Effective Transmittance**

$$\tau_{v,j}^{\text{tot}} = \tau_{v,j}^{\text{wvcon}} \tau_{v,j}^{\text{fix}} \left(\frac{\tau_{v,j}^{\text{fix}+\text{CH}_4}}{\tau_{v,j}^{\text{fix}}} \right) \left(\frac{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}}}{\tau_{v,j}^{\text{fix}+\text{CH}_4}} \right) \left(\frac{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}+\text{N}_2\text{O}}}{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}}} \right) \left(\frac{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}+\text{N}_2\text{O}+\text{CO}_2}}{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}+\text{N}_2\text{O}}} \right) \times$$

$$\left(\frac{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}+\text{N}_2\text{O}+\text{CO}_2+\text{wv}}}{\tau_{v,j}^{\text{wvcon}} \tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}+\text{N}_2\text{O}+\text{CO}_2}} \right) \left(\frac{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}+\text{N}_2\text{O}+\text{CO}_2+\text{wv}+\text{O}_3}}{\tau_{v,j}^{\text{fix}+\text{CH}_4+\text{CO}+\text{N}_2\text{O}+\text{CO}_2+\text{wv}}} \right)$$

Fast Transmittance Model for Stratospheric Sounding Unit (SSU)

- Stratospheric Sounding Unit data is a three-channel sensor in the CO₂ 15 μm absorption band onboard NOAA series satellites (started from TIROS-N in 1978 and ended at NOAA-14 in 2006).
- The data in past 29 years is an unique near-global source on temperature for middle and upper stratosphere.
- The SSU data has been extensively used to study the temperature trends in the stratosphere, as well as their possible causes (e.g. Nash and Forrester, 1986; Ramaswamy et al., 2001; Shine et al., 2003; World Meteorological Organization (WMO), 1988, 2007; Liu and Weng, 2009).

SSU Sensor Response Function (SRF)

Different from a conventional sensor response function, the SSU SRF is a product of traditional broadband and the CO₂ cell absorption line responses.

SSU SRF = $G_v H_v$

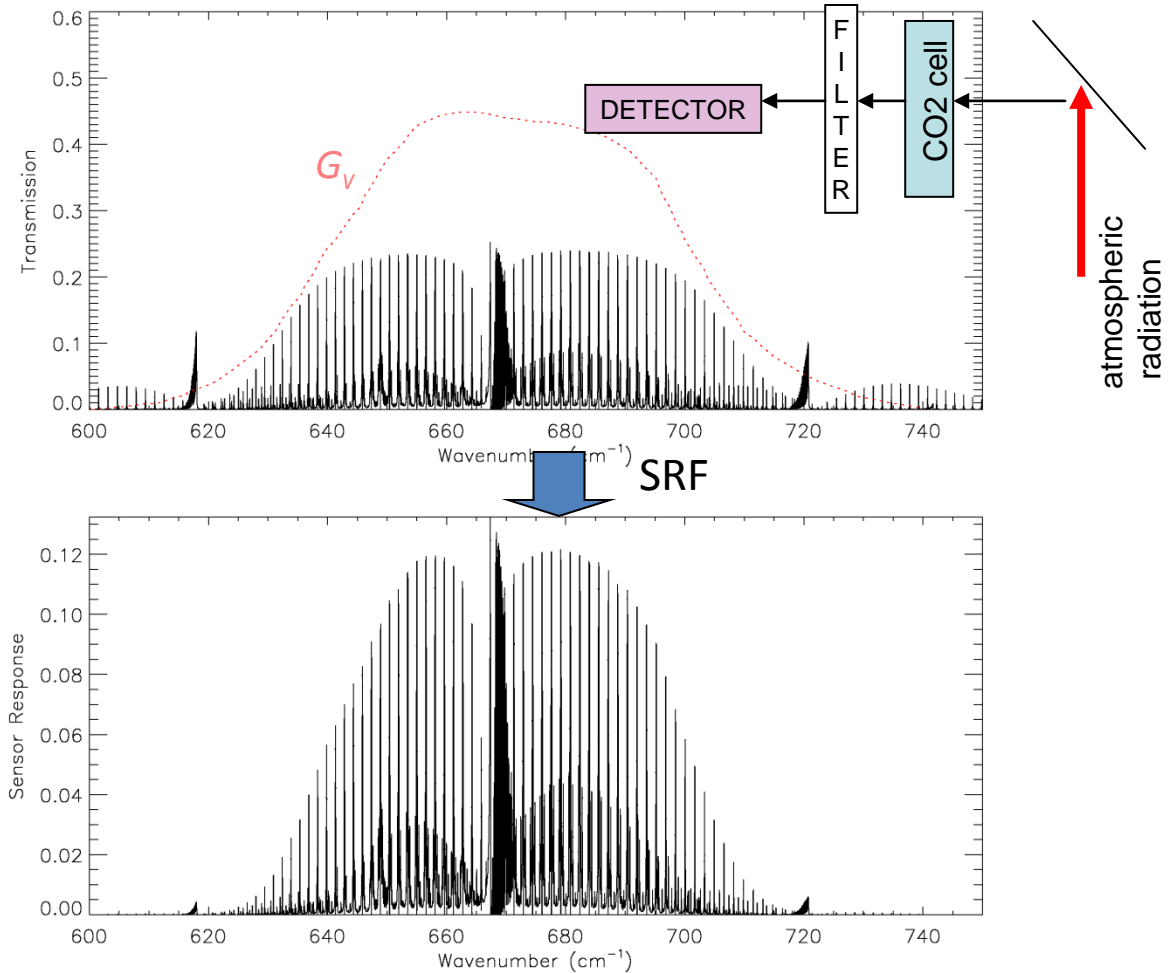
Filter function \rightarrow G_v \leftarrow High-frequency gas cell response

Two cell approximation
(Brindley et al., 1998):

$$H_v = \tau_v^{low\ p\ cell} - \tau_v^{high\ p\ cell}$$

Transmittance of the low CO₂ pressure cell

Transmittance of the high CO₂ pressure cell

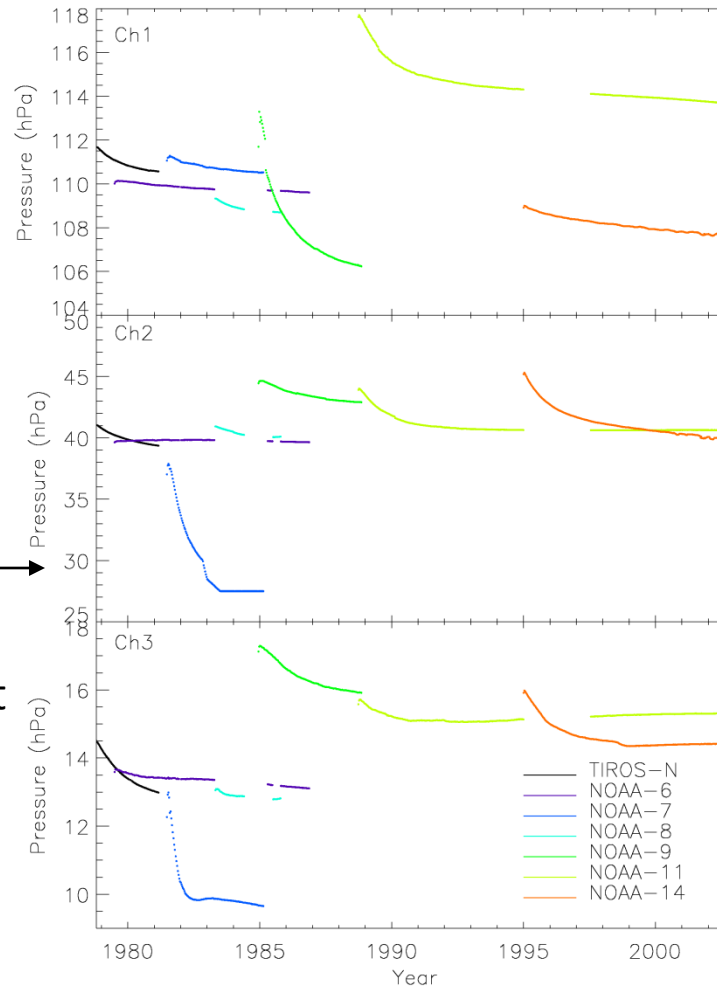


SSU Fast RT Model Taking CO₂ leaking into Account

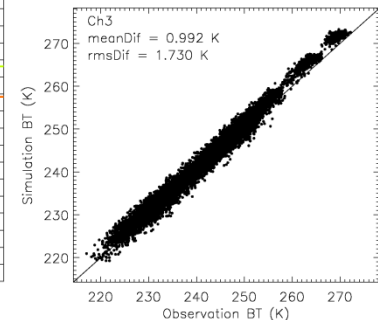
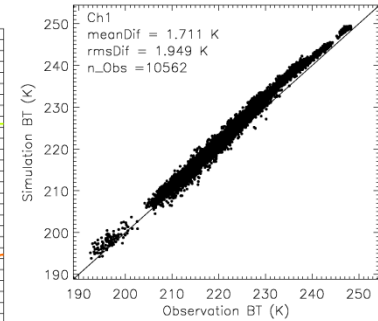
- Based on the sensitivity studies, the fast RT model for SSU utilizes a spectral resolution of $5 \times 10^{-4} \text{ cm}^{-1}$
- CO₂ and O₃ as variable gases.
- The fast model (implemented in CRTM version 2) takes account of the variations of the cell pressures:
 - Use a series of the transmittance coefficient sets for each sensor at different values of CO₂ cell pressure with corresponding SRF.
 - The transmittances at an arbitrary value of CO₂ cell pressure are obtained through interpolation from the transmittances computed at two adjacent CO₂ cell pressure nodes which bracket the desired value.
- It can also be used to address two important corrections in deriving trends from SSU measurements: CO₂ cell leaking correction, and atmospheric CO₂ concentration correction.

Fast Transmittance Model for SSU

- The SSU channel spectral response function (SRF) is a combination of the instrument filter function and the transmittance of a CO₂ cell.
- The SRF varies due to the cell CO₂ leaking problem.
- CRTM-v2 includes schemes to take the SRF variations into account (Liu and Weng, 2009; Chen et al. 2011)
- CO₂ and O₃ are variable gases



CO₂ cell pressure variations, which causes SSU SRF variations.



CRTM simulations compared with SSU observations for SSU noaa-14.

Zeeman Effects in CRTM

Energy level splitting:

In the presence of an external magnetic field, each energy level associated with the total angular momentum quantum number J is split into $2J+1$ levels corresponding to the azimuthal quantum number $M = -J, \dots, 0, \dots, J$

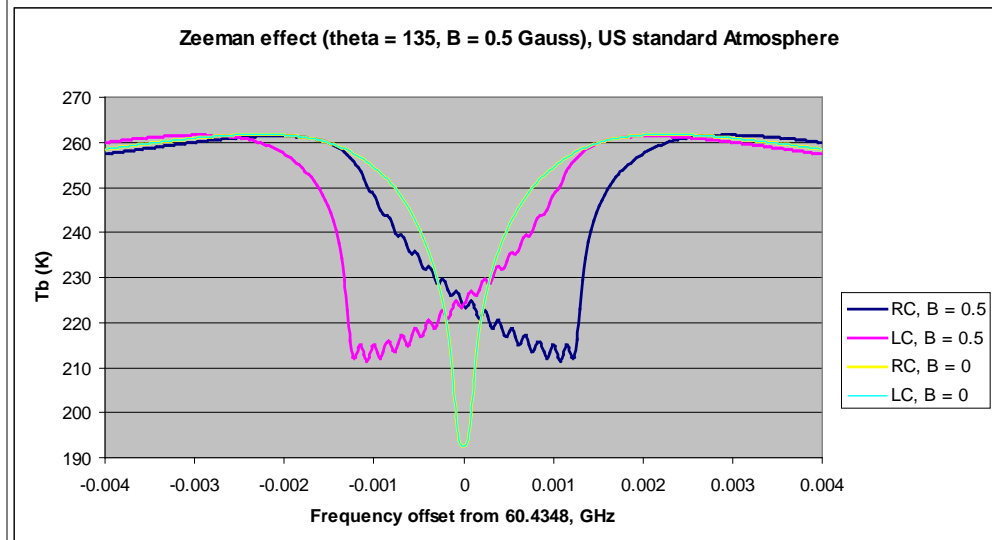
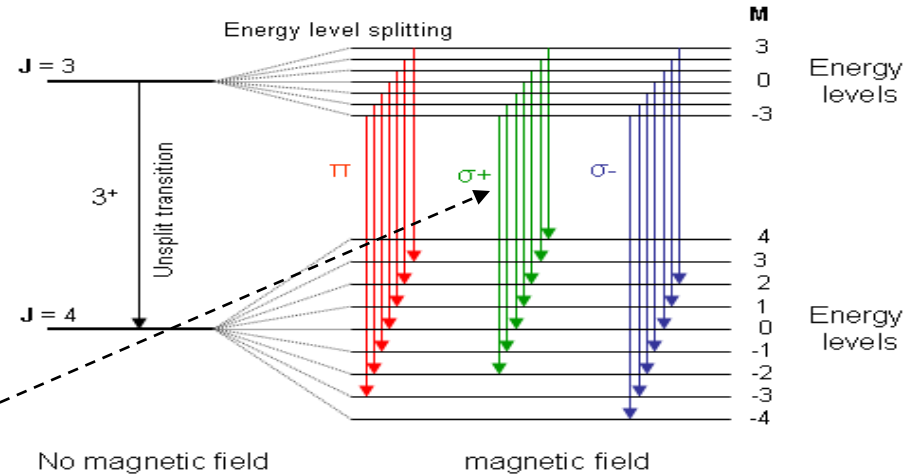
Transition lines (Zeeman components)

The selection rules permit transitions with $\Delta J = \pm 1$ and $\Delta M = 0, \pm 1$. For a change in J (i.g. $J=3$ to $J=4$, represented by 3^+), transitions with

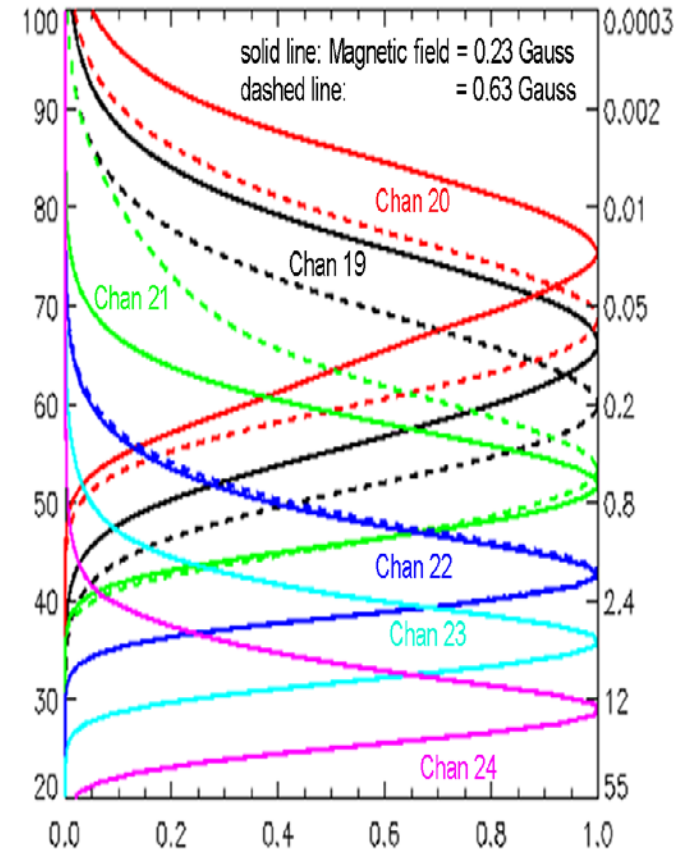
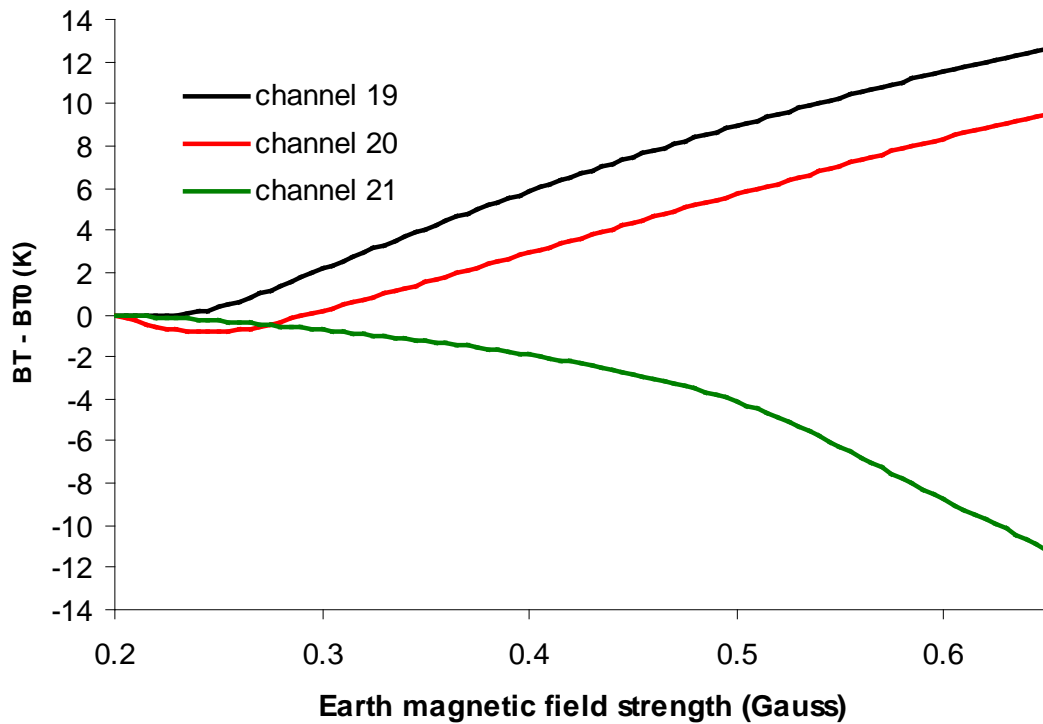
- $\Delta M = 0$ are called π components,
- $\Delta M = 1$ are called $\sigma+$ components and
- $\Delta M = -1$ are called $\sigma-$ components.

Polarization:

The three groups of Zeeman components also exhibit polarization effects with different characteristics. Radiation from these components received by a circularly polarized radiometer such as the SSMIS upper-air channels is a function of the magnetic field strength $|\mathbf{B}|$, the angle θ_B between \mathbf{B} and the wave propagation direction \mathbf{k} as well as the state of atmosphere, not dependent on the azimuthal angle of \mathbf{k} relative to \mathbf{B} .



SSMIS Zeeman Splitting Related Errors



Fast Zeeman Absorption Model

- (1) Atmosphere is vertically divided into N fixed pressure layers from 0.000076 mb (about 110km) to 200 mb. (currently N=100, each layer about 1km thick).
- (2) The Earth's magnetic field is assumed constant vertically
- (3) For each layer, the following regression is applied to derive channel optical depth with a left-circular polarization:

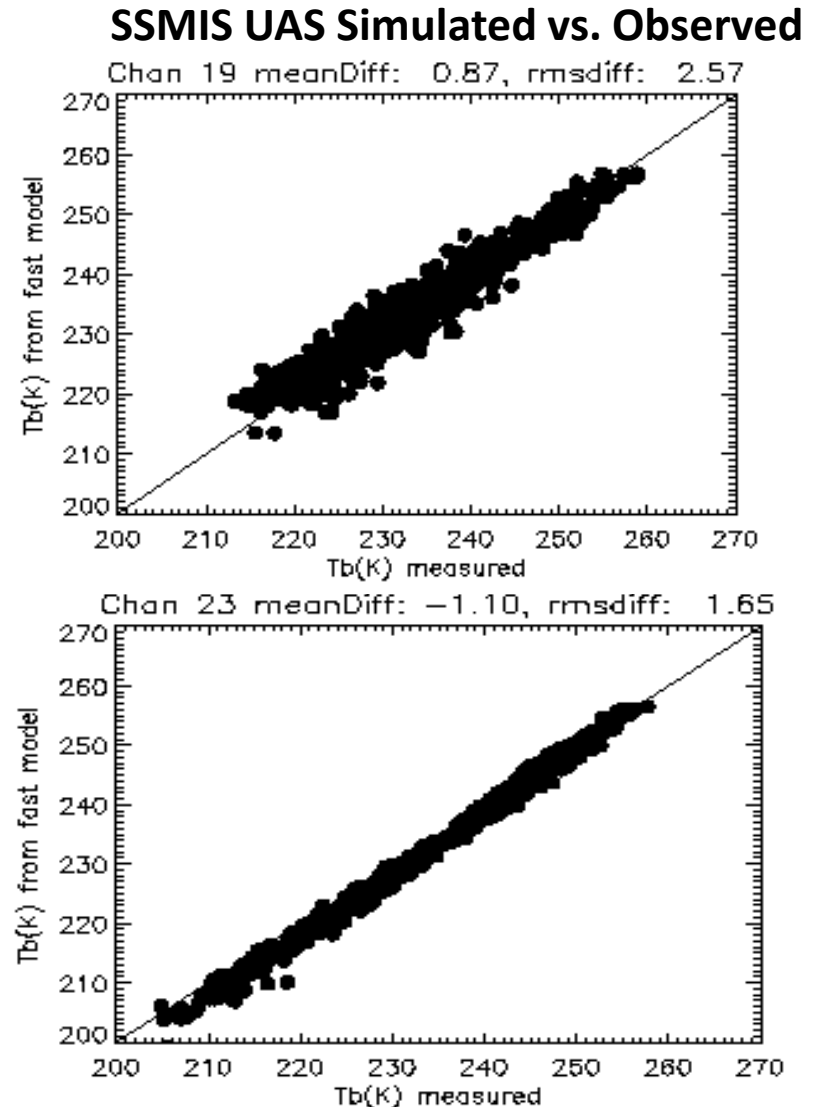
$$\tau_i = \tau_{i-1} \exp(-OD_{lc,i} / \cos(\theta)), \quad \tau_0 = 1$$

$$OD_{lc,i} = c_{i,0} + \sum_{j=1}^m c_{i,j} x_{i,j}$$

$\psi = 300/T$; T – temperature

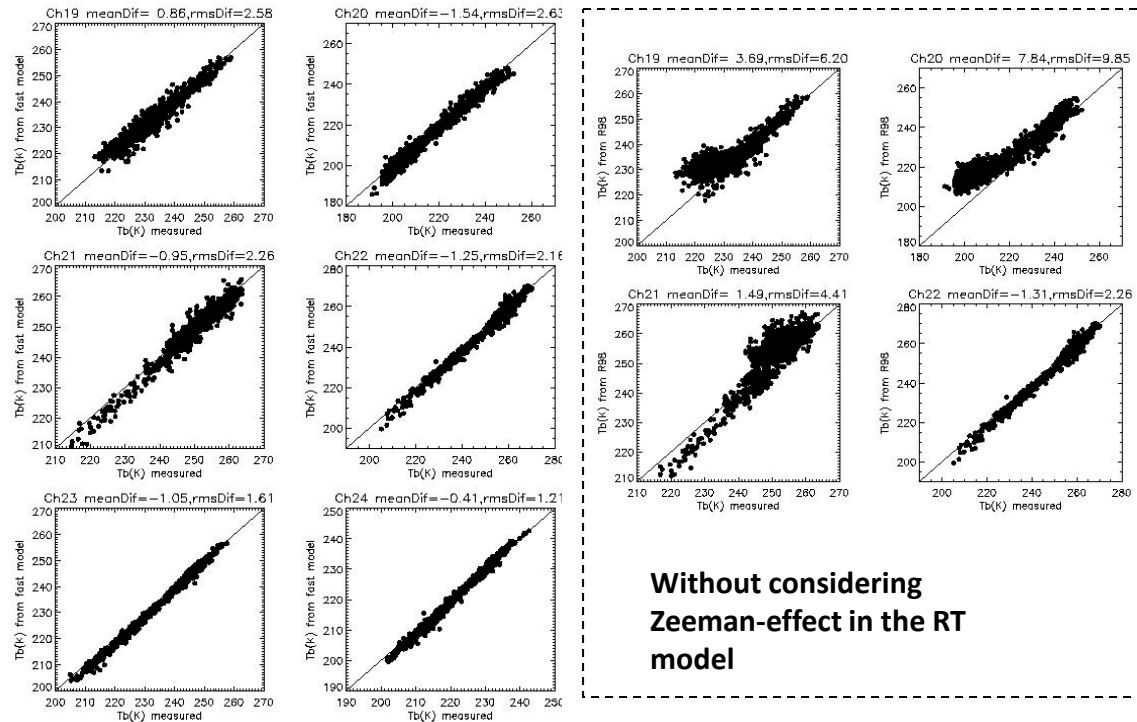
B – Earth magnetic field strength

θ_B – angle between magnetic field and propagation direction



Fast Transmittance Model for SSMIS Upper Atmospheric Sounding (UAS) Channels

- Zeeman-splitting can have an effect up to 10 K on SSMIS UAS channels.
- The Doppler shift from Earth-rotation can have an effect up to 2 K on SSMIS UAS channels.
- Fast transmittance algorithms are implemented to take both effects into account.



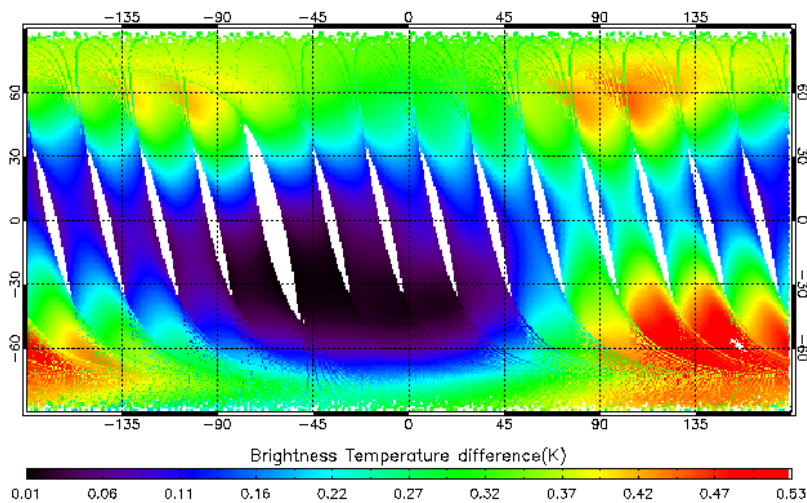
CRTM simulations compared to observations (SSMIS f16)

AMSU-A Channel-14 Brightness Temperature Differences Between RT Models w/o Zeeman-splitting Effect

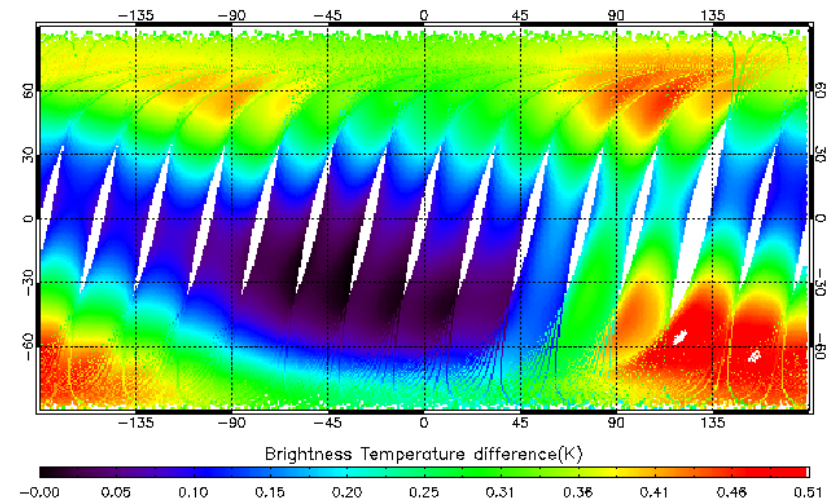
Model inputs:

B_e , θ_e , Φ_e – calculated using IGRF10 and data from AMSU-A MetOp-a 1B data files on September 8, 2007.

Atmospheric profile – US standard atmosphere applied over all regions.



Ascending

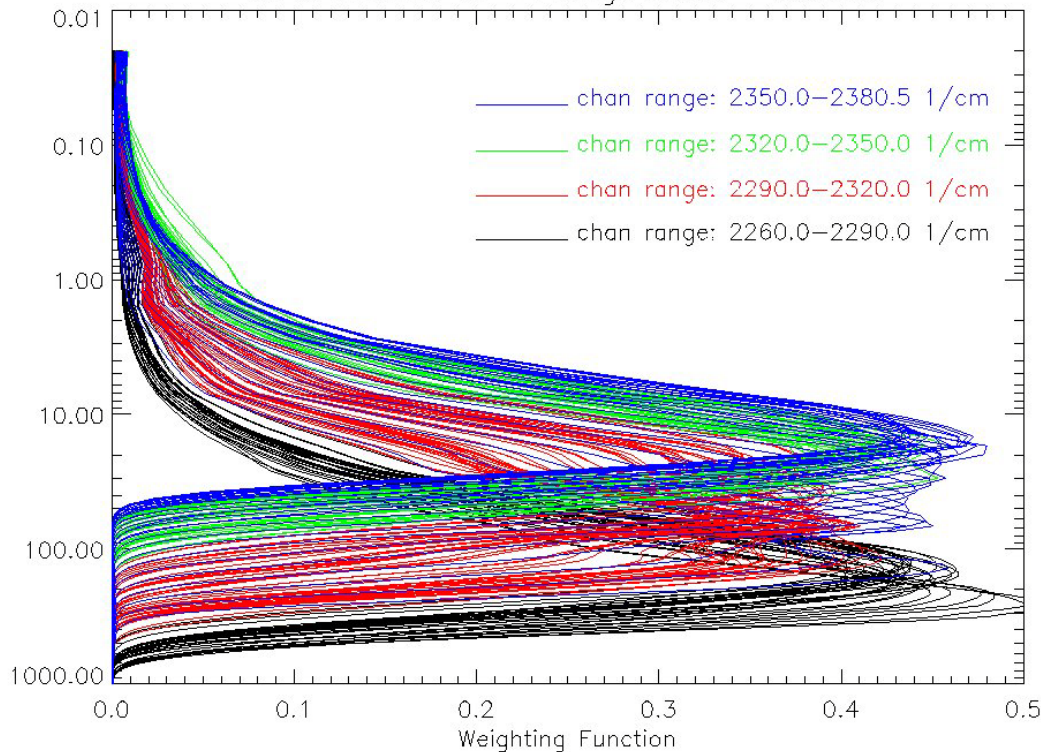


Descending

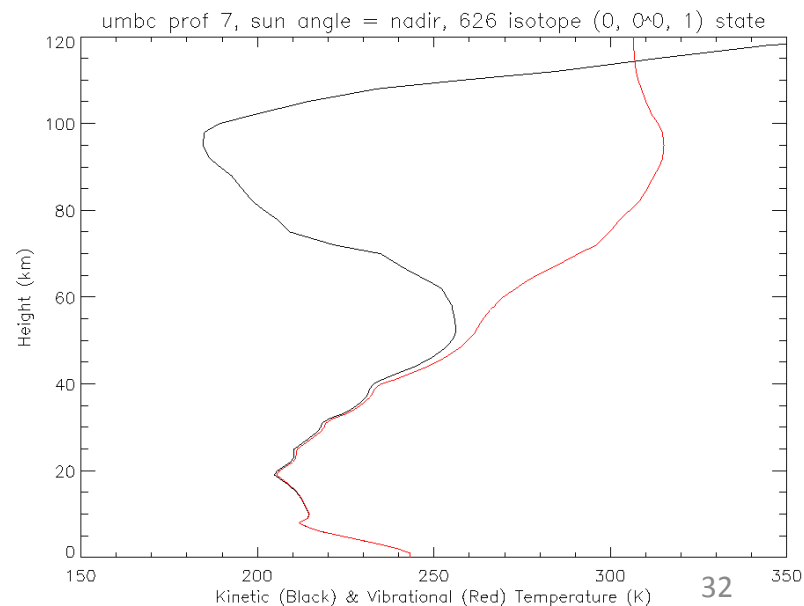
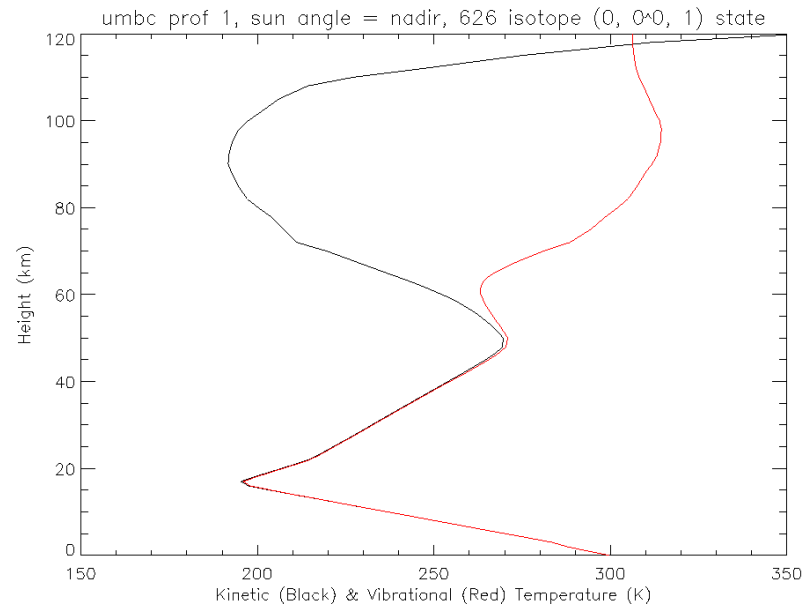
Non-Local Thermodynamic Equilibrium (NLTE) Module in CRTM

Weighting functions in shortwave region
affected by NLTE

AIRS channel WF in range 2260 – 2380.5



vibrational temperature



Non-Local Thermodynamic Equilibrium (NLTE) Module

$$R_{ch}^{NLTE} = R_{ch}^{LTE} + \Delta R_{ch}$$

$$\Delta R_{ch} = c_0 + \sum_{i=1}^4 c_i x_i$$

Predictors:

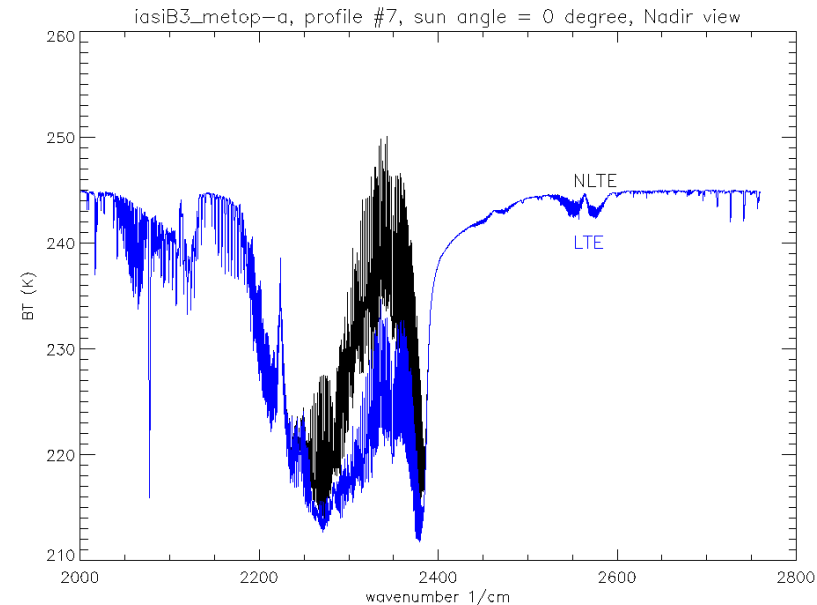
x_1 - Solar angle

x_2 - Mean temperature from 0.005 To 0.2 mb

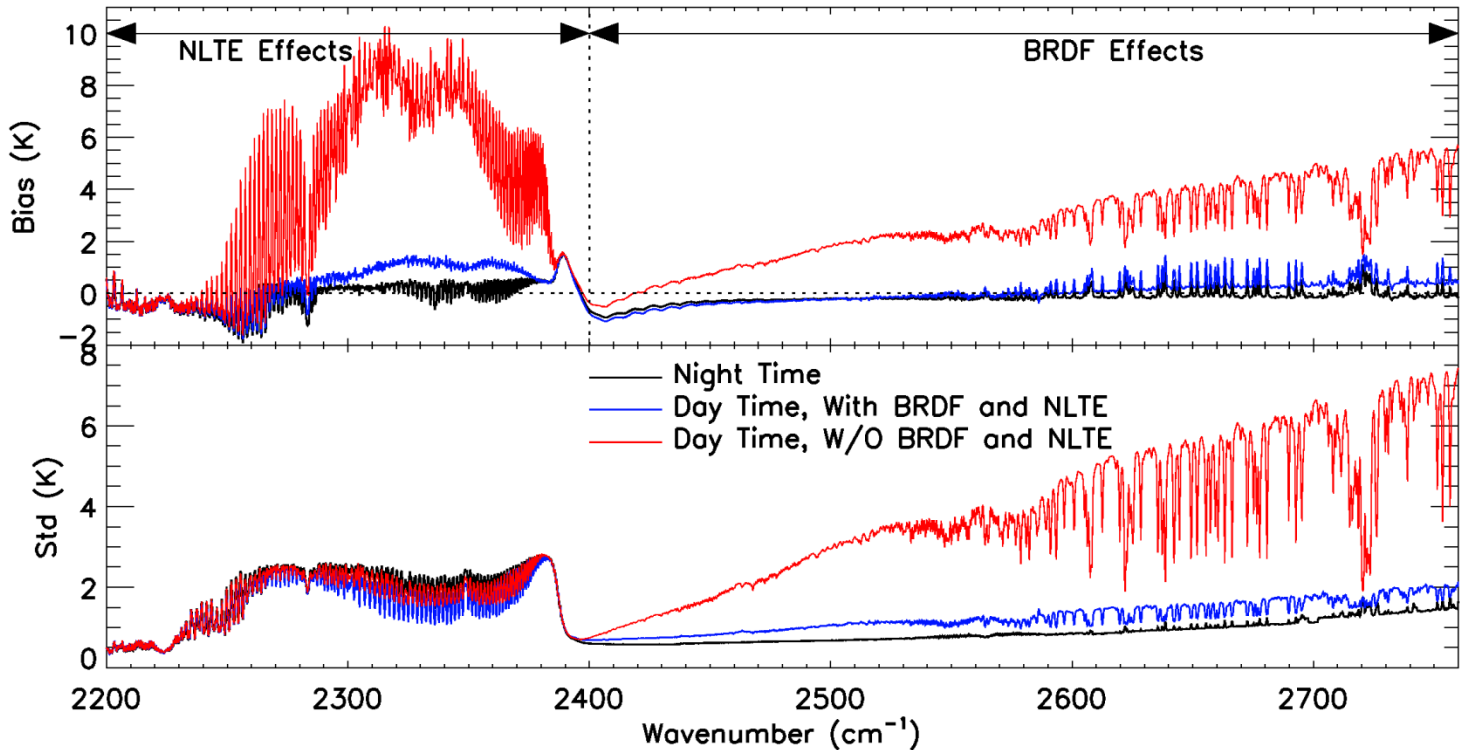
x_3 - Mean temperature from 0.2 To 52 mb

x_4 - Sensor zenith angle at the Earth surface

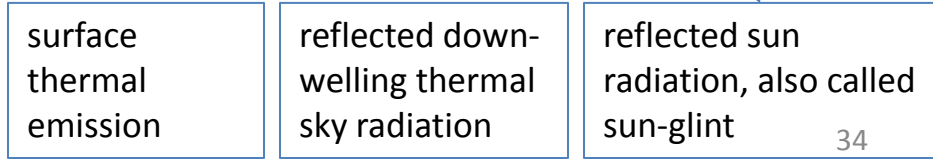
c_i - Regression coefficients, derived from LBLRTM and UMBC 48 profiles.



Validation of Ocean BRDF and NLTE Effects in CRTM by using IASI Data

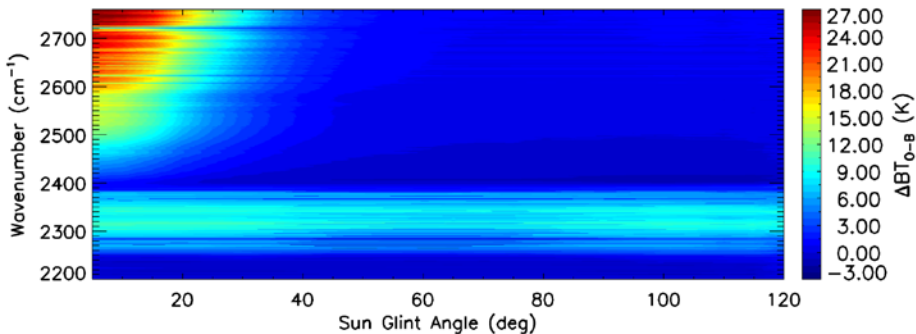
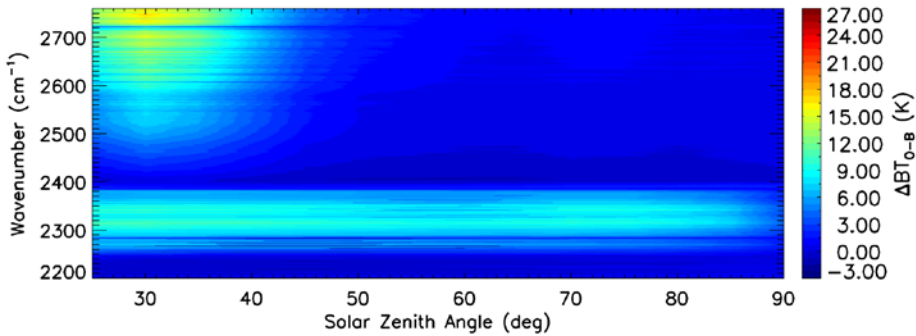


$$I = I_{em} + I_{sky} + I_{sun}$$

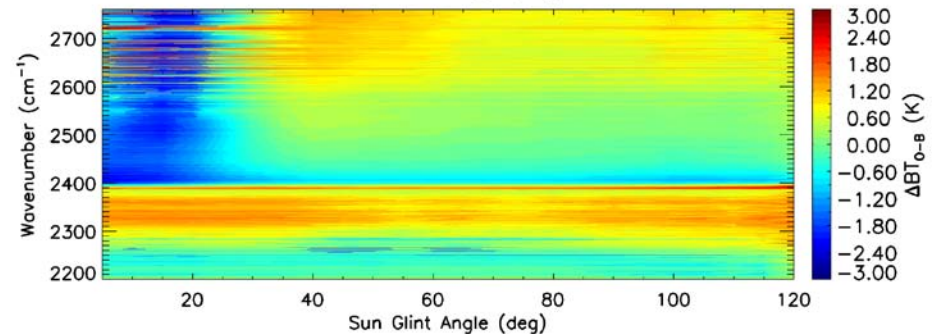
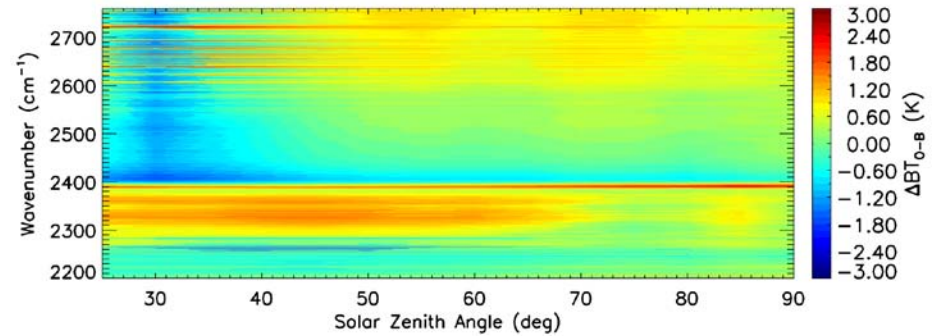


Daytime Biases as a Function of Solar Zenith Angle and Sun Glint Angle

(CRTM v2.0.5 w/o BRDF and NLTE)

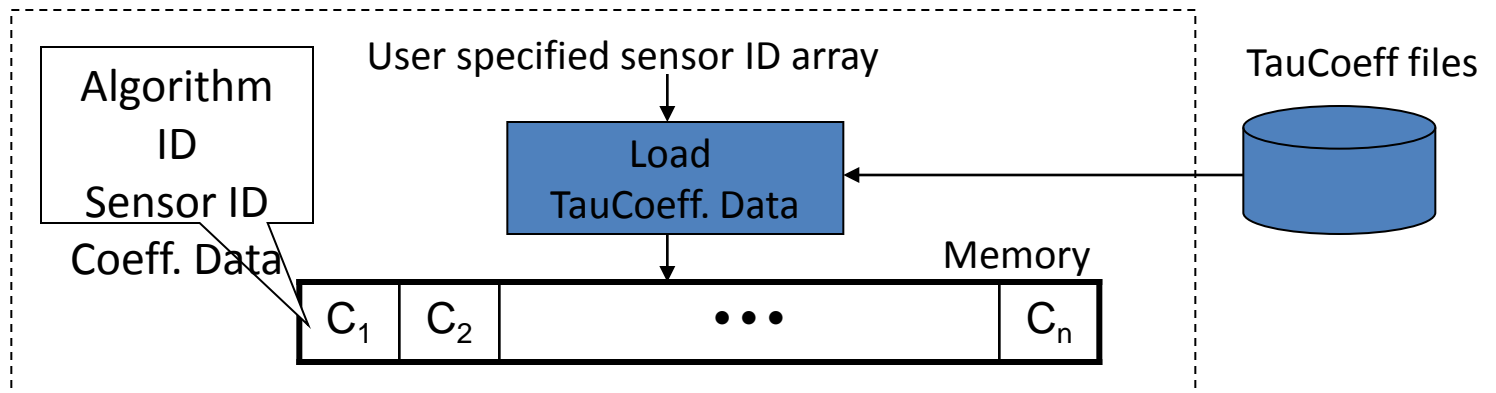


(CRTM v2.1 with NLTE)

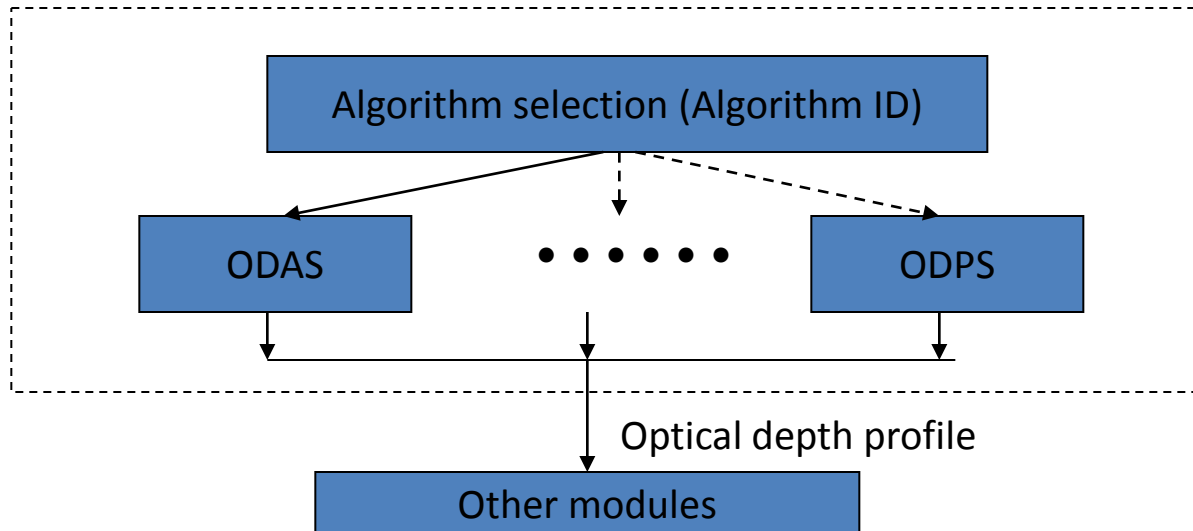


Multiple Transmittance Algorithms Framework

CRTM Initialization: load transmittance coefficient data



CRTM transmittance models: ODAS, ODPS, ODSSU, ODZeeman



CRTM Aerosol Scattering Module

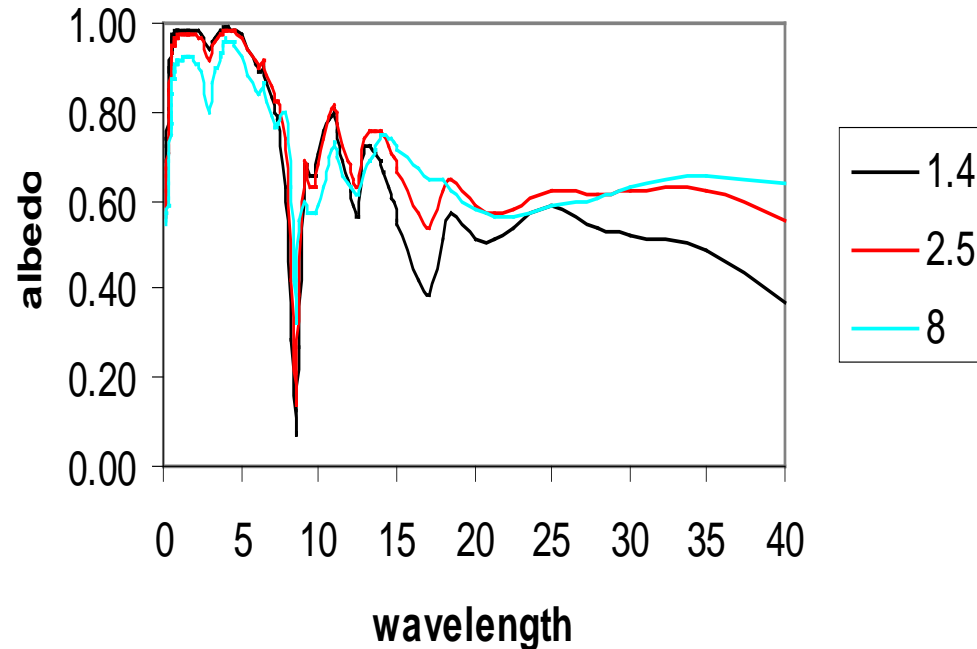
Goddard Chemistry Aerosol Radiation and Transport (GOCART) Aerosol Optical Model

1. Sulfur: DMS (Dimethyl sulfide), SO₂, SO₄, MSA (methanesulfonate)
2. Carbon: Hydrophobic BC/OC, hydrophilic BC/OC (water-like)
3. Dust: 8 bins: 0.1-0.18, 0.18-0.3, 0.3-0.6, 0.6-1, 1.0-1.8, 1.8-3.0, 3.0-6.0, 6.0-10.0 μm
4. Sea-salt: 4 bins: 0.1-0.5, 0.5-1.5, 1.5-5.0, 5.-10. μm

Lognormal size distribution, 35 size bins.

EPA Community Multiscale Air Quality (CMAQ) Aerosol Optical Model

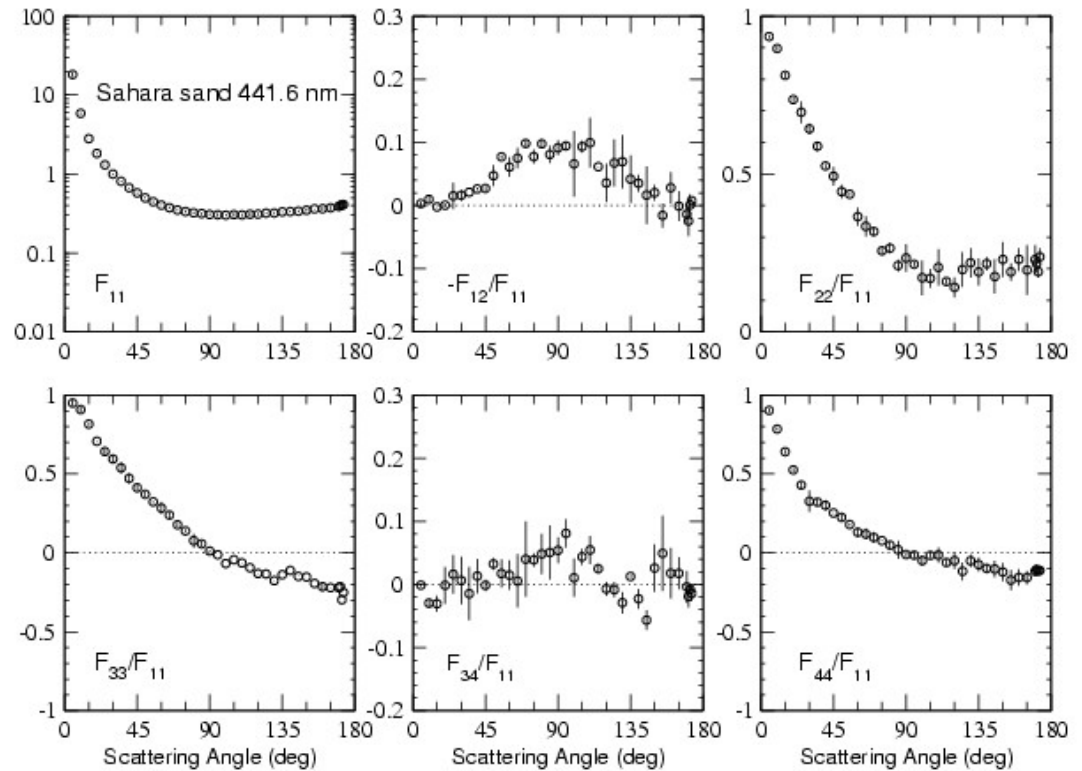
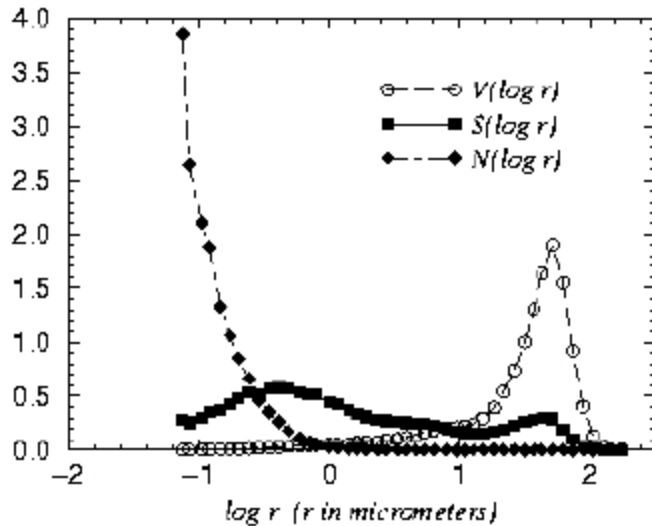
Dust



Dust Aerosol Phase Matrix Elements



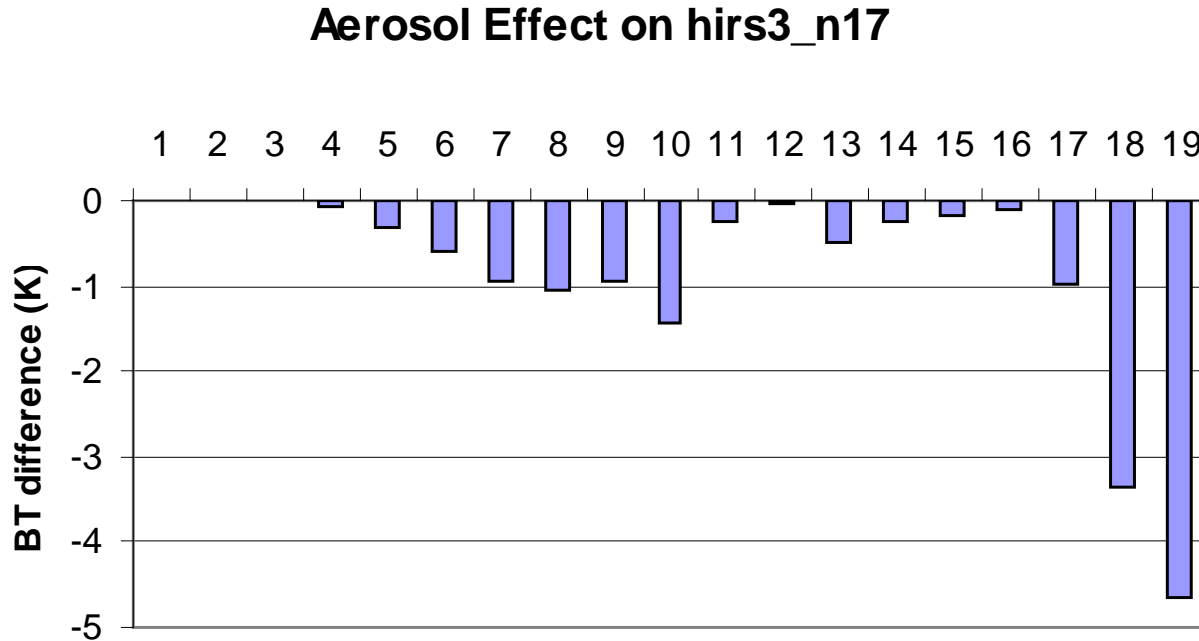
Sahara sand
size distributions



Phase functions

From Amsterdam Light Scattering Database

Aerosol Effect on NOAA-17 HIRS/3



0.1 g/m² OC aerosol at layer 63 (300 hPa)

0.1 g/m² Dust aerosol at layer 80 (592 hPa)

0.1 g/m² Dust aerosol at layer 82 (639 hPa)

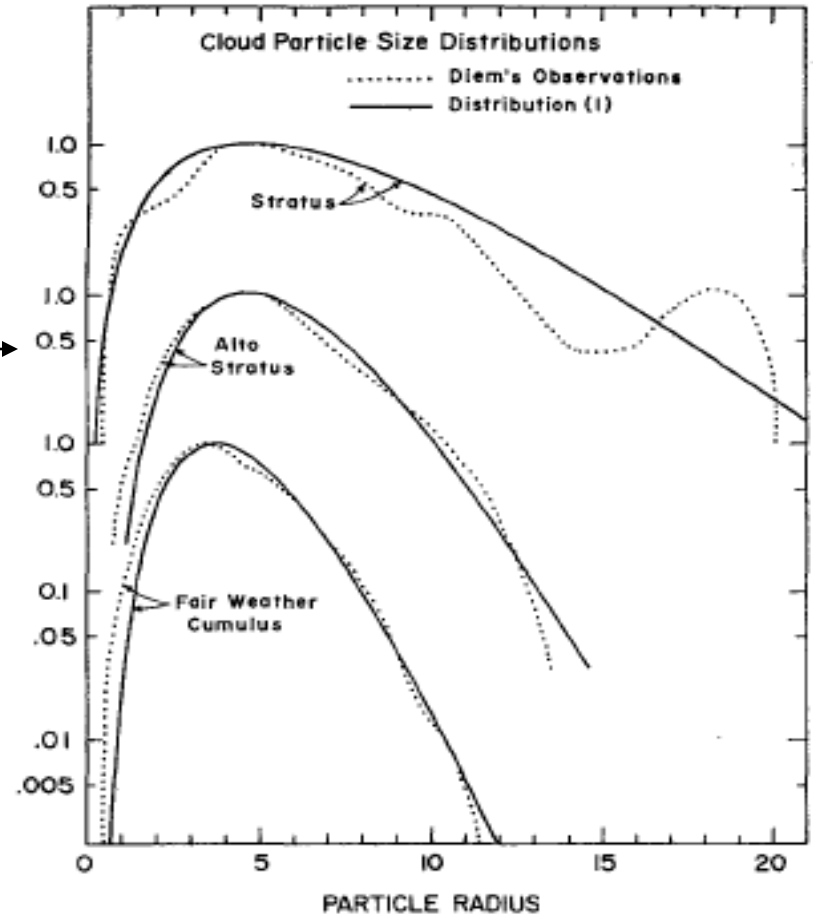
Cloud Particle Size Parameters

Gamma size distribution for small particle size:

$$f(r) = \frac{\Gamma(v)}{r_n} (r / r_n)^{v-1} e^{-r/r_n}$$

Hansen (1971)

For rain drops, snow, graupel/hail, Marshall-Palmer size distribution is used



Cloud Optical Parameter Module

- The 6 cloud types include water, ice, rain, snow, graupel and hail.
- Lookup table approach: the microphysical properties (extinction coefficient, single-scattering albedo, asymmetry factor, and Legendre phase function coefficients) of cloud particles are stored in lookup tables for IR and MW wavelengths based on widely-known publications (Simmer, 1994; Liou and Yang, 1995; Macke et al., 1996; Mishchenko et al., 2000; Baum et al., 2005, Yang et al., 2005). This table is searched with particle mean size and cloud water content (or mixing ratio). Note that the phase matrix elements are decomposed into a series of Legendre polynomials and the coefficients associated with the polynomials are also stored in the table.
- MW: the Mie theory is assumed in all calculations for spherical liquid and ice water cloud particles, and modified gamma size distributions (Simmer, 1994).
- IR (water cloud): spherical particles, Mie scattering, a modified gamma size distribution.
- IR (ice cloud): nonspherical hexagonal columns and with gamma size distribution, and the single-scattering properties of ice particles are computed from a composite method based on the finite-difference time domain technique, an improved geometric-optics method, and the Lorenz-Mie solutions for equivalent spheres (Fu et al., 1998; Yang et al., 2005).

Phase Function Model

- Rayleigh function: molecular scattering (1871)
- Henyey-Greenstein: approximate scattering (1941), for particles having finite size, no polarization.
- HG-Rayleigh scattering matrix, is a good approximation for cloud scattering in MW and aerosol scattering in IR.

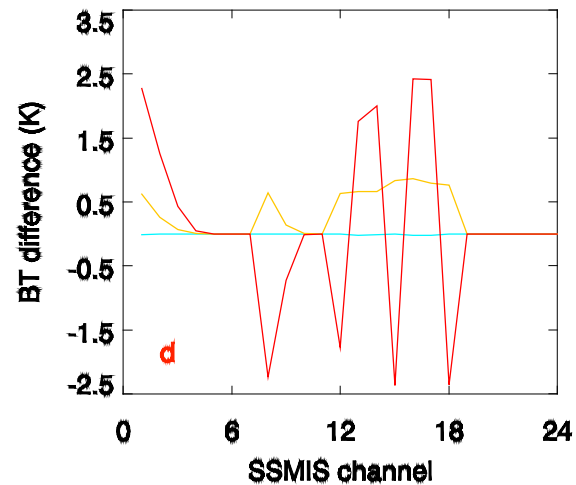
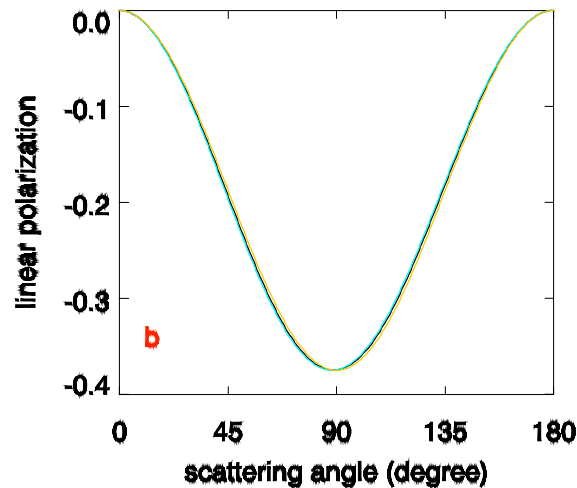
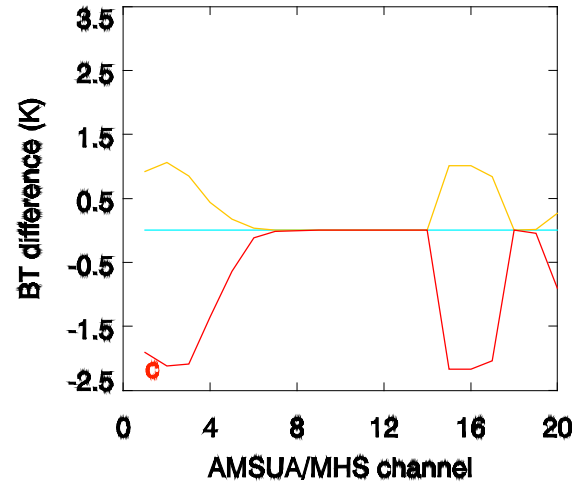
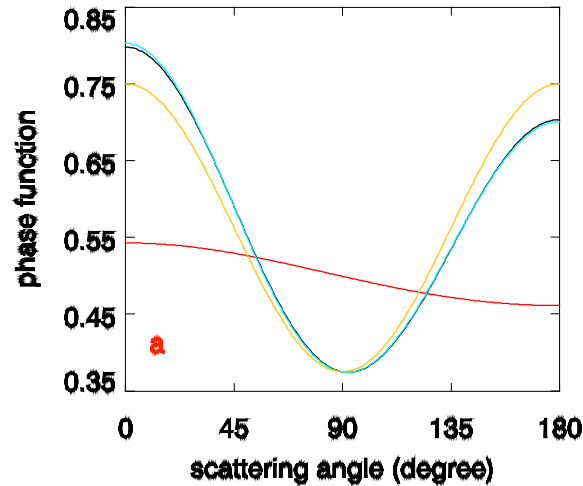
$$\mathbf{P}(\Theta, g) = C \frac{1 - G^2}{(1 + G^2 - 2G \cos \Theta)^{3/2}} \begin{bmatrix} 1 + \cos^2 \Theta & -1 + \cos^2 \Theta & 0 & 0 \\ -1 + \cos^2 \Theta & 1 + \cos^2 \Theta & 0 & 0 \\ 0 & 0 & \cos \Theta & 0 \\ 0 & 0 & 0 & \cos \Theta \end{bmatrix} \quad (1)$$

The normalization factor C and the asymmetry factor G used in HG part in HG-Rayleigh can analytically derived from

$$\int_0^\pi P(\Theta, g) \sin \Theta d\Theta = 1 \quad (2) \quad \text{-----} \rightarrow \quad C = \frac{3}{8 + 3G^2}$$

$$\int_0^\pi \cos \Theta P(\Theta, g) \sin \Theta d\Theta = g \quad (3) \quad \text{----} \rightarrow \quad G = f(g)$$

Test HG-Rayleigh Scattering Matrix in CRTM



$g=0.027$
 $r=90$ micron

— FDTD
— HG-Rayleigh
— Rayleigh
— HG

(Liu and Weng, 2006, Applied Optics)

Radiative Transfer Solver

A vertically-stratified, plane-parallel and non-polarized atmosphere, the monochromatic radiative transfer equation

$$\mu \frac{dI(\tau; \mu, \phi)}{d\tau} = I(\tau; \mu, \phi) - \frac{\overline{\omega}}{4\pi} \int P(\tau; \mu, \phi; \mu', \phi') I(\tau; \mu', \phi') d\mu' d\phi' - \frac{\overline{\omega}}{4\pi} P(\tau; \mu, \phi; -\mu_{\otimes}, \phi_{\otimes}) F_{\otimes} e^{-\tau/\mu_{\otimes}} - (1 - \overline{\omega}) B(T)$$

RT Solution under Clear-Sky Conditions $\overline{\omega} \approx 0$

$$I(\mu) = [r \int_0^{\tau_N} B(T) d\Gamma_d(\tau', \mu_d) + r_{\otimes} \frac{F_{\otimes}}{\pi} \Gamma_d(0, \mu_{\otimes}) + \varepsilon B(T_s)] \Gamma_u(\tau_N, \mu) - \int_0^{\tau_N} B(T) d\Gamma_u(\tau', \mu)$$

$$\Gamma_u(\tau, \mu) = e^{-\tau/\mu} \quad \Gamma_d(\tau, \mu) = e^{-(\tau_N - \tau)/|\mu|}$$

$$I_{ch}(\mu) = (\overline{r} I_{ch}^{\downarrow}(\mu_d) + \overline{r}_{\otimes} \frac{\overline{F}_{\otimes}}{\pi} \Gamma_{ch,d}(p_0, \mu_{\otimes}) + \overline{\varepsilon} B(T_{s,e})) \Gamma_{ch,u}(p_N, \mu)$$

$$+ \sum_{i=1}^N (\Gamma_{ch,u}(p_{i-1}, \mu) - \Gamma_{ch,u}(p_i, \mu)) B(T_{i,e})$$

$$I_{ch}^{\downarrow}(\mu_d) = \sum_{i=1}^N (\Gamma_{ch,d}(p_i, \mu_d) - \Gamma_{ch,d}(p_{i-1}, \mu_d)) B(T_{i,e}) + I_{bg} \Gamma_{ch,d}(p_0, \mu_d)$$

Radiative Transfer Solver

RT Solution under Cloudy Conditions

$$\mu_i \frac{dI(\tau, \mu_i)}{d\tau} = I(\tau, \mu_i) - \varpi P(\mu_i, \mu_j) I(\tau, \mu_j) w_j - \varpi P(\mu_i, \mu_{-j}) I(\tau, \mu_{-j}) w_j - (1 - \varpi) B(T)$$

$$-\mu_i \frac{dI(\tau, \mu_{-i})}{d\tau} = I(\tau, \mu_{-i}) - \varpi P(\mu_{-i}, \mu_j) I(\tau, \mu_j) w_j - \varpi P(\mu_{-i}, \mu_{-j}) I(\tau, \mu_{-j}) w_j - (1 - \varpi) B(T)$$

$$\frac{d}{d\tau} \begin{bmatrix} \mathbf{I}_u \\ \mathbf{I}_d \end{bmatrix} = - \begin{bmatrix} \boldsymbol{\alpha} & \boldsymbol{\beta} \\ -\boldsymbol{\beta} & -\boldsymbol{\alpha} \end{bmatrix} \begin{bmatrix} \mathbf{I}_u \\ \mathbf{I}_d \end{bmatrix} - (1 - \varpi) B(T) \begin{bmatrix} \mathbf{u}^{-1} \boldsymbol{\Xi} \\ -\mathbf{u}^{-1} \boldsymbol{\Xi} \end{bmatrix}$$

$$\boldsymbol{\alpha}(\mu_i, \mu_j) = [\varpi P(\mu_i, \mu_j) w_j - \delta_{ij}] / \mu_i$$

$$\boldsymbol{\beta}(\mu_i, \mu_{-j}) = \varpi P(\mu_i, \mu_{-j}) w_j / \mu_i$$

$$\mathbf{u} = [\mu_1, \mu_2, \dots, \mu_N]_{diagonal}$$

$$\boldsymbol{\Xi} = [1, 1, \dots, 1]^T$$

μ_i : Gaussian quadrature points

w_i : Gaussian quadrature weights

$P(\mu_i, \mu_j), P(\mu_i, \mu_{-j})$

azimuth-averaged forward and backward phase matrix

$P(\mu_i, \mu_j) = P(\mu_{-i}, \mu_{-j})$

$P(\mu_{-i}, \mu_j) = P(\mu_i, \mu_{-j})$

Advanced Doubling-Adding (ADA) Method

Layer transmission and reflection

$$\mathbf{r}(\delta_0) = \delta_0 \boldsymbol{\beta} \quad \mathbf{t}(\delta_0) = \mathbf{E} + \boldsymbol{\alpha} \delta_0 \quad \delta = \delta_n = 2^n \delta_0$$

$$\mathbf{r}(\delta_{i+1}) = \mathbf{t}(\delta_i) [\mathbf{E} - \mathbf{r}(\delta_i) \mathbf{r}(\delta_i)]^{-1} \mathbf{r}(\delta_i) \mathbf{t}(\delta_i) + \mathbf{r}(\delta_i)$$

$$\mathbf{t}(\delta_{i+1}) = \mathbf{t}(\delta_i) [\mathbf{E} - \mathbf{r}(\delta_i) \mathbf{r}(\delta_i)]^{-1} \mathbf{t}(\delta_i)$$

Layer source function

$$\mathbf{S}_u = [(\mathbf{E} - \mathbf{t} - \mathbf{r})B(T_1) - (B(T_2) - B(T_1))\mathbf{t} + \frac{B(T_2) - B(T_1)}{(1 - \varpi g)\delta} (\mathbf{E} + \mathbf{r} - \mathbf{t})\mathbf{u}] \boldsymbol{\Xi}$$

$$\mathbf{S}_d = [(\mathbf{E} - \mathbf{t} - \mathbf{r})B(T_1) + (B(T_2) - B(T_1))(\mathbf{E} - \mathbf{r}) + \frac{B(T_2) - B(T_1)}{(1 - \varpi g)\delta} (\mathbf{t} - \mathbf{E} - \mathbf{r})\mathbf{u}] \boldsymbol{\Xi}$$

Vertical integration

$$\mathbf{I}_u(n) = \varepsilon B(T_s) \quad \mathbf{R}(n) \quad \text{the surface reflection matrix, loop } k \text{ from } n \rightarrow 1$$

$$\begin{aligned} \mathbf{I}_u(k-1) &= \mathbf{S}_u(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} \mathbf{R}(k) \mathbf{S}_d(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} \mathbf{I}_u(k) \\ &= \mathbf{S}_u(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} [\mathbf{R}(k) \mathbf{S}_d(k) + \mathbf{I}_u(k)] \end{aligned}$$

$$\mathbf{R}(k-1) = \mathbf{r}(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} \mathbf{R}(k) \mathbf{t}(k)$$

$$\text{TOA radiance } \mathbf{I}_u = \mathbf{I}_u(0) + \mathbf{R}(0) \mathbf{I}_{sky}$$

ADA method remark

Numerically exactly

Analytical expressions replace the most complicated terms: source functions.

F90/F95 matrix and vector manipulation makes coding simple, also simple for tangent-linear and adjoint coding, good for code maintenance

Add a viewing angle in the streams for satellite radiance

Fast, about 60 times faster than the original double-adding method

Easy extension, for example:

Double the size of vector and matrix dimension and other minor change for the atmospheric residual polarization

Add a sun angle in the streams and add a loop over azimuthal-component for visible/UV radiance simulation

CRTM Baseline Solver + solar radiation

(Advanced Doubling-Adding, ADA)

1. Compute layer transmission and reflection (loop i from 0 → n-1)

baseline $\mathbf{r}(\delta_0) = \delta_0 \boldsymbol{\beta}$ $\mathbf{t}(\delta_0) = \mathbf{E} + \boldsymbol{\alpha} \delta_0$ $\delta = \delta_n = 2^n \delta_0$ $\mathbf{t}(\delta_{i+1}) = \mathbf{t}(\delta_i) [\mathbf{E} - \mathbf{r}(\delta_i) \mathbf{r}(\delta_i)]^{-1} \mathbf{t}(\delta_i)$
 $\mathbf{r}(\delta_{i+1}) = \mathbf{t}(\delta_i) [\mathbf{E} - \mathbf{r}(\delta_i) \mathbf{r}(\delta_i)]^{-1} \mathbf{r}(\delta_i) \mathbf{t}(\delta_i) + \mathbf{r}(\delta_i)$

new $\mathbf{t} = (A_{22})^{-1}$ $\mathbf{r} = A_{12} \mathbf{t}$ where $\exp(A\delta) = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix}$ and **A** is the phase matrix.

2. Compute layer source functions

$$\mathbf{S}_u = [(\mathbf{E} - \mathbf{t} - \mathbf{r})B(T_1) - (B(T_2) - B(T_1))\mathbf{t} + \frac{B(T_2) - B(T_1)}{(1 - \omega g)\delta} (\mathbf{E} + \mathbf{r} - \mathbf{t})\mathbf{u}] \boldsymbol{\Xi} + \frac{\omega F_0}{\pi} \exp(-\tau_{k-1}(\mu_0)) [(\mathbf{E} - \mathbf{t} \exp(-\delta(\mu_0))) \Psi_u - \mathbf{r} \Psi_d]$$

$$\mathbf{S}_d = [(\mathbf{E} - \mathbf{t} - \mathbf{r})B(T_1) + (B(T_2) - B(T_1))(\mathbf{E} - \mathbf{r}) + \frac{B(T_2) - B(T_1)}{(1 - \omega g)\delta} (\mathbf{t} - \mathbf{E} - \mathbf{r})\mathbf{u}] \boldsymbol{\Xi} + \frac{\omega F_0}{\pi} \exp(-\tau_{k-1}(\mu_0)) [(\exp(-\delta(\mu_0))E - \mathbf{t}) \Psi_d - \mathbf{r} \exp(-\delta(\mu_0)) \Psi_u]$$

$$\begin{bmatrix} \Psi_d \\ \Psi_u \end{bmatrix} = -\frac{\omega F_\lambda}{(1 + \delta_{0m})\pi} \begin{bmatrix} \boldsymbol{\alpha} + E/\mu_0 & \boldsymbol{\beta} \\ -\boldsymbol{\beta} & -\boldsymbol{\alpha} + E/\mu_0 \end{bmatrix}^{-1} \begin{bmatrix} \phi(\mu_i, \mu_0) \\ \phi(-\mu_i, \mu_0) \end{bmatrix}$$

3. Vertical integration

$$\mathbf{I}_u(n) = \varepsilon B(T_s) + \frac{F_\lambda \exp(-\tau_N(\mu_0))}{(1 + \delta_{0m})\pi} R_s(\mu_0) \quad \mathbf{R}(n) \quad \text{the surface reflection matrix, loop k from n} \rightarrow 1$$

$$\begin{aligned} \mathbf{I}_u(k-1) &= \mathbf{S}_u(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} \mathbf{R}(k) \mathbf{S}_d(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} \mathbf{I}_u(k) \\ &= \mathbf{S}_u(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} [\mathbf{R}(k) \mathbf{S}_d(k) + \mathbf{I}_u(k)] \end{aligned}$$

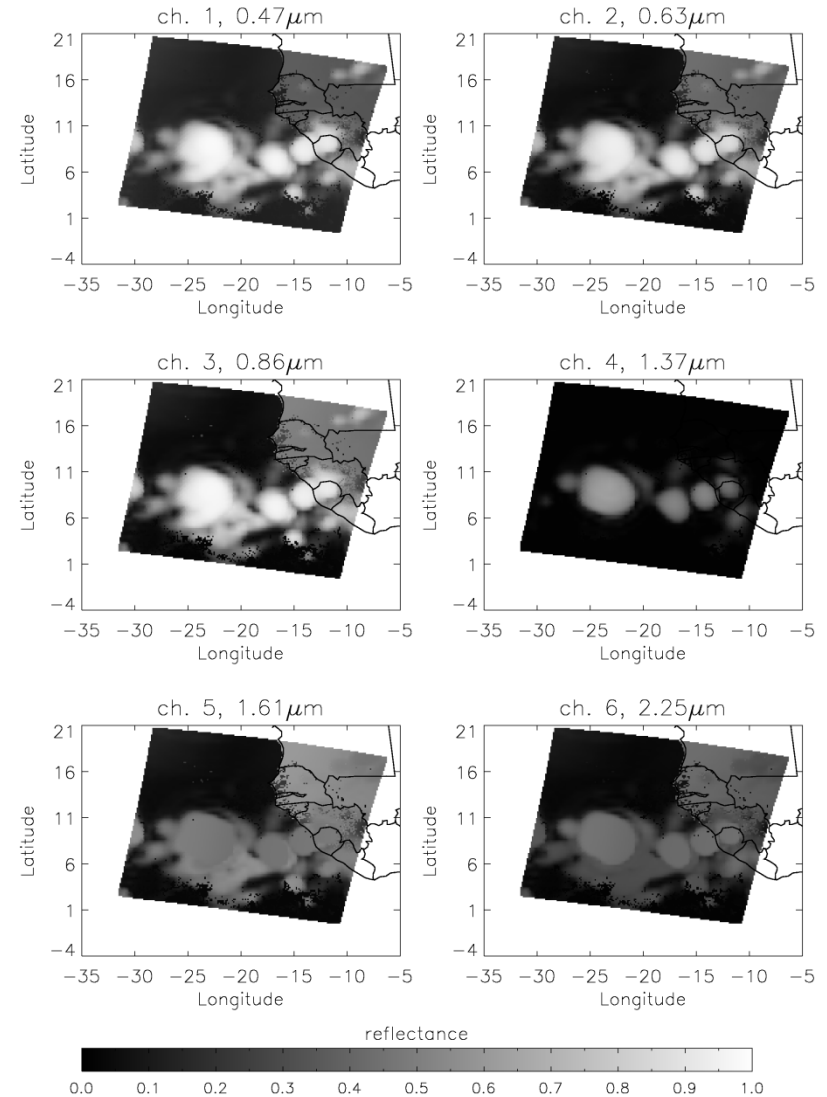
$$\mathbf{R}(k-1) = \mathbf{r}(k) + \mathbf{t}(k) [\mathbf{E} - \mathbf{R}(k) \mathbf{r}(k)]^{-1} \mathbf{R}(k) \mathbf{t}(k)$$

4. Final TOA radiance Radiance = $\mathbf{I}_u(0) + \mathbf{R}(0) \mathbf{I}_{sky}$

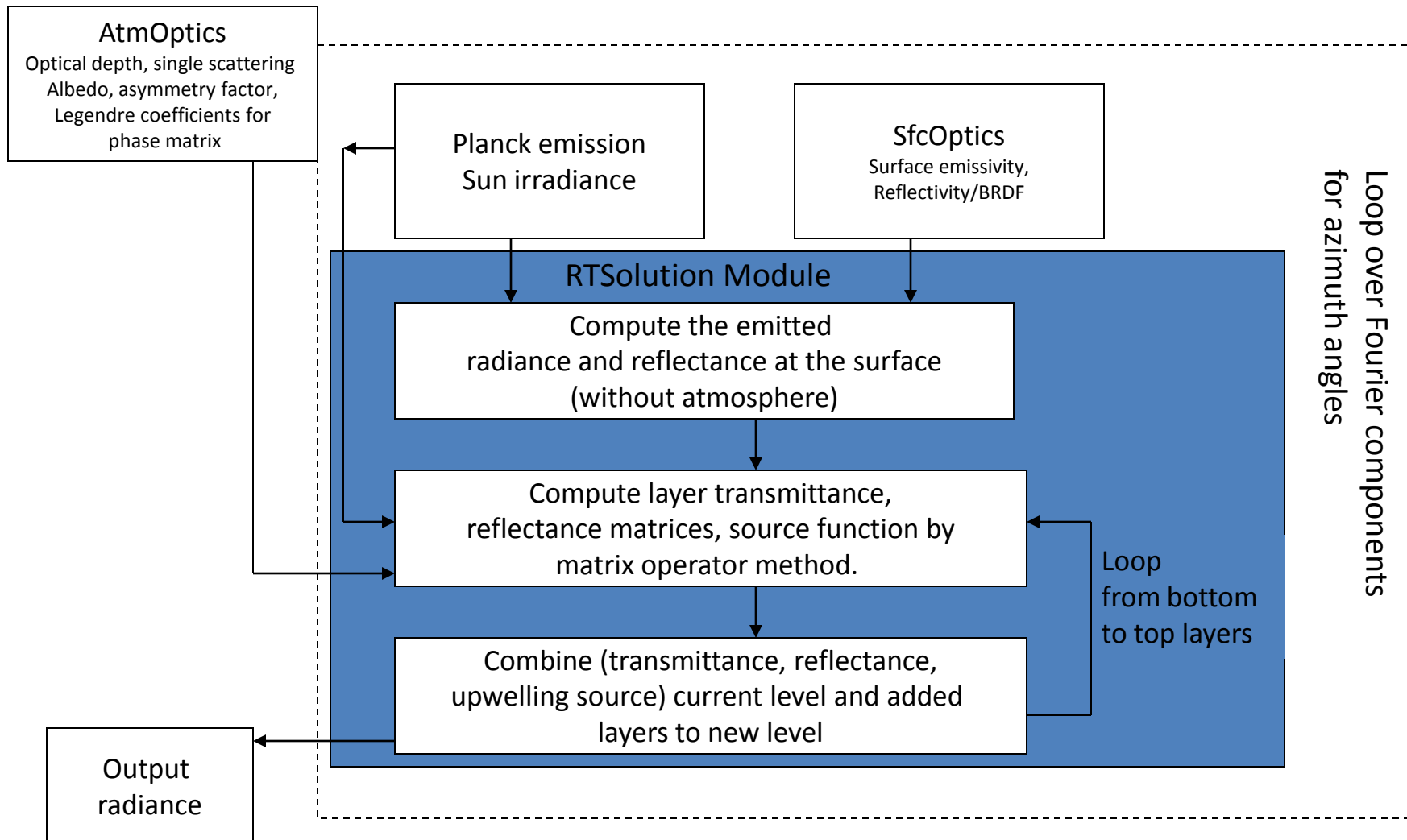
Components for Visible/UV Sensors

- MoleculeScatter module (new): compute molecule scattering optical properties
- Extension of AtmAbsorption module: compute molecule absorption for Vis/UV sensors
- Extension of CloudScatter and AerosolScatter modules: compute cloud and aerosol optical properties for Vis/UV sensors
- Extension of the Advanced Doubling-Adding (ADA) method: add integration of the RT solution over Fourier components for azimuth angle

GOES-R ABI simulations with MODIS terra geometry parameters, GDAS data and GOCART aerosol data.



RT Solution for Cloud/Aerosol Scattering Environment: ADA with a Matrix Operator Method



(Liu and Weng, 2006, JAS; Liu 2010)

CRTM Surface Emissivity Module

Ocean



Sea Ice



Snow



Canopy (bare soil)



Desert



Microwave land emissivity model (NESDIS model) (Weng, Yan, Grody, 2001), desert microwave emissivity library (Yan and Weng, 2011), and improved NESDIS land surface emissivity model (Zheng et al., 2011); **TELSEM**, and **CNRM** databases

NPOESS Infrared emissivity database
IASI Land Infrared emissivity database
UWIREMIS database

Empirical snow and sea ice microwave emissivity algorithm (Yan and Weng, 2003; 2008)

Two layer snow emissivity model (Yan, Weng, Liang, 2010)

Fast multi-layer snow emissivity model (Liang, Weng, Yan, 2010)

FASTEM3 microwave emissivity model from (English and Hewison, 1998)

FASTEM4 microwave emissivity model (Liu, Weng, English, 2010)

FASTEM5

IR emissivity model (Wu and Smith, 1991; van Delst et al., 2001; Nalli et al., 2008)

CRTM URLs and Support Email

- CRTM software ftp site (Source code, Coefficients for each sensor, User guide, and Example programs):
<ftp://ftp.emc.ncep.noaa.gov/jcsda/CRTM/>
- CRTM support email list:
listncep.list.emc.jcsda_crtm.support@noaa.gov
- CRTM trac page:
<https://svnemoc.ncep.noaa.gov/trac/crtm>
- CRTM repository (for checkouts, commits, etc)
<https://svnemoc.ncep.noaa.gov/projects/crtm>
- CRTM Announcement mailing list:
https://lstrv.ncep.noaa.gov/mailman/listinfo/ncep.list.emc.jcsda_crtm
- CRTM CWG mailing list:
https://lstrv.ncep.noaa.gov/mailman/listinfo/ncep.list.emc.jcsda_cwg
- CRTM Developers mailing list:
https://lstrv.ncep.noaa.gov/mailman/listinfo/ncep.list.emc.jcsda_crtm.developers

Summary

- CRTM is a fast and accurate model to compute satellite radiance and radiance derivatives for IR, MW, Visible and UV sensors.
- It includes advanced RT components to compute absorption, emission and scattering from various gases, clouds, aerosols and surfaces.
- It has been extensively validated against its base models and observations.
- The user interface and program structure are designed for easy use and future expansion.
- CRTM continues to update new components (NLTE, additional SOI RT solver) and to improve in computational efficiency, transmittance model and surface emissivity/reflection models (e.g. FASTEM5, and databases).

References

- Carter, C., Q. Liu, W. Yang, D. Hommel, and W. Emery, 2002: Net heat flux, visible/infrared imager/radiometer suite algorithm theoretical basis document. Available on http://npoesslib.ipo.noaa.gov/u_listcategory_v3.php?35.
- Chen, Y., F. Weng, Y. Han, and Q. Liu, 2012: Planck weighted transmittance and correction of solar reflection for broadband infrared satellite channels. *J. Atmos. Oceanic. Technol.*, **29**, 382-396, doi:10.1175/JTECH-D-11-00102.1
- Chen, Y., Y. Han, and F. Weng, 2011: Comparison of two transmittance algorithms in the Community Radiative Transfer Model: application to AVHRR. *J. Geophys. Res.*, **117**, D06206, doi:10.1029/2011JD016656.
- Chen, Y., Y. Han, P. Van Delst, and F. Weng, 2010: On water vapor jacobian in fast radiative transfer model. *J. Geophys. Res.*, **115**, D12303, doi:10.1029/2009JD013379.
- Chen, Y., Y. Han, Q. Liu, P. Van Delst, and F. Weng, 2011: Community Radiative Transfer Model for Stratospheric Sounding Unit. *J. Atmos. Oceanic. Technol.*, **28**, 767-778.
- Chen, Y., F. Weng, Y. Han, and Q. Liu, 2008: Validation of the Community Radiative Transfer Model (CRTM) by using CloudSat data. *J. Geophys. Res.*, **113**, D00A03, doi:10.1029/2007JD009561.
- Cox, C. and W. Munk, 1954, Statistics of the sea surface derived from sun glitter. *J. Mar. Res.* **13** 198-227.
- Clough, S. A., M. J. Iacono and J. L. Moncet, 1992: Line-by-line calculations of atmospheric fluxes and cooling rates: application to water vapor. *J. Geophys. Res.* **97**, 15761-15785.
- English, S.J. and T.J. Hewison, 1998: A fast generic millimetre wave emissivity model. *Microwave Remote Sensing of the Atmosphere and Environment Proc. SPIE* **3503** 22-30.
- Errico, R. M., 1997: What is an adjoint model. *Bull. Amer. Meteor. Soci.*, **78**, 2577-2591.

References

- Evans, K. F. and G. L. Stephens, 1991: A new polarized atmospheric radiative transfer model. *J. Quant. Spectrosc. Radiat. Transfer*, **46**, 413-423.
- Giering, R. and T. Kaminski, 1998: Recipes for Adjoint Code Construction. *ACM Transation on Mathematical Software*, **24**, 437-474.
- Han, Y, P. van Delst, and F. Weng, 2010: An improved fast radiative transfer model for special sensor microwave imager/sounder upper atmosphere sounding channels. *J. Geophys. Res.*, **115**, D15109, doi:10.1029/2010JD013878.
- Han Y., P. van Delst, Q. Liu, F. Weng, B. Yan, R. Treadon, and J. Derber, 2006: JCSDA Community Radiative Transfer Model (CRTM) - Version 1, *NOAA Technical Report NESDIS 122*, pp40.
- Han, Y., F. Weng, Q. Liu, and P. van Delst, 2007: A fast radiative transfer model for SSMIS upper atmosphere sounding channels. *J. Geophys. Res.*, **112**, D111121, doi:10.1029/2006JD008208.
- Hansen, J.E., 1971: Multiple scattering of polarized light in planetary atmosphere. *J. Atmos. Sci.*, **28**, 120-125.
- Kleespies, T. J., P. V. Delst, L. M. McMillin, J. Derber, 2004: Atmospheric Transmittance of an Absorbing Gas. 6. OPTRAN Status Report and Introduction to the NESDIS/NCEP Community Radiative Transfer Model, *Appl. Opt.*, **43**, 3103-3109.
- Liou, K, 1980: An introduction to atmospheric radiation, Academic. Press, Inc, New York.
- Liu, Q., and F. Weng, 2006: Combined Henyey-Greenstein and Rayleigh phase function. *Appl. Opt.*, **45**, 7475-7479.
- Liu, Q., and F. Weng, 2006: Advanced Doubling-Adding Method for Radiative Transfer in Planetary Atmospheres. *J. Atmos. Sci*, **63**, 3459-3465.
- Liu, Q., and F. Weng, 2009: Recent stratospheric temperature observed from satellite measurements. *SOLA*, **5**, doi:10.2151/sola.2009-014.

References

- Liu, Q., F. Weng, and S. English, 2011: An improved fast microwave water emissivity model. *IEEE Trans. Geoscience and Remote Sensing*, **49**, 1238-1250, DOI:10.1109/TGRS.2010.2064779.
- Liu, Q., X. Liang, Y. Han, P. van Delst, Y. Chen, A. Ignatov, and F. Weng, 2009: Effect of out-of-band response in NOAA-16 AVHRR Channel 3B on top-of-atmosphere radiances calculated with the Community Radiative Transfer Model. *J. Atmos. Oceanic. Technol.*, **26**, 1968-1972.
- McMillin, L. M., L. J. Crone, M. D. Goldberg, and T. J. Kleespies, 1995: Atmospheric transmittance of an absorbing gas. 4. OPTRAN: a computationally fast and accurate transmittance model for absorbing gases with fixed and variable mixing ratios at variable viewing angles. *Appl. Opt.* **34**, 6269 - 6274.
- Nalli, N. R., P. J. Minnett, and P. van Delst, 2008: Emissivity and reflection model for calculating unpolarized isotropic water surface-leaving radiance in the infrared. I: Theoretical development and calculations, *Appl. Opt.*, **47**, 3701-3721.
- Nalli, N. R., P. J. Minnett, E. Maddy, W. W. McMillan, and M. D. Goldberg, 2008: Emissivity and reflection model for calculating unpolarized isotropic water surface-leaving radiance in the infrared. 2: Validation using Fourier transform spectrometers, *Appl. Opt.*, **47**, 4649-4671.
- Saunders, R. M., M. Matricardi, and P. Brunel, 1999: An improved fast radiative transfer model for assimilation of satellite radiance observation, *QJRMS*, **125**, 1407-1425.
- Weng, F., 2007: Advances in radiative transfer modeling in support of satellite data assimilation. . *J. Atmos. Sci.*, **64**, 3803-3811.
- Weng, F., B. Yan, and N. Grody, 2001: A microwave land emissivity model, *Geophys. Res.*, **106**, 20,115-20,123.

References

- Weng, F., and Q. Liu, 2003: Satellite Data Assimilation in Numerical Weather Prediction Models, Part I: Forward Radiative Transfer and Jacobian Modeling in Cloudy Atmospheres. *J. Atmos. Sci.*, **60**, 2633 – 2646.
- Weng, F., Y. Han, P. van Delst, Q. Liu, and B. Yan, 2005: JCSDA Community radiative transfer model (CRTM), *Technical Proceedings of Fourteenth International ATOVS Study Conference*, Beijing
- Wu , X. and W. L. Smith, 1997: Emissivity of rough sea surface for 8-13 μm : modeling and verification. *Appl. Opt.*, **36**, 2609-2619.
- Xiong, X. and L.M. McMillin, 2005: An Alternative to the Effective Transmittance Approach for Calculating Polychromatic Transmittances in Rapid Transmittance Models, *Appl. Opt.*, **44**, 67-76 (2005).
- Yan, B., and F. Weng, 2011: Effects of microwave desert surface emissivity on AMSU-A data assimilation. *IEEE Trans. Geoscience and Remote Sensing*, **49**, 1238-1250, DOI:10.1109/TGRS.2010.2091508.
- Yan, B., F. Weng, and H. Meng, 2008: Retrieval of snow surface microwave emissivity from the advanced microwave sounding unit. . *J. Geophys. Res.*, **113**, D19206, doi:10.1029/2007JD009559.
- Yan, B., F. Weng, K. Okamoto, 2004: Improved Estimation of Snow Emissivity from 5 to 200 GHz. *8th Specialist Meeting on Microwave Radiometry and Remote Sensing Applications*, 24-27 February, 2004, Rome, Italy.
- Yang, P., B.-C. Gao, B. A. Baum, W. Wiscombe, Y. Hu, S. L. Nasiri, A. Heymsfield, G. McFarquhar, and L. Miloshevich, 2001: Sensitivity of cirrus bidirectional reflectance in MODIS bands to vertical inhomogeneity of ice crystal habits and size distributions. *J. Geophys. Res.*, **106**, 17267-17291.