

## Lecture 2

# Microwave Remote Sensing: Theory, Algorithm and Applications

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**National Oceanic and Atmospheric Administration**

**2012 Update**

# Outline

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- Basic principle of remote sensing over land
- Microwave retrieval of land emissivity
- Physical Base for MW Remote Sensing of Clouds
- Cloud Liquid Water Algorithm
- Cloud Ice Water Algorithm
- Microwave Sounding Algorithm

# Principle of Microwave Land Remote Sensing

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Emission-based radiative transfer equation:

$$T_b = \varepsilon T_s \exp(-\tau_s / \mu) + T_u + (1 - \varepsilon) T_d \exp(-\tau_s / \mu)$$



$$T_b = T_s [1 - (1 - \varepsilon) \Upsilon^2] - \Delta T (1 - \Upsilon) [1 + (1 - \varepsilon) \Upsilon]$$

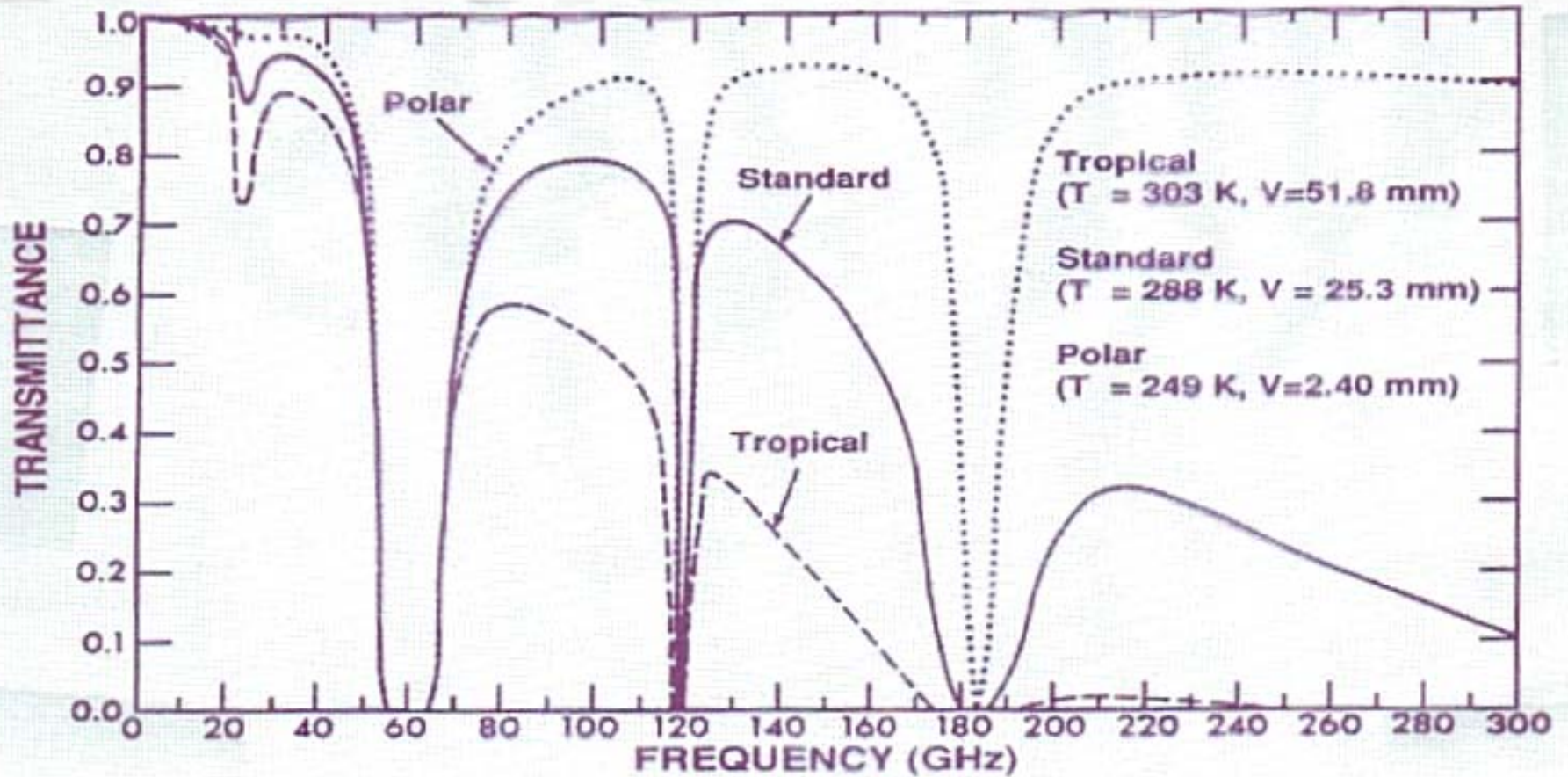
If atmosphere is transparent like a glass window, then  $\Upsilon = 1$

$$T_b = \varepsilon T_s$$

Brightness temperature is a linear function of surface emissivity!

*This is a basic principle for microwave remote sensing of land surface property.*

# Microwave Transmissivity Spectrum



## BT Sensitivity to Surface Emissivity

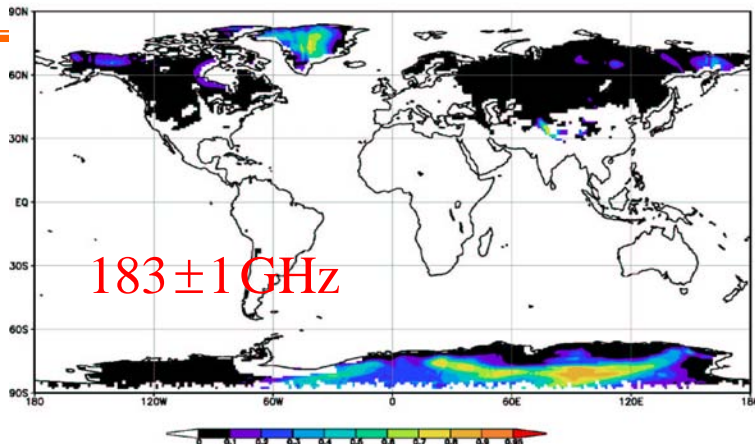
Freq (GHz)	$T_s = 230 \text{ K}$ and $TPW = 0.5 \text{ mm}$					
	$P_s = 600 \text{ (mb)}$			$P_s = 1000 \text{ (mb)}$		
	$T_d(\text{K})$	$\tau$	$\Delta T_B(\text{K})$	$T_d(\text{K})$	$\tau$	$\Delta T_B(\text{K})$
6.925	1.50	0.99	9.08	4.00	0.98	8.87
10.65	1.60	0.99	9.07	4.40	0.98	8.84
18.7	2.30	0.99	9.02	6.20	0.97	8.70
23.8	3.30	0.98	8.93	8.50	0.96	8.51
36.5	7.10	0.97	8.63	19.10	0.91	7.69
50.3	49.30	0.77	5.59	112.50	0.49	2.29
52.8	111.20	0.49	2.34	188.60	0.15	0.25
89	8.20	0.96	8.54	22.30	0.90	7.46
150	4.40	0.98	8.84	12.50	0.94	8.21
183.3±7	16.60	0.93	7.89	43.50	0.81	6.02
183.3±3	55.30	0.75	5.24	104.10	0.54	2.71
183.3±1	134.60	0.39	1.50	160.10	0.29	0.81

$$\Delta T_B = \tau(T_s - T_d)\Delta\epsilon, \quad \Delta\epsilon = 0.04$$

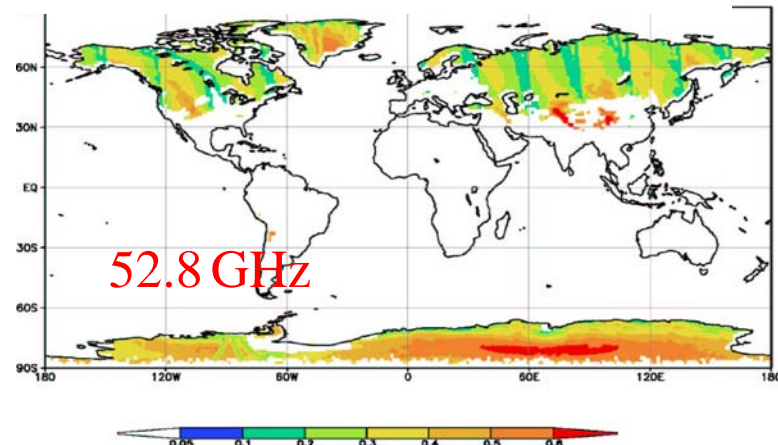
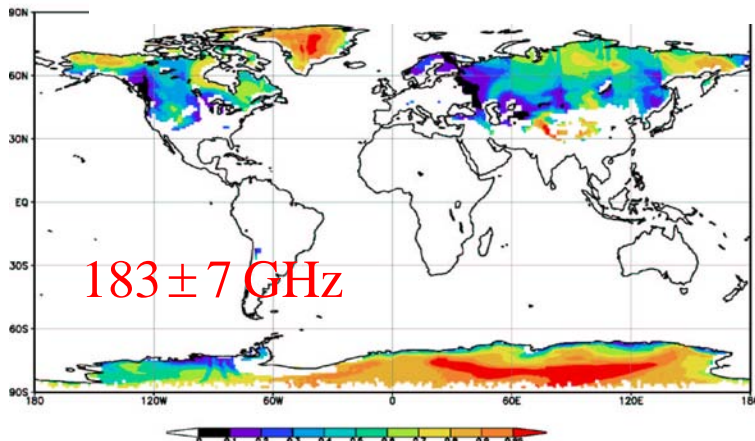
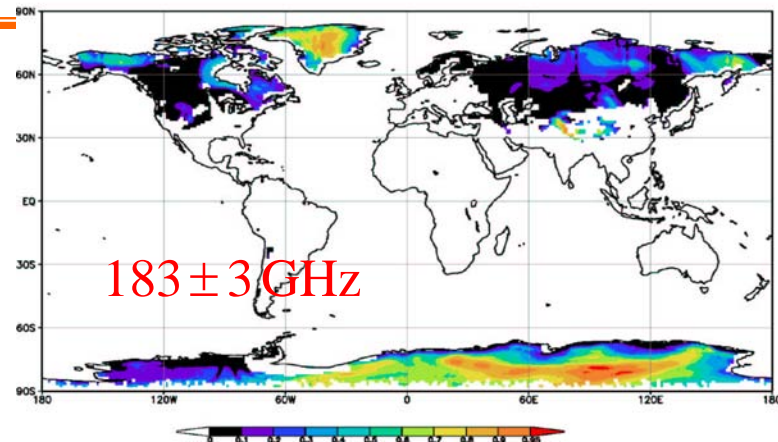
Surface emissivity uncertainty of 5-10% will produce brightness temperature uncertainty up to several degrees!

# Atmospheric Transmittance ( $\gamma$ )

Atmospheric Transmittance at  $183.3 \pm 1$  GHz



Atmospheric Transmittance at  $183.3 \pm 3$  GHz



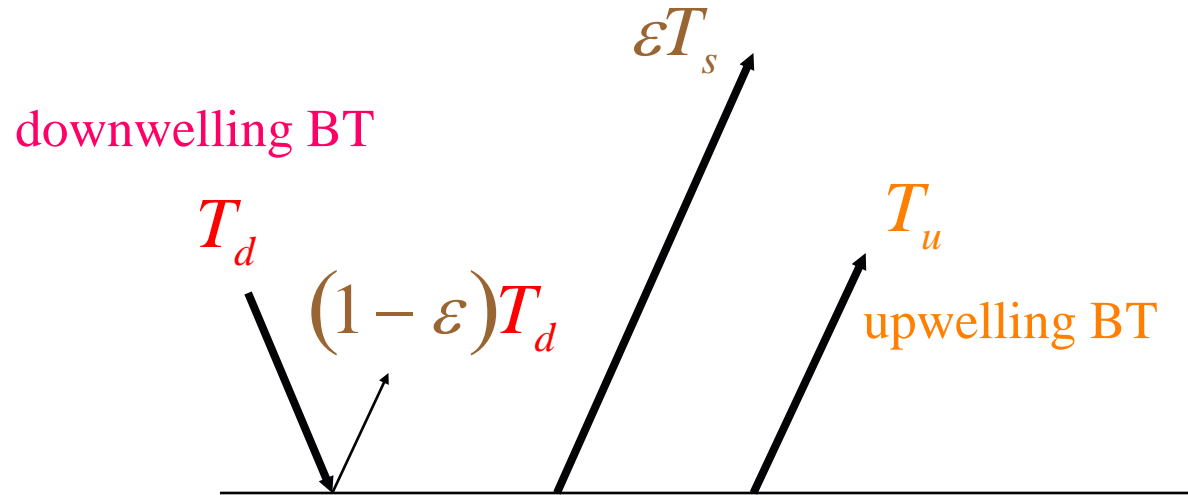
A typical channel for atmospheric profiling can become surface sensitive in certain conditions (e.g. dry moisture, high elevation).

# Satellite Microwave Window Channels

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- **SSM/I** 19.35, 37, 85.5 GHz
- **AMSU** 31.4, 50.3, 89, 150 GHz
- **TMI** 10.7, 19.35, 37, 85.5 GHz
- **AMSR-E** 6.6, 10.7, 19.35, 37, 85.5 GHz
- **SSMIS** 19.35, 37, 50.3, 90, 150 GHz
- **Windsat** 6.6, 10.7, 19.35, 37 GHz

# Retrieval of Microwave Land Emissivity



$$\varepsilon = \frac{T_b - T_u - T_d \tau}{\tau(T_s - T_d)}$$

$$T_d = \int_{\tau_0}^{\tau_s} B(\tau, T) \exp\left(-\frac{(\tau - \tau_0)}{\mu}\right) d\tau, \quad T_u = \int_{\tau_s}^{\tau_0} B(\tau, T) \exp\left(-\frac{(\tau_s - \tau)}{\mu}\right) d\tau$$



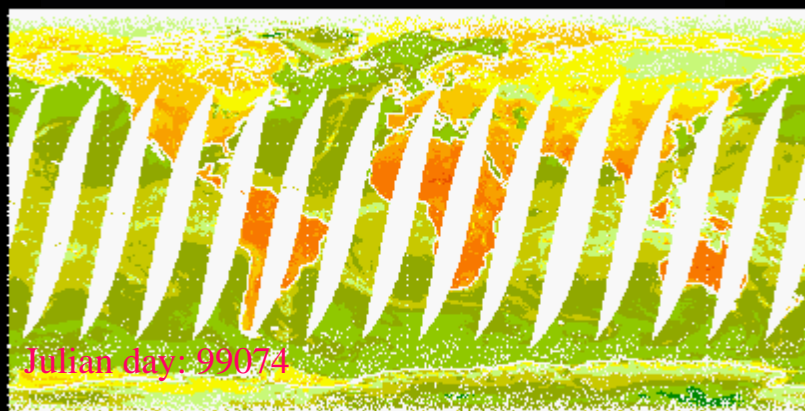
# Required Data Sets

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- **Satellite microwave brightness temperatures**  
(F-14 SSM/I)
- **Atmospheric temperature and moisture profiles**  
(GDAS, AMSU-A/B)
- **Land surface temperature**  
(GDAS, AVHRR)
- **Precipitation screening**  
(AVHRR, Scattering Index)

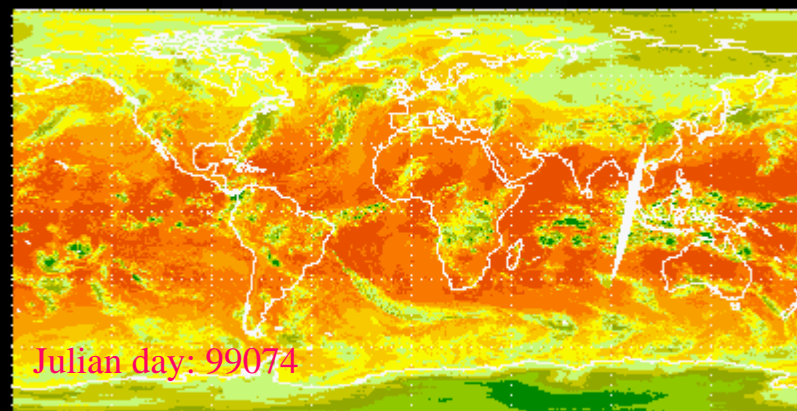
# Multi-Sensor and NWP Data Sets

SSM/I Antenna Temperature at 19:36 GHz



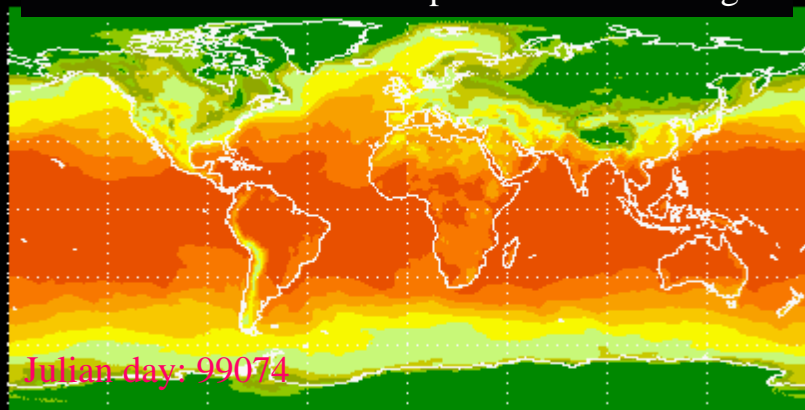
missing 160 165 180 185 210 225 240 255 270 285 300 K

AVHRR Infrared 11  $\mu\text{m}$



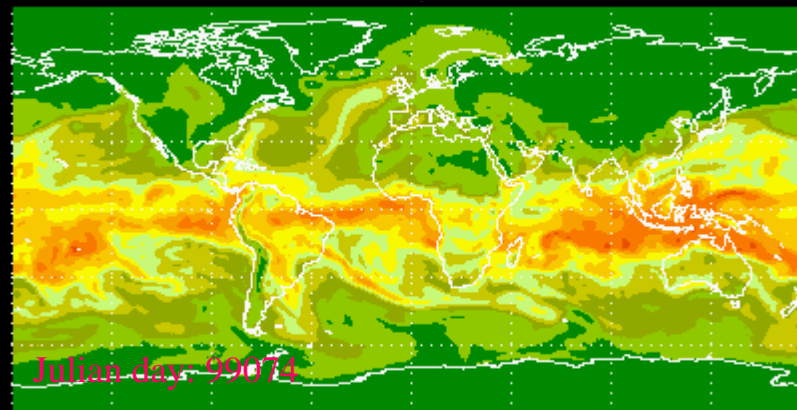
missing 200 210 220 230 240 260 280 270 280 290 300 K

GDAS Land Surface Temperature at 2-m Height



250 255 260 265 270 275 280 285 290 295 300 K

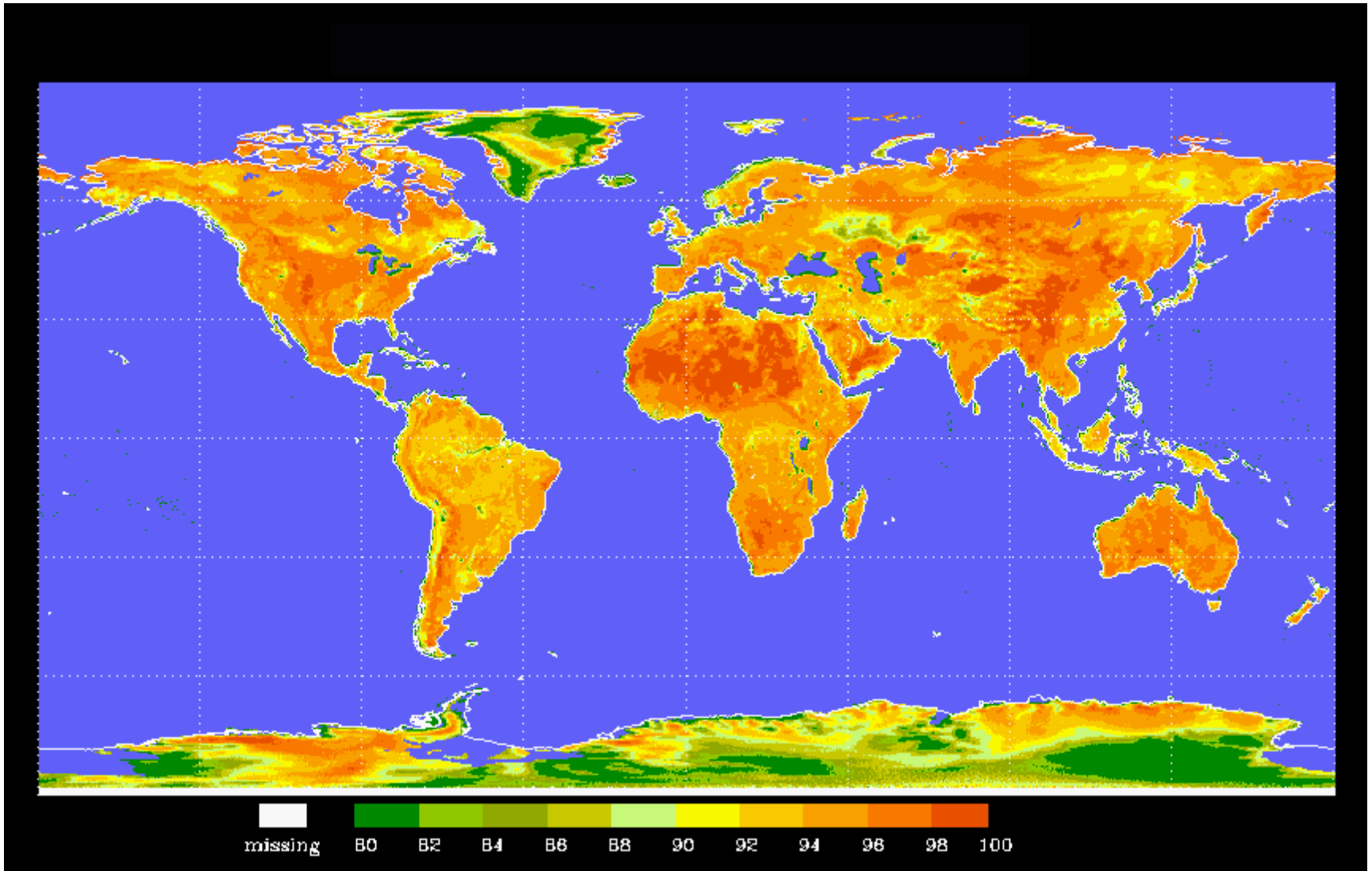
GDAS Atmospheric Total Precipitable Water



0 7 14 21 28 35 42 49 56 63 70 mm

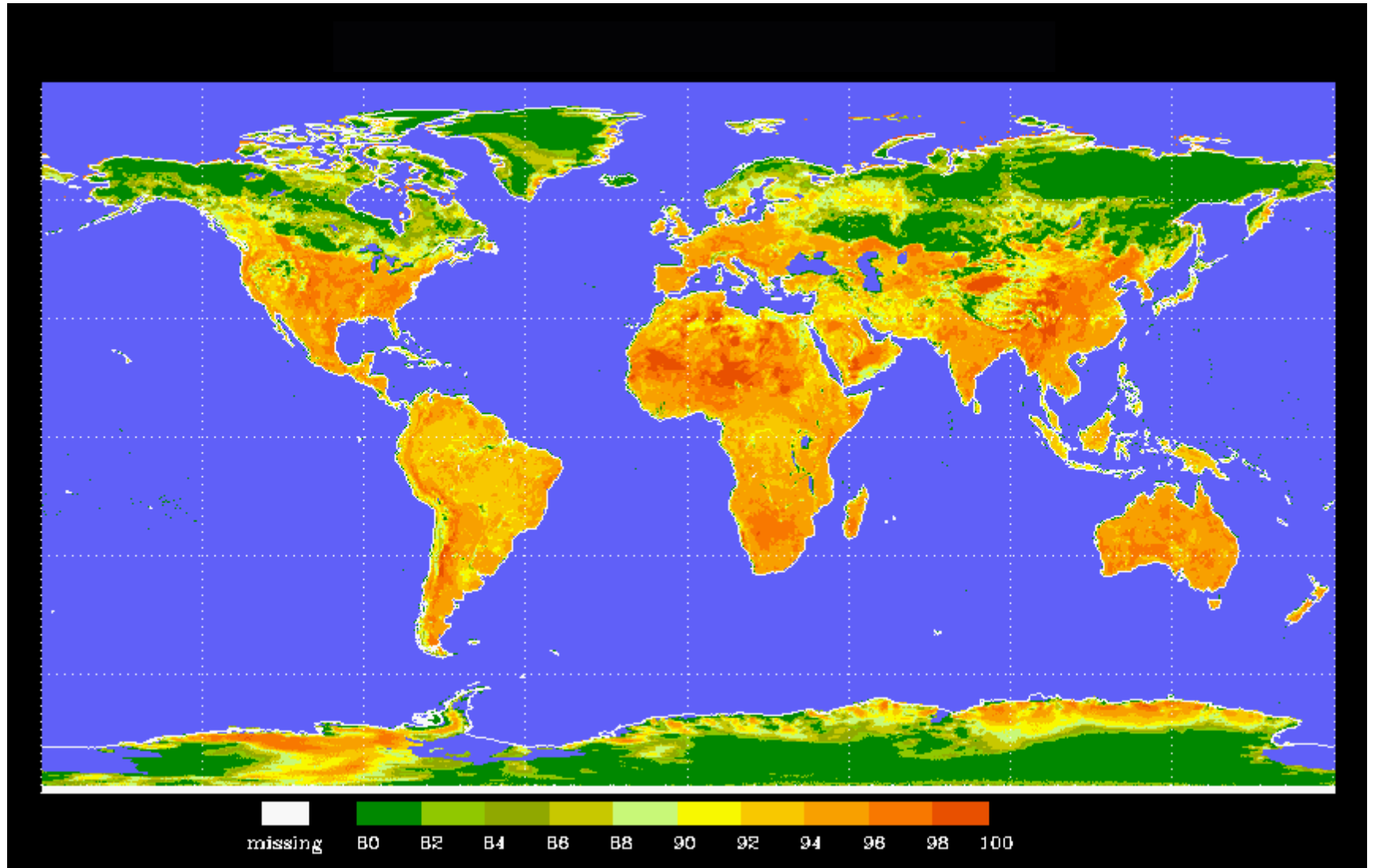
# SSM/I Land Surface Emissivity (v-pol) at 19.35 GHz

## March 1999



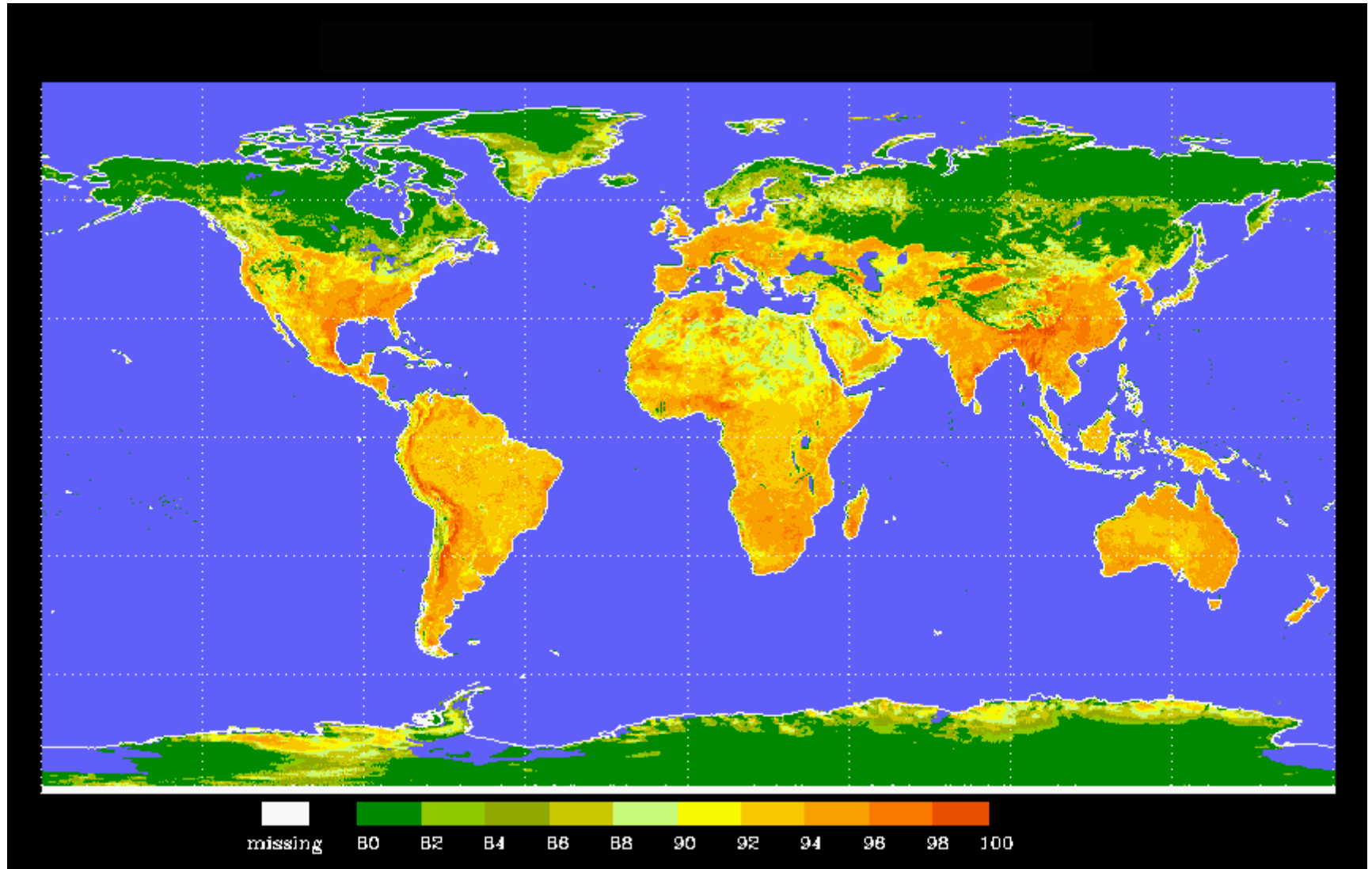
# SSM/I Land Surface Emissivity (v-pol) at 37.00 GHz

## March 1999



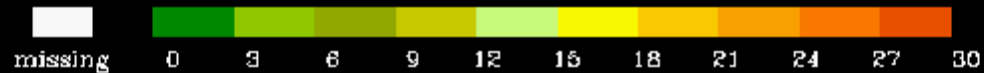
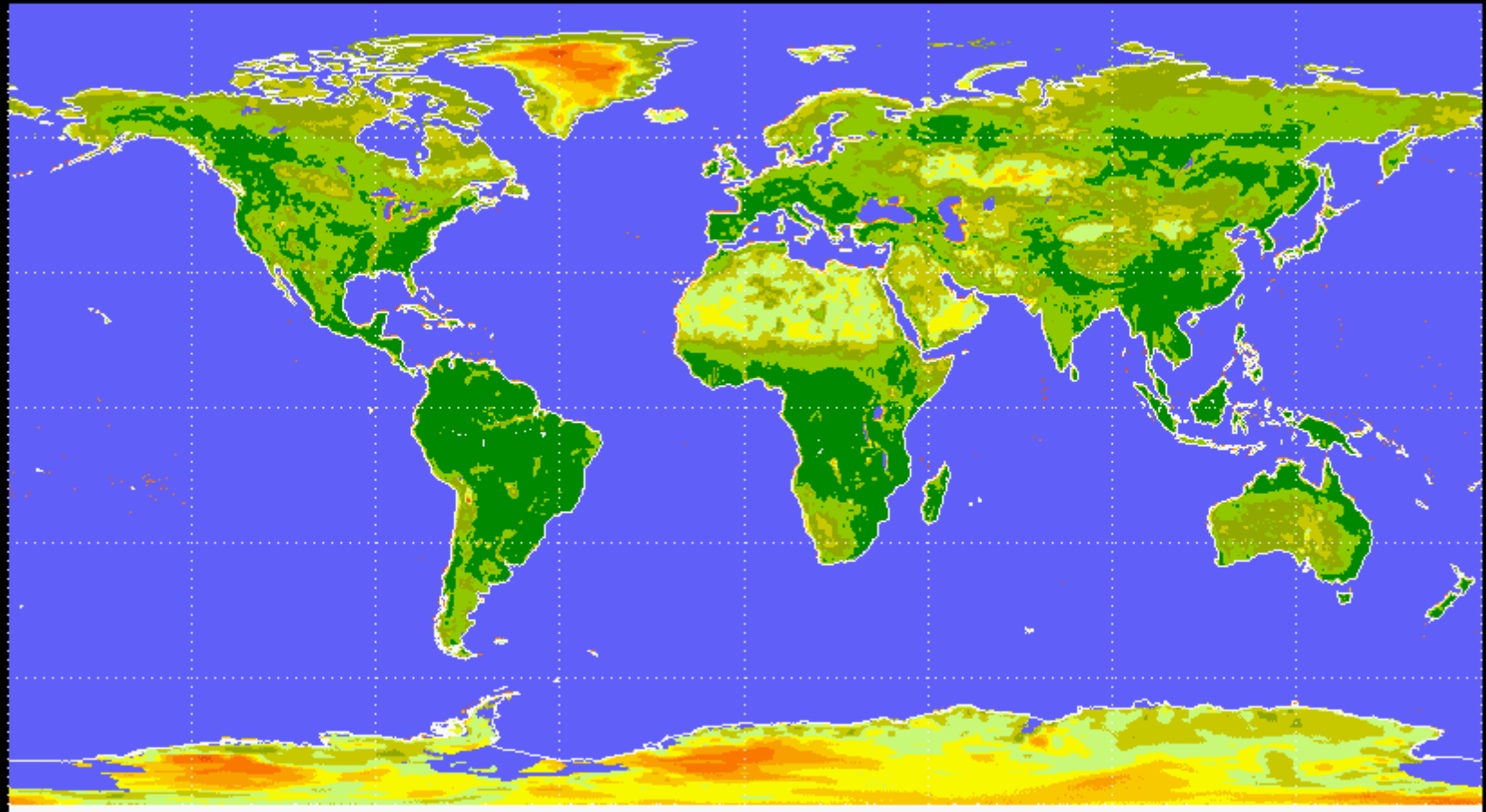
# SSM/I Land Surface Emissivity (v-pol) at 85.50 GHz

## March 1999

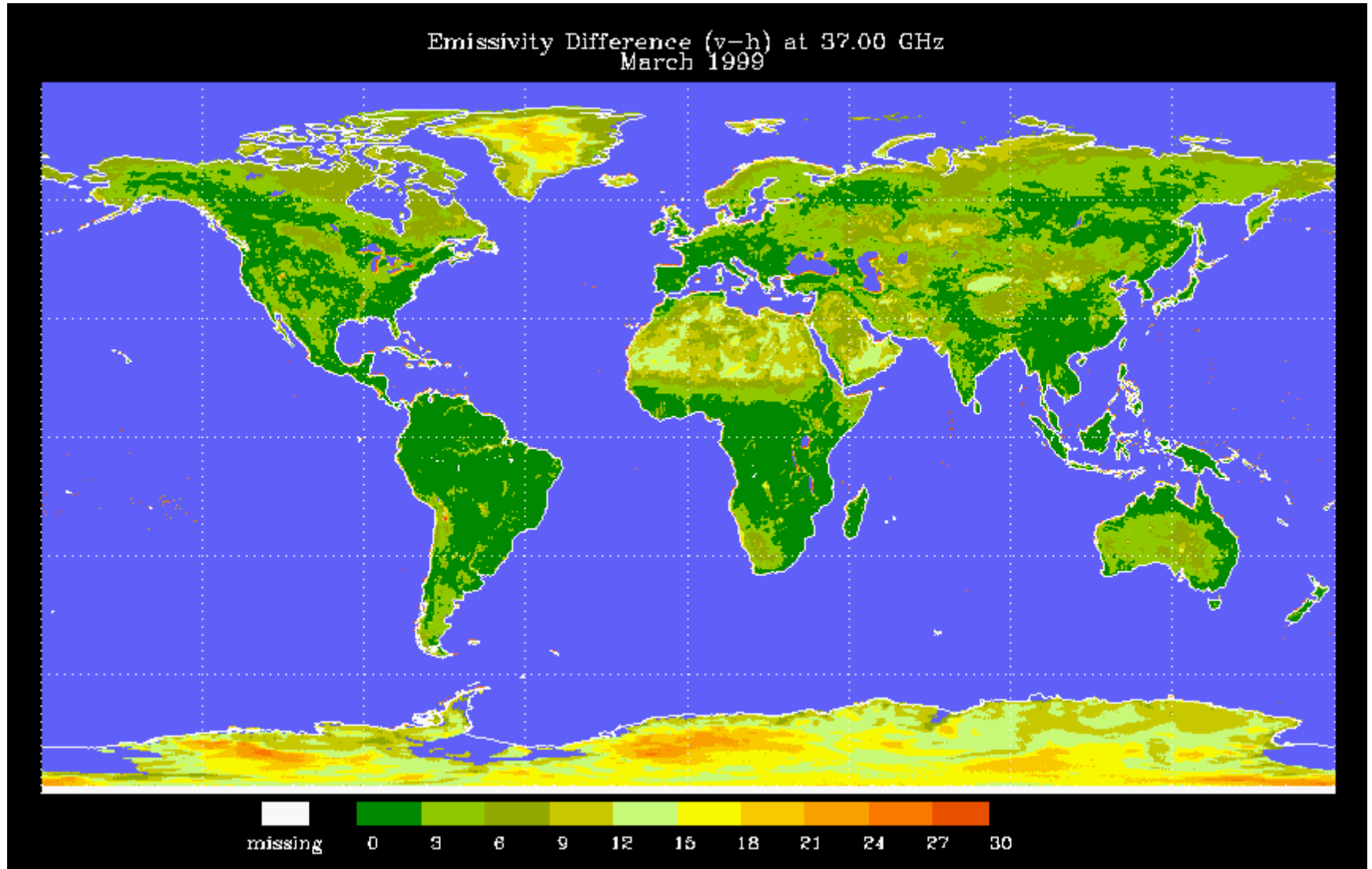


# Polarization Difference (19 GHz)

Emissivity Difference (v-h) at 19.35 GHz  
March 1999

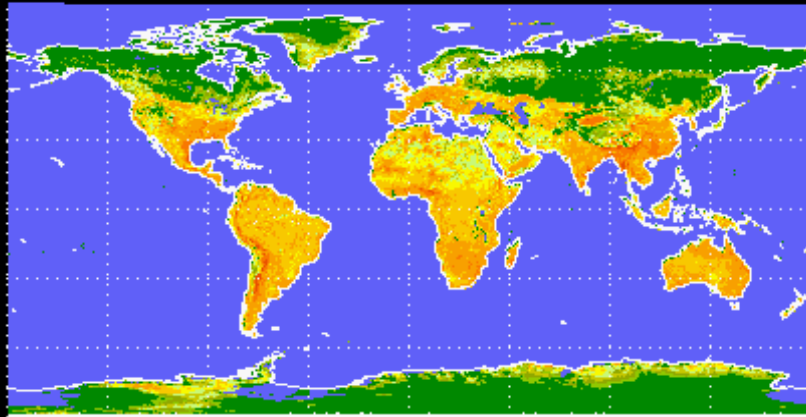


# Polarization Difference (37 GHz)

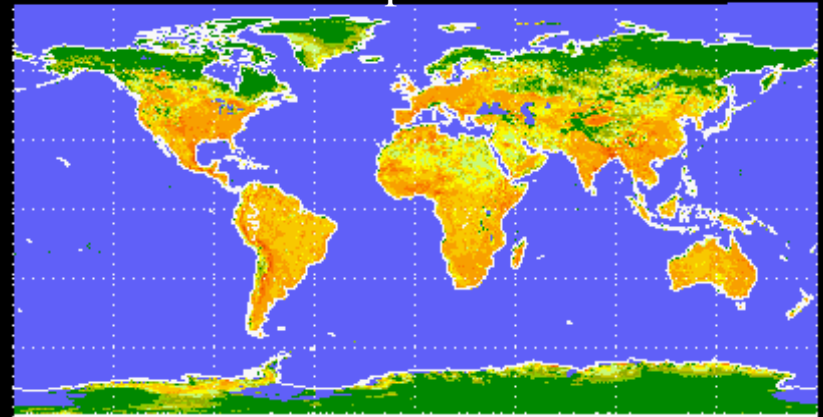


# Land Surface Emissivity at 85 GHz Derived from SSM/I

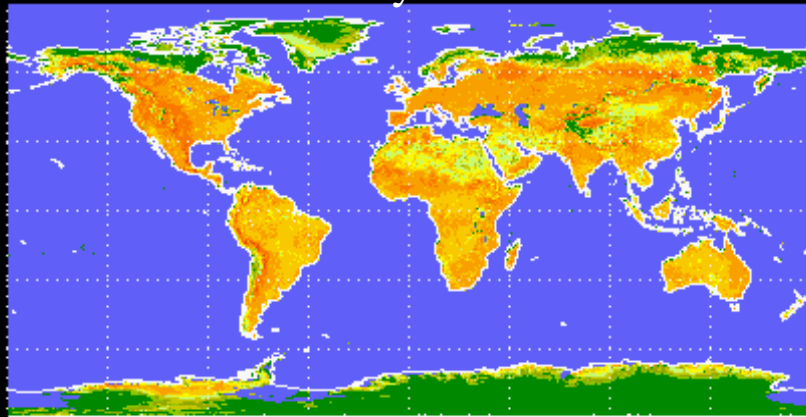
March 1999



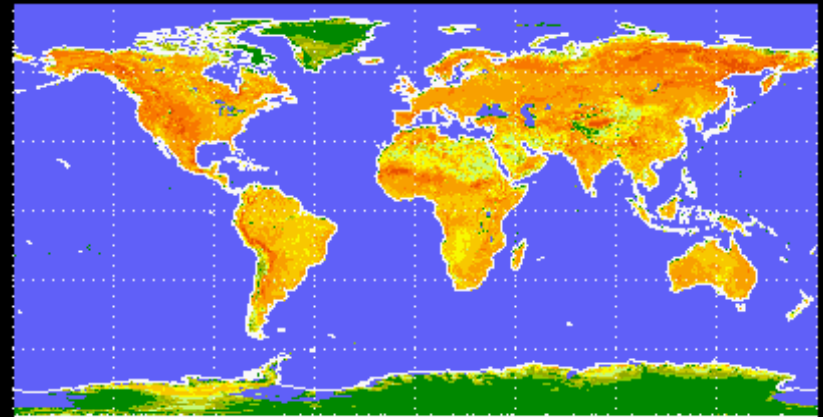
April 1999



May 1999



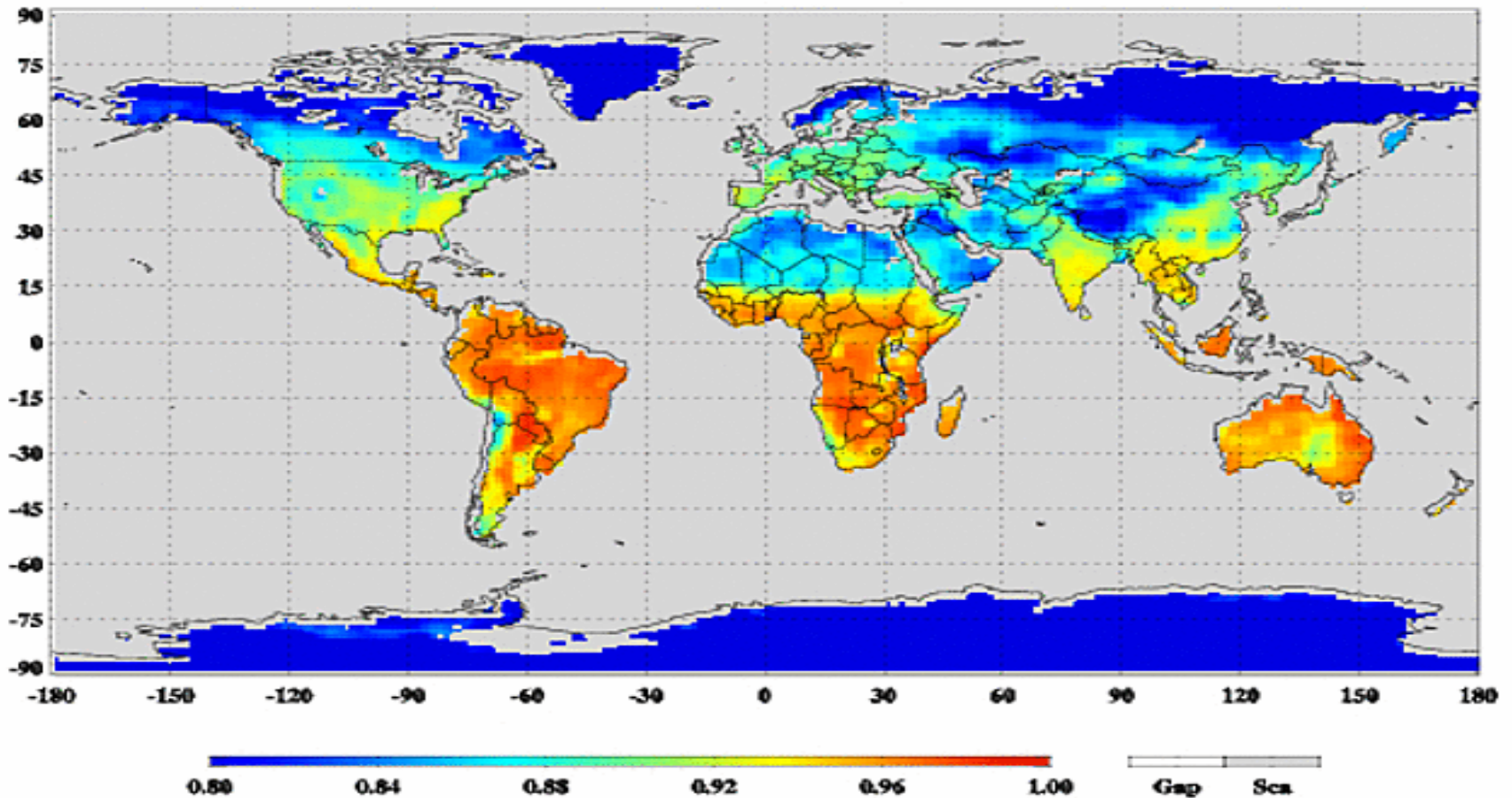
June 1999





# DMSP SSM/I Emissivity Climatology (1992-2006) at 37.0 GHz H-Pol

DMSP SSM/I Emissivity Climatology (1992~2006) at 37.0 GHz H-POL  
Jan. 1 ~ Jan. 5



# Global Land Emissivity Characterization

## SSM/I Fifteen Year Time Series

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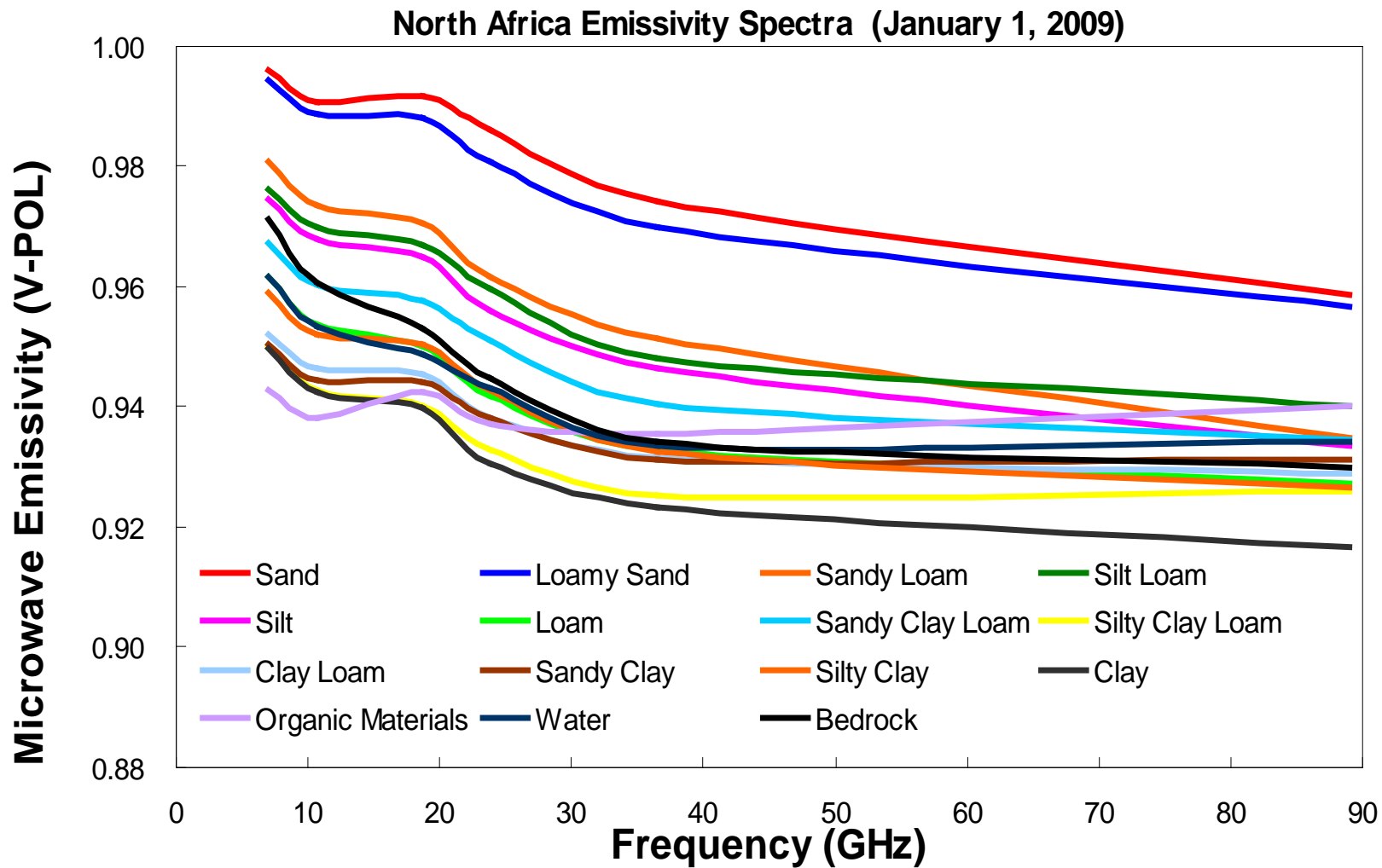
### *Findings:*

- Large seasonal change at higher frequencies
- Large polarization difference for several surfaces such as desert, snow, flooding
- Deserts appear as a scattering medium

SSM/I surface emissivity climatological data set is developed at various time scales (e.g. pentad, weekly and monthly, anomaly). SSM/I sensors from F10 to 15 satellites are intercalibrated to a reference satellite (F13).

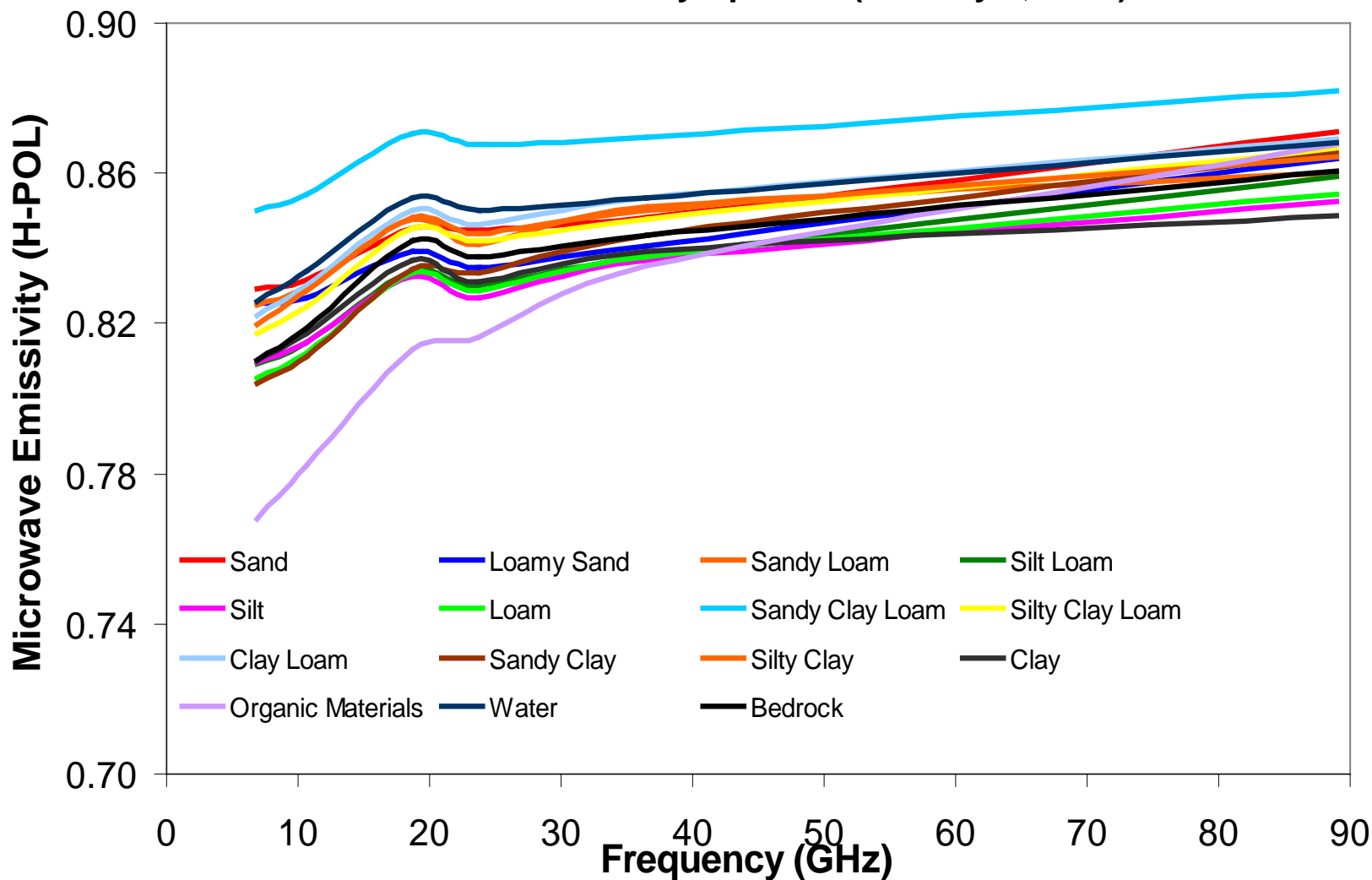
# Mean Emissivity Spectra over North Africa

## V-POL

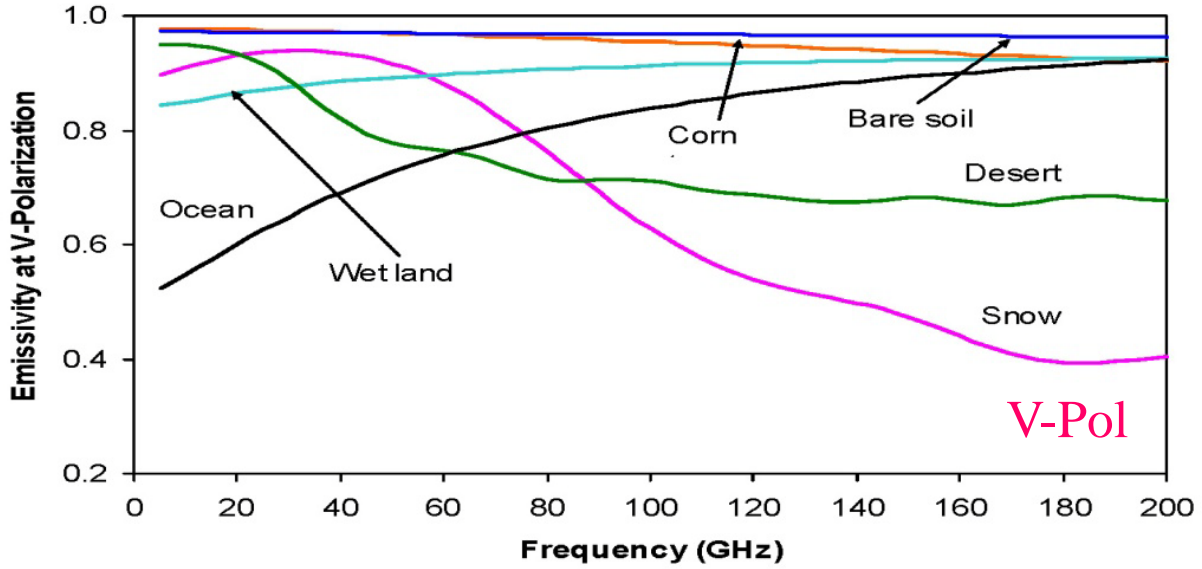


# Mean Emissivity Spectra over North Africa H-POL

North Africa Emissivity Spectra (January 1, 2009)

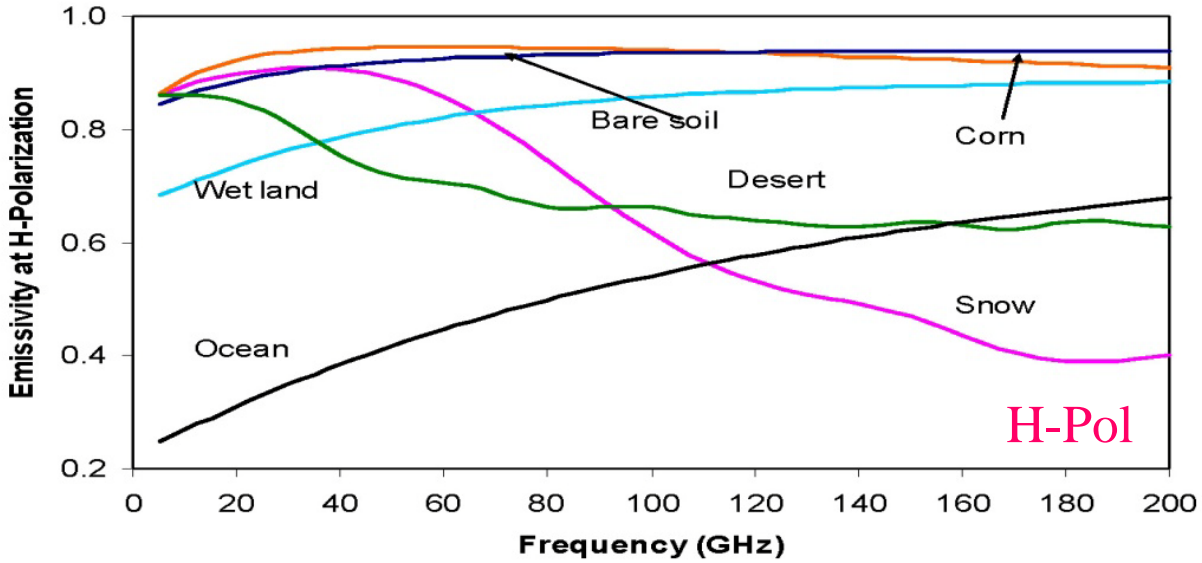


Surface emissivity spectra at a viewing angle of 53 degree



# Microwave Emissivity Spectra over Various Surface Conditions

Surface emissivity spectra at a viewing angle of 53 degree



# Microwave Emissivity Spectra over Various Surface Conditions (cont.)

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*By considering*

- **Open water** – two-scale roughness theory
- **Canopy** – Geometric optical scattering
- **Bare soil** – Coherent reflection and surface roughness
- **Snow/desert** – Dense medium scattering

*We obtained the following conclusions:*

Model-simulated microwave emissivity spectra is qualitatively consistent with satellite and ground-based retrievals. Deserts is treated as scattering in order to produce observed characteristics from satellite.

# Land Emissivity Summary

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- ✓ Land emissivity is
  - highly variable over deserts and large polarization difference
  - highly variable for snow conditions
  - high values over vegetated land ( $> 0.9$ )
- ✓ The uncertainty on retrieved land emissivity is larger at channels near water vapor and oxygen absorption lines

# Significance of Microwave Remote Sensing of Atmosphere

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- Validation of clouds predicted from forecast models
- Useful for climate and radiation feedback studies
- Complementary to the technology from visible wavelength
- Temperature and water vapor profiles under all weather conditions



# Principle of MW Remote Sensing of Clouds

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Emission-Based Radiative Transfer Equation:

$$T_b = \varepsilon T_s \exp(-\tau_s / \mu) + T_u + (1 - \varepsilon) T_d \exp(-\tau_s / \mu)$$



$$T_b = T_s [1 - (1 - \varepsilon) \Upsilon^2] - \Delta T (1 - \Upsilon) [1 + (1 - \varepsilon) \Upsilon]$$

If atmosphere is isothermal,  $\Delta T = 0$

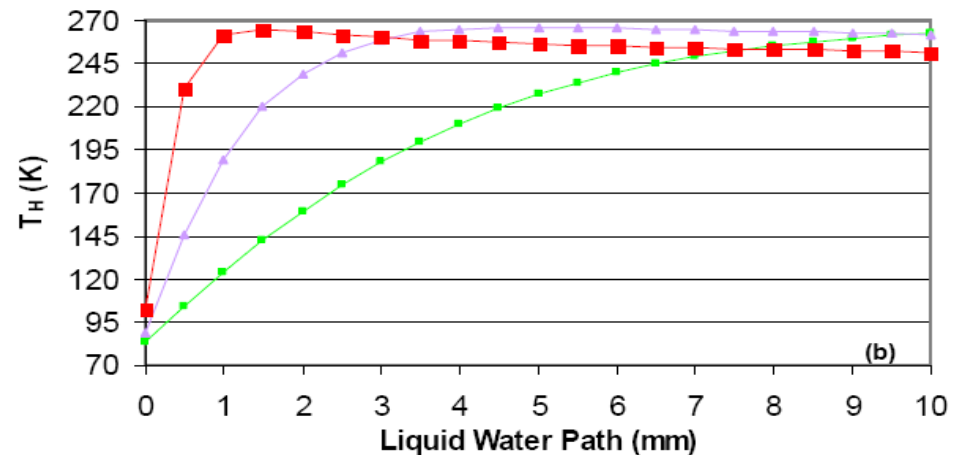
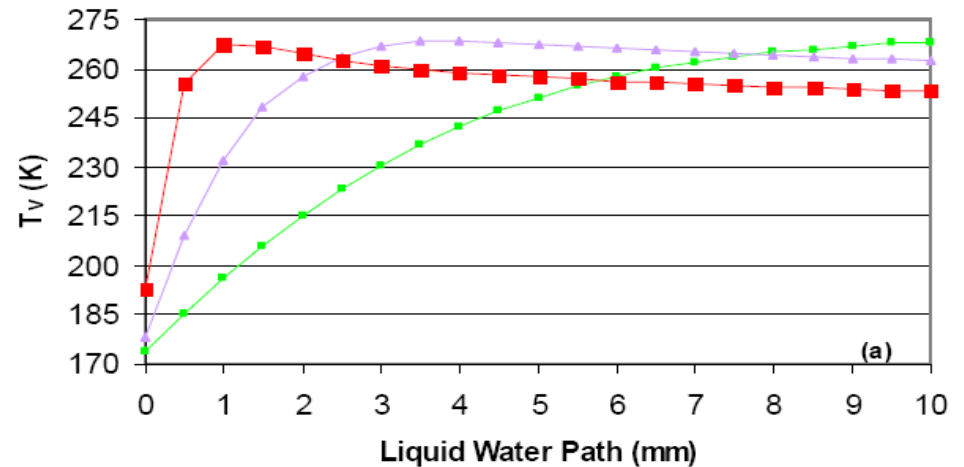
$$T_b = T_s [1 - (1 - \varepsilon) \Upsilon^2]$$

$T_b$  is a quadratic function of atmospheric transmittance which is determined by cloud liquid and water vapor absorption.

This is a basic principle for microwave remote sensing of cloud properties!

# Microwave Remote Sensing of Liquid Phase Clouds

- A large contrast exists between cloudy and “clear” conditions, thanks to low ocean emissivity.
- Brightness temperature increases exponentially with liquid water, thus requiring a logarithmic function for linearization
- “The linear regime” is dependent on frequency. We can meet the need of more customer (e.g. rain water...) if the measurements at each frequency are optimally utilized in the retrievals



—■— 10.65 GHz    —▲— 18.7 GHz    —■— 36.5 GHz

# Emission-Based RTM

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$$T_b = T_s [1 - (1 - \varepsilon) \Upsilon^2]$$

$$\Upsilon = \exp[-(\tau_o + \tau_V + \tau_L) / \mu]$$

$$\tau_V = \kappa_V V = \int_0^\infty \kappa^{H_2O} \rho_V dz$$

$$\tau_L = \kappa_L L = \int_{\Delta Z} \kappa^{Ray} LWC dz$$

$$\kappa^{Ray} = \frac{6\pi}{\lambda \rho_w} \text{Im} \left\{ \frac{m^2 - 1}{m^2 + 2} \right\}$$

## Emission-Based RTM (cont.)

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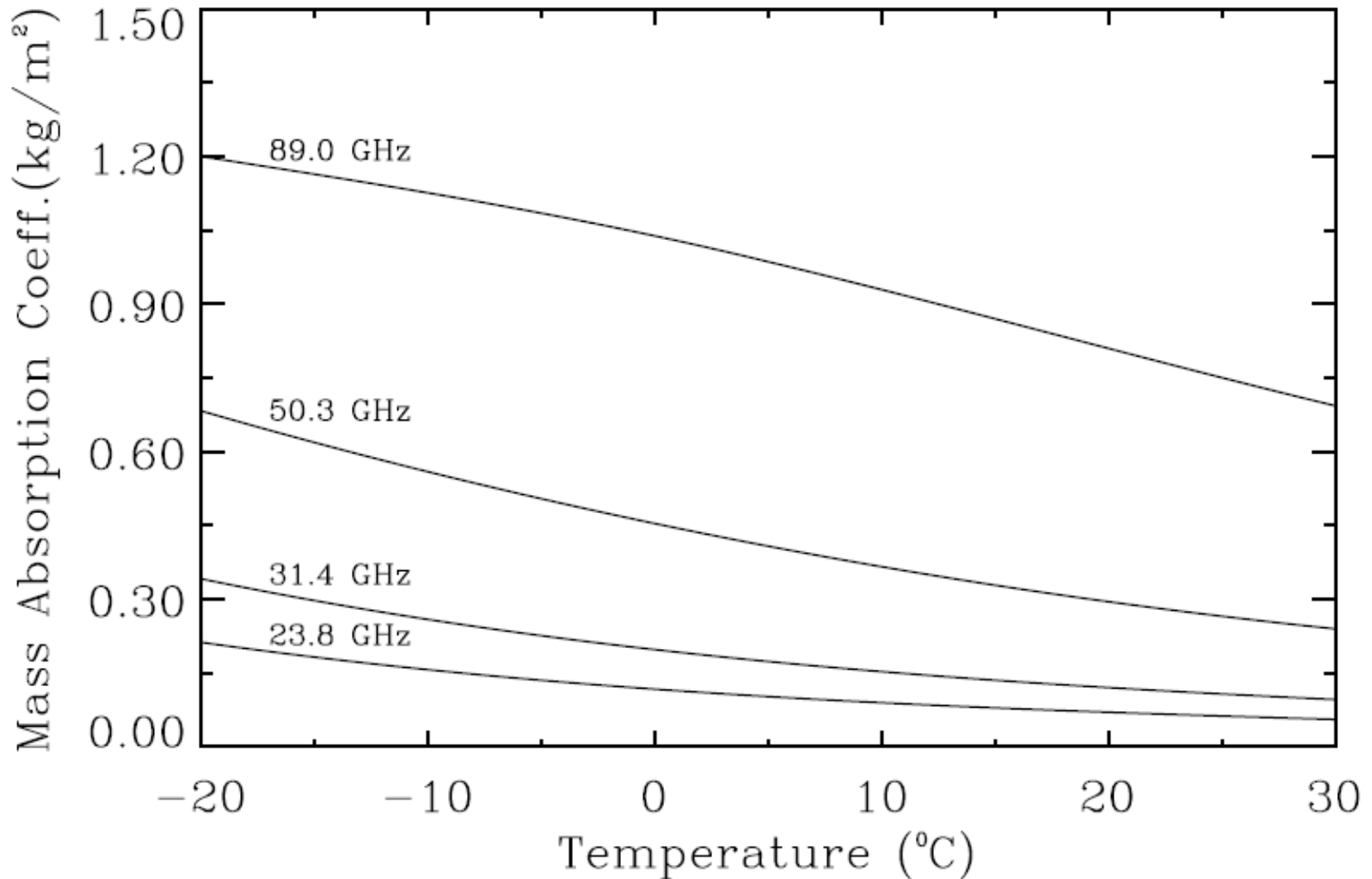
$$\Upsilon = \exp[-(\tau_o + \kappa_V V + \kappa_L L)/\mu]$$

$$\kappa_V V + \kappa_L L = -\frac{\mu}{2} \left\{ \ln(T_s - T_b) - \ln[T_s (1 - \varepsilon)] + \frac{2\tau_{o_2}}{\mu} \right\}$$

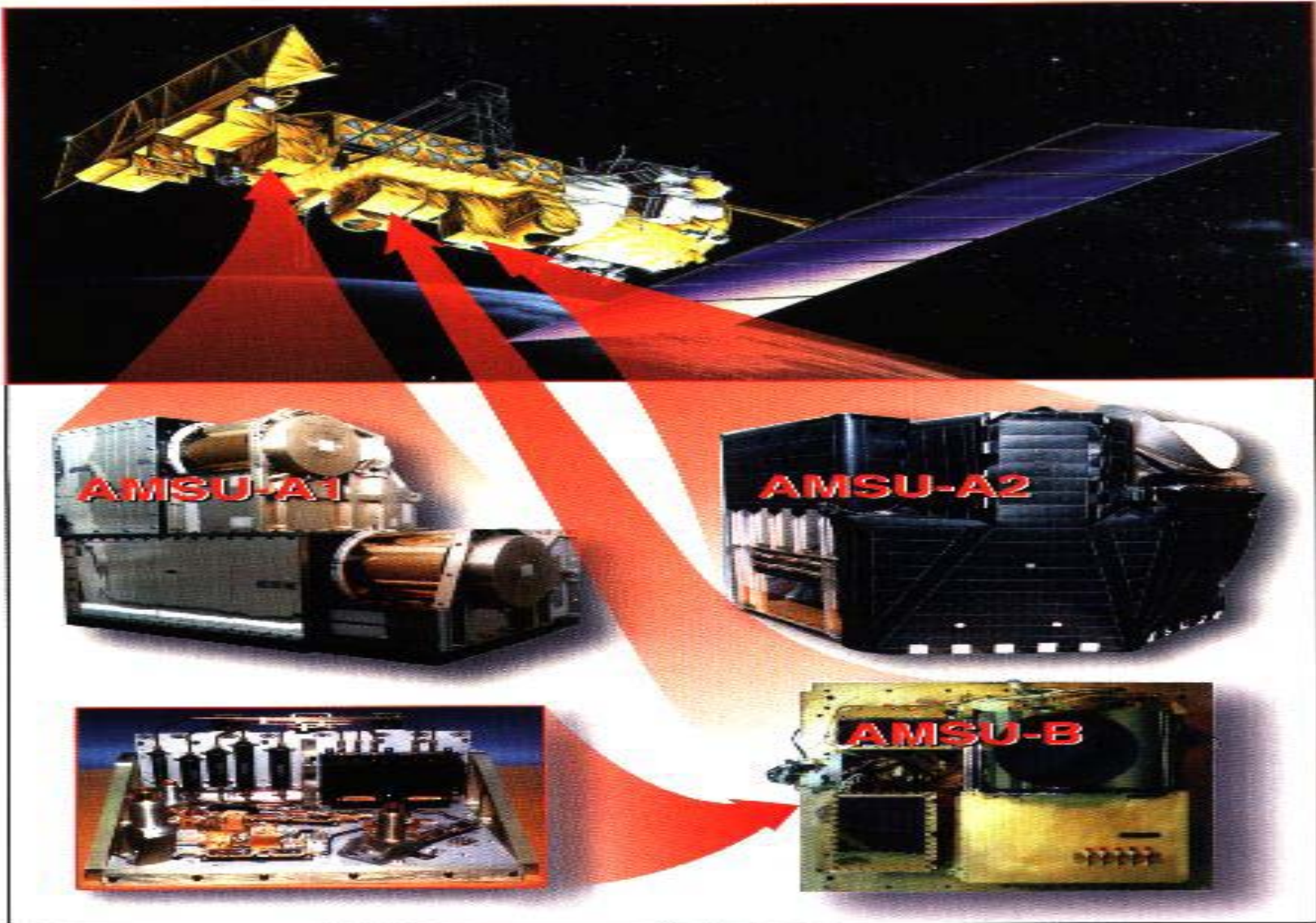
$$L = a_0 \mu [\ln(T_s - T_{b,1}) - a_1 \ln(T_s - T_{b,2}) - a_2]$$

$$V = b_0 \mu [\ln(T_s - T_{b,1}) - b_1 \ln(T_s - T_{b,2}) - b_2]$$

# Cloud Absorption in Relation to Temperature



# AMSU on Board NOAA POES Since 1998



# AMSU on Board NOAA POES Since 1998 (cont.)

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There are 20 channels divided into three sub-modules:

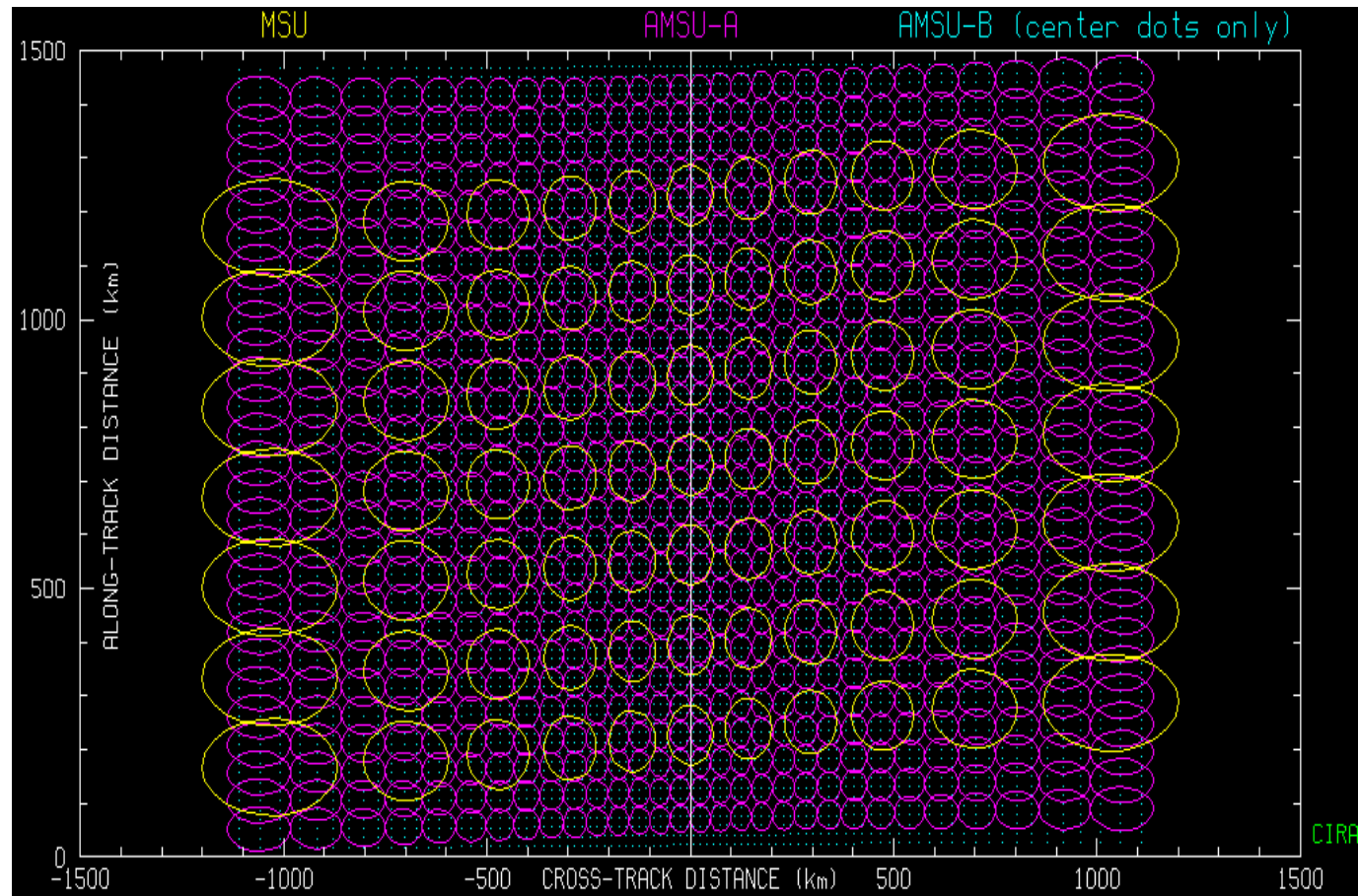
AMSU-A1 – 13 channels located near the 60 GHz oxygen absorption band

AMSU-A2 – two window channels at 23.8 and 31.4 GHz

AMSU-B – two high frequency channels at 89 and 150 GHz,  
and three channels near 183 GHz water vapor absorption line

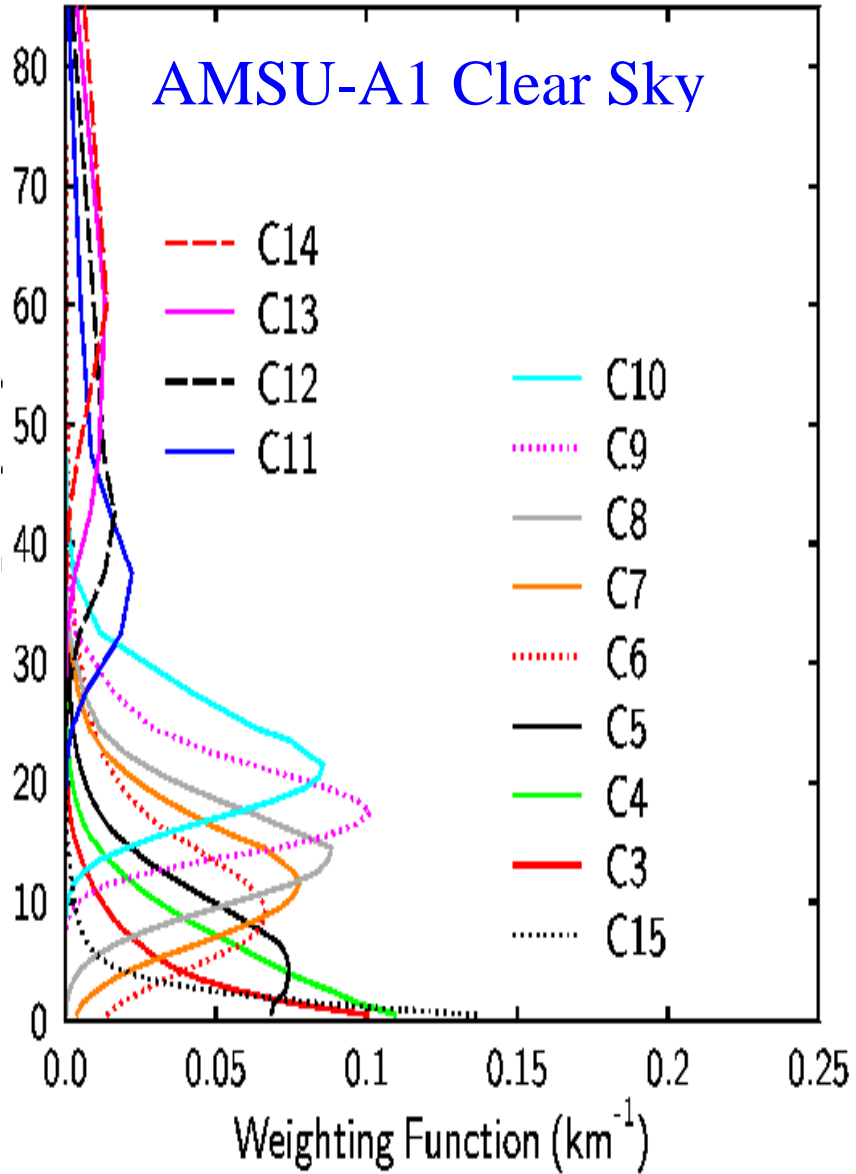
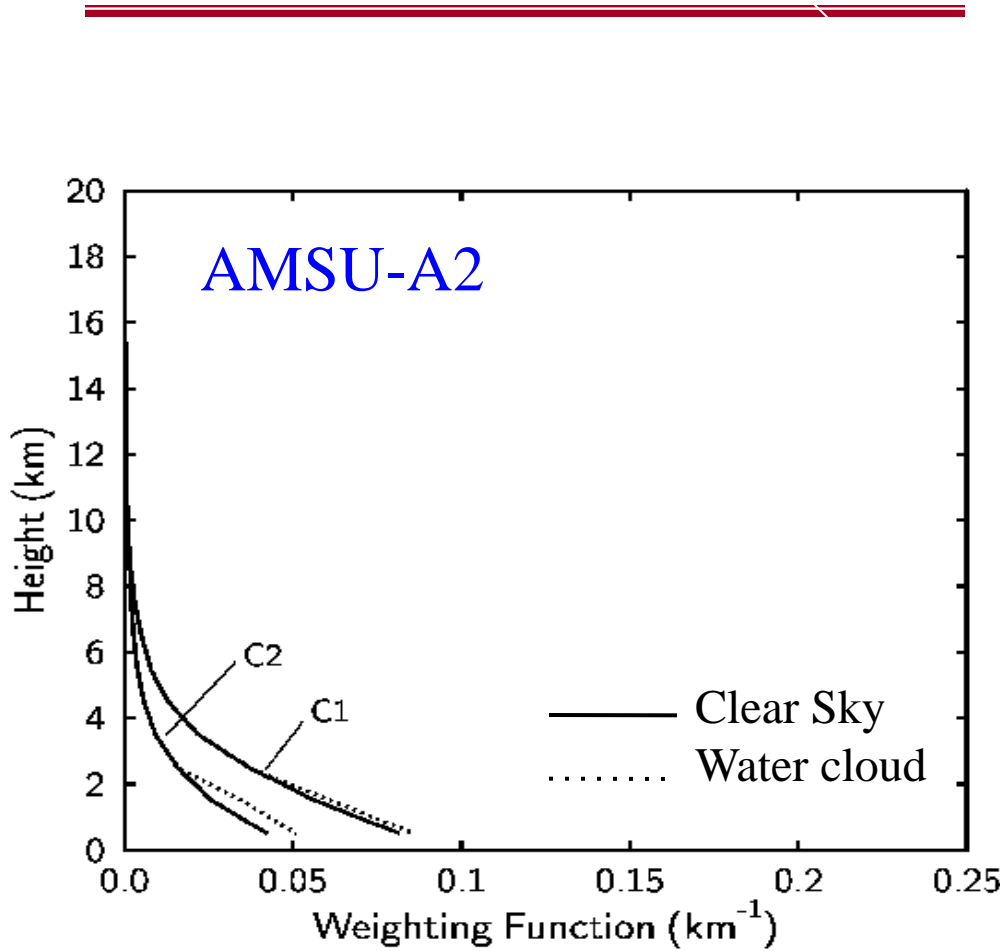
# AMSU on Board NOAA POES Since 1998 (cont.)

The field-of-view size varies as the instruments scan crossing track.

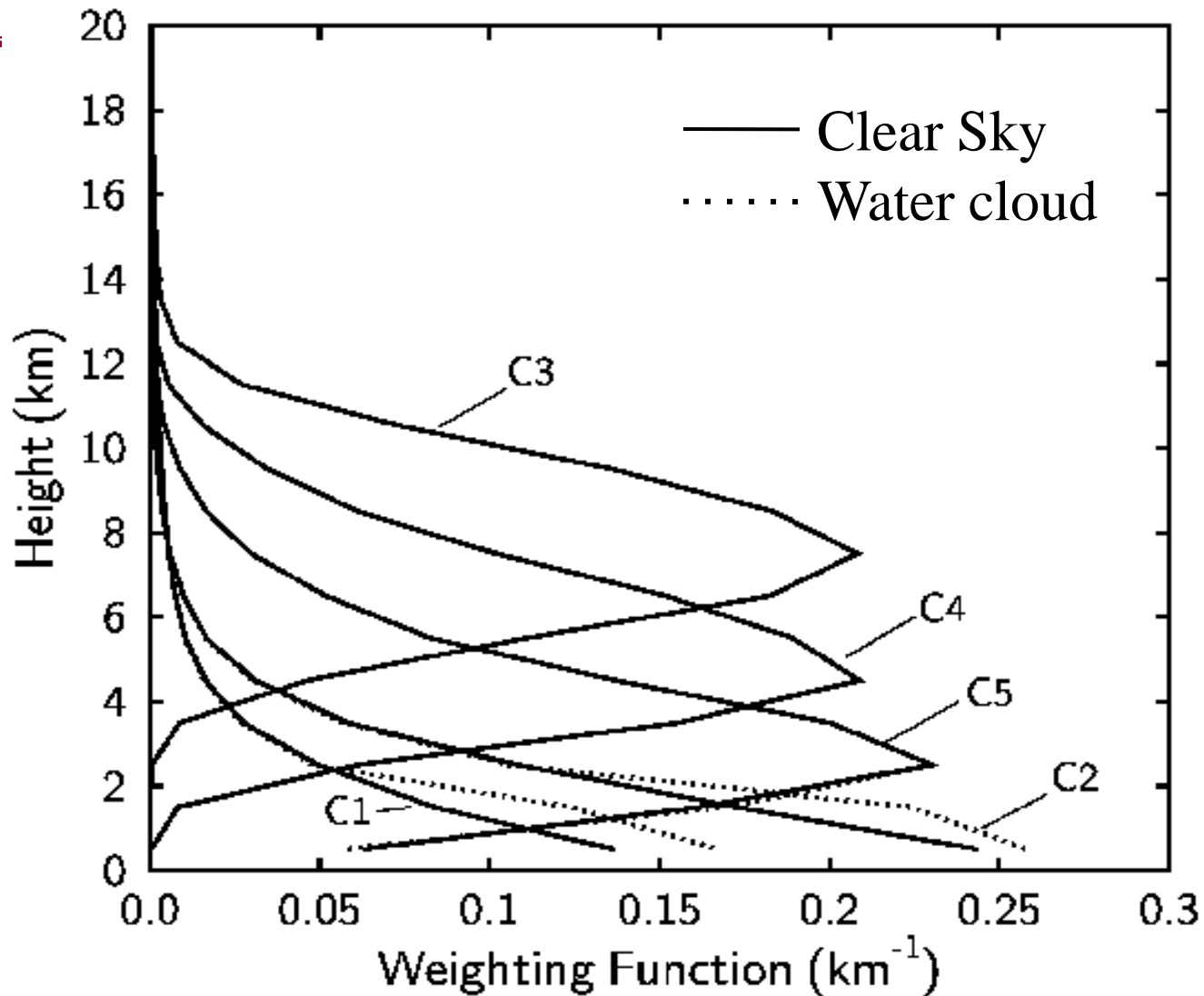




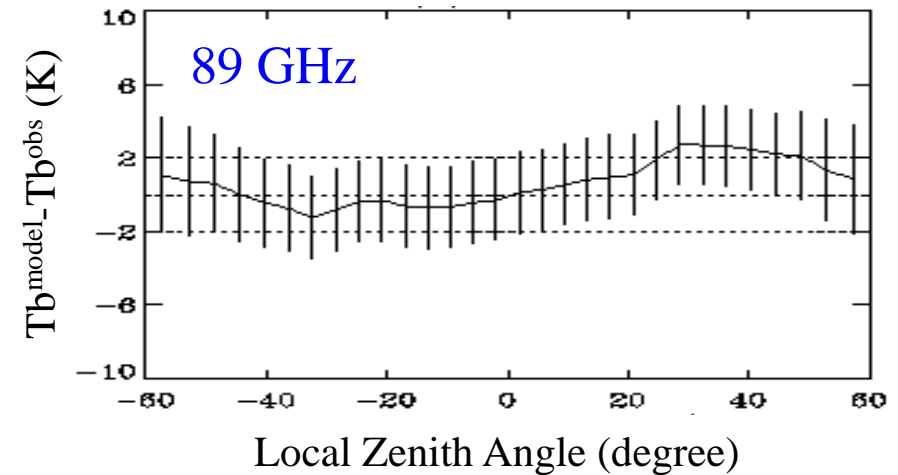
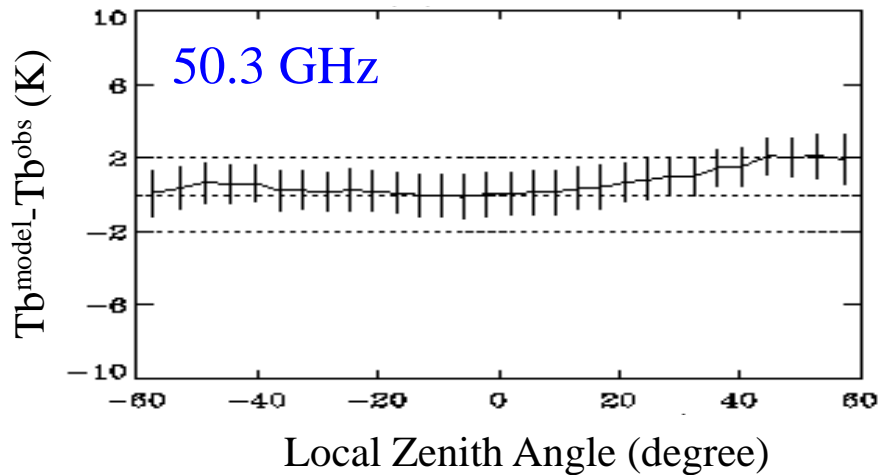
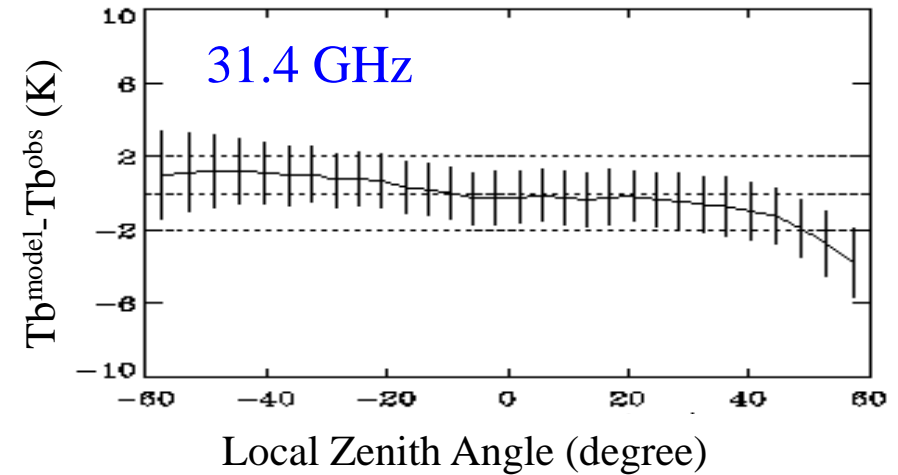
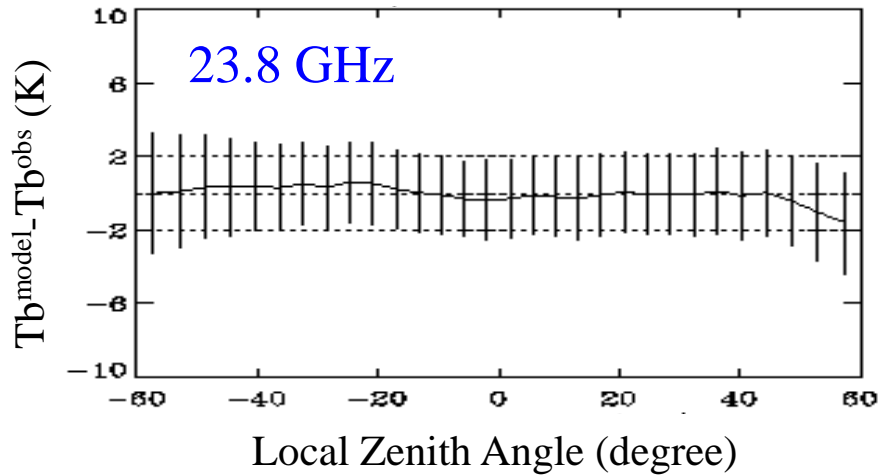
# AMSU-A Weighting Functions



# AMSU-B Weighting Functions

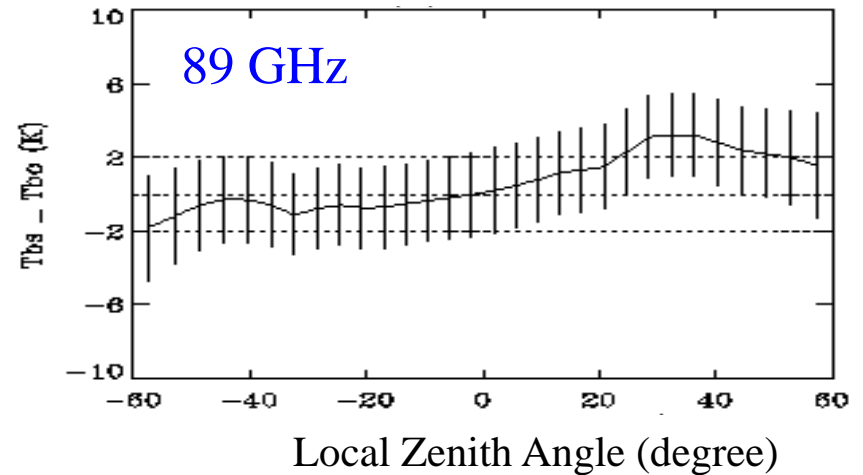
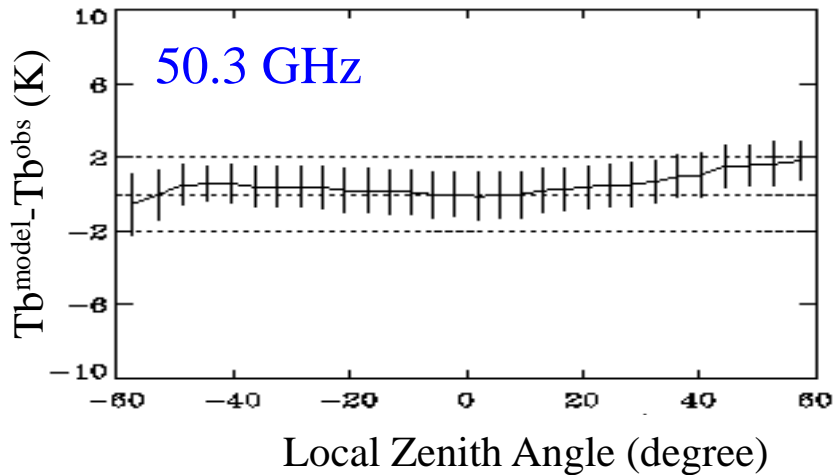
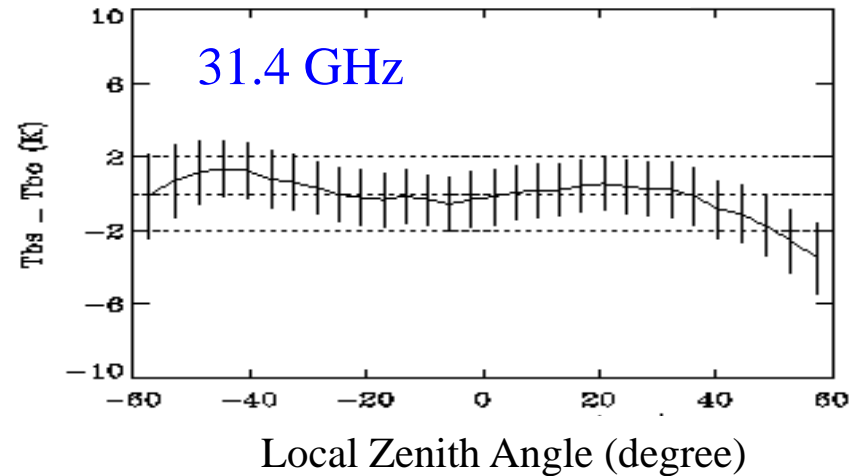
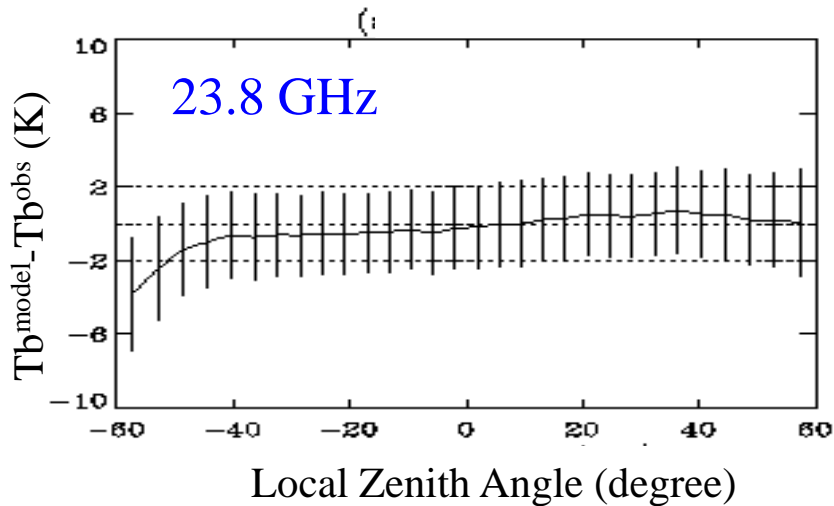


# NOAA-16 AMSU-A Radiance Asymmetry (Channels 1, 2, 3, 15)



$$\Delta T = A_0 \exp\{ -0.5[(\theta - A_1) / A_2]^2 \} + A_3 + A_4 \theta + A_5 \theta^2$$

# NOAA-16 AMSU-A Radiance Asymmetry (Channel 1,2,3,15)



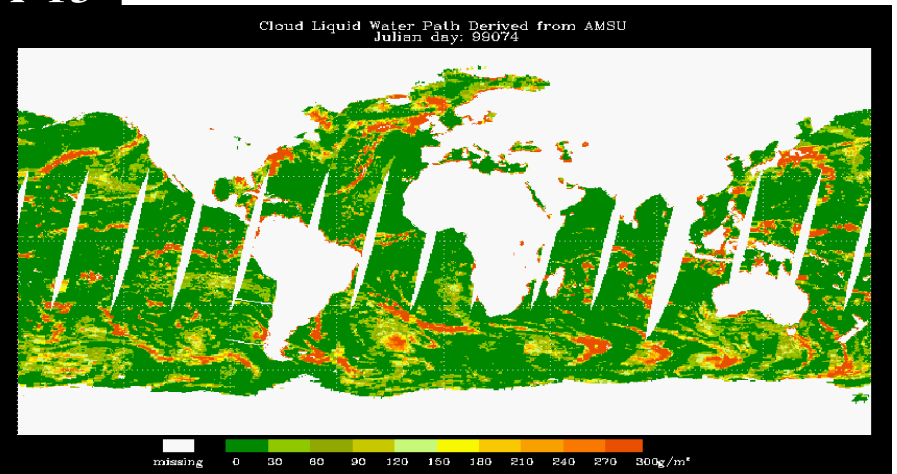
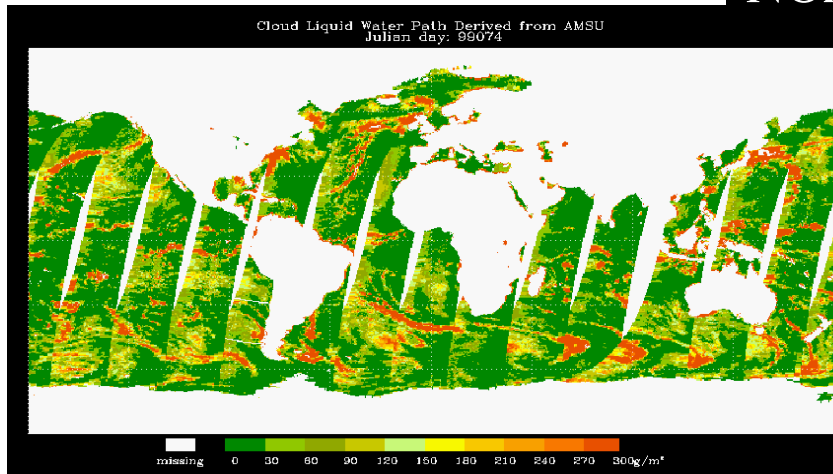
$$\Delta T = A_0 \exp\{ -0.5[(\theta - A_1) / A_2]^2 \} + A_3 + A_4 \theta + A_5 \theta^2$$

# AMSU Cloud Liquid Water

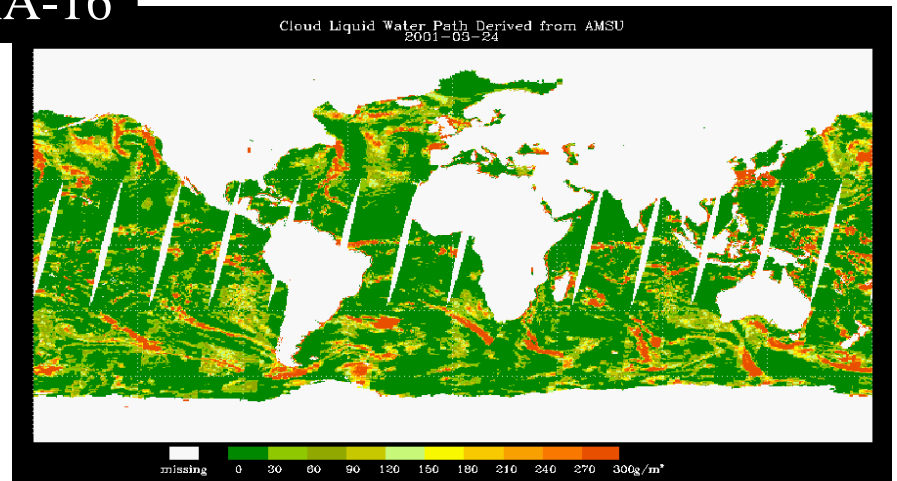
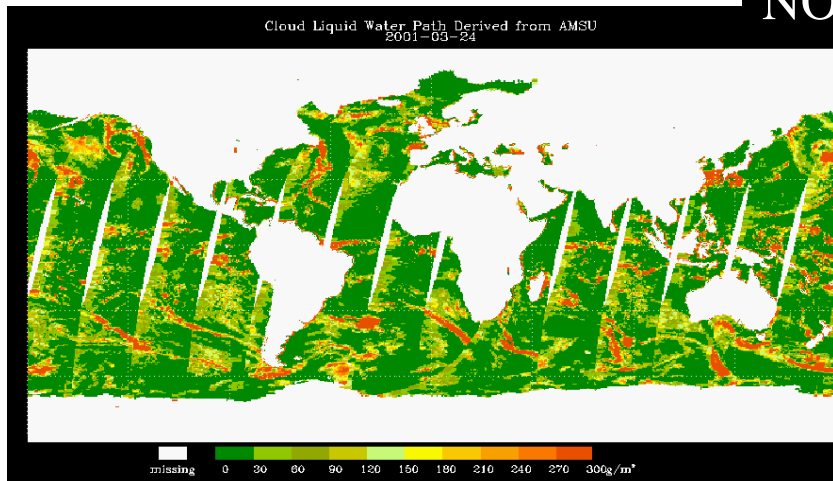
Before Asymmetry Correction

After Asymmetry Correction

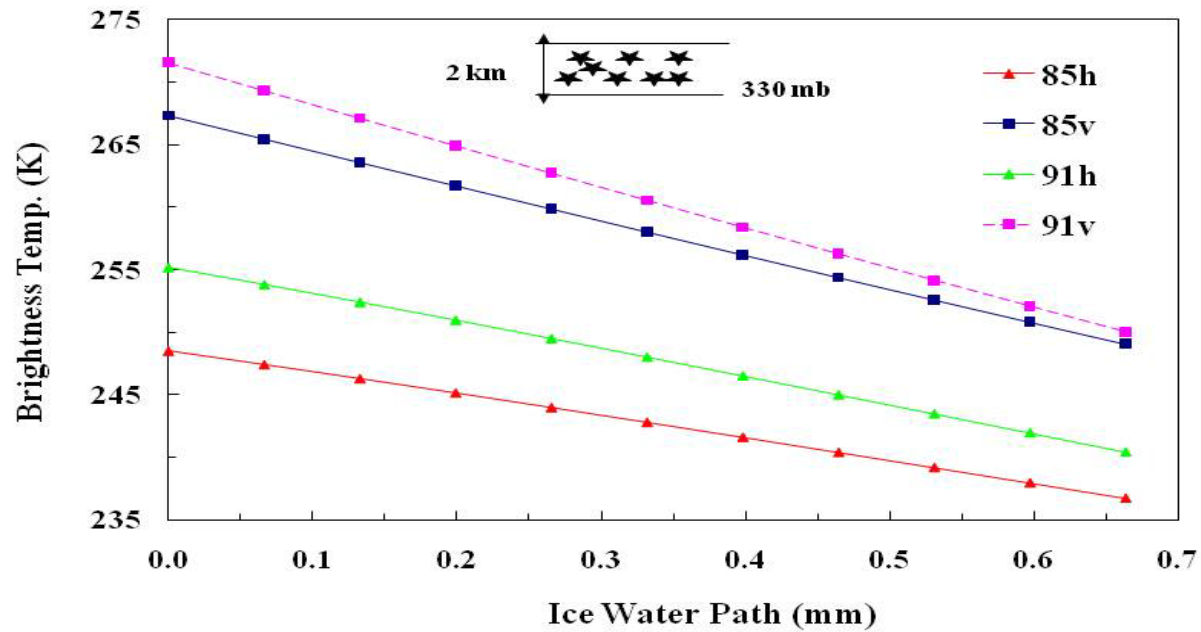
NOAA-15



NOAA-16



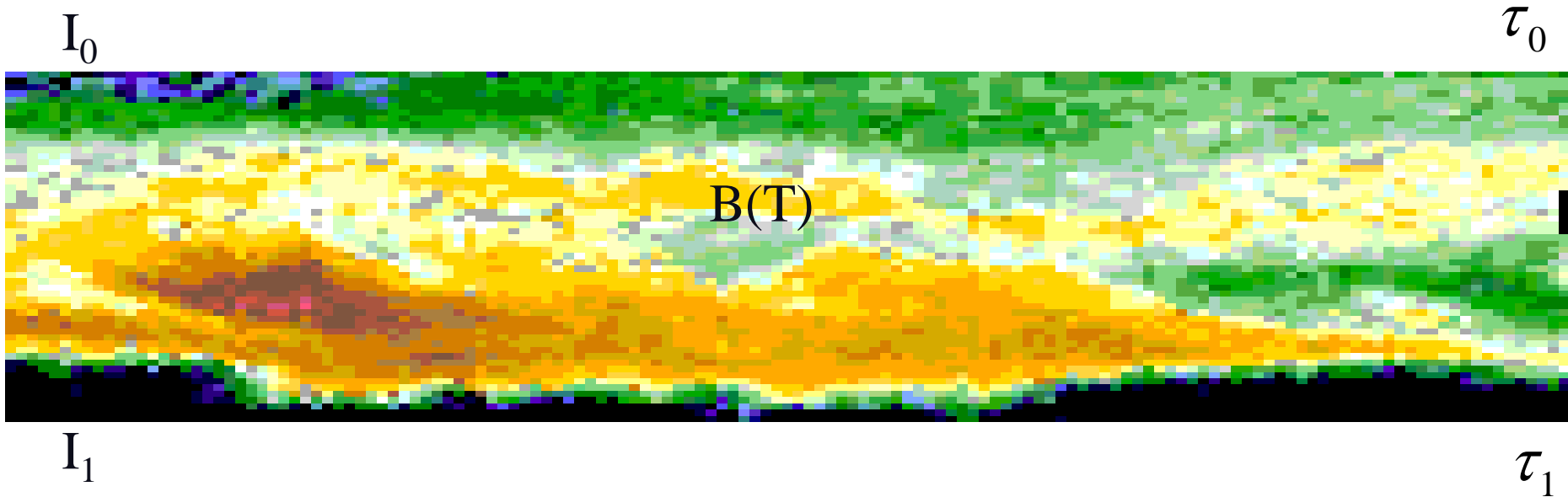
# Microwave Remote Sensing of Ice Phase Clouds



# Cloud Ice Water Path Algorithm

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$$I(\tau, \mu) = \frac{(I_0 - B)[\gamma_1 e^{-\kappa(\tau-\tau_1)} - \gamma_2 e^{\kappa(\tau-\tau_1)}] - (I_1 - B)[\beta^{-1} e^{\kappa(\tau-\tau_0)} - \beta e^{-\kappa(\tau-\tau_0)}]}{\gamma_4 e^{-\kappa(\tau_1-\tau_0)} - \gamma_3 e^{\kappa(\tau_1-\tau_0)}} + B$$



# Cloud Ice Water Path Algorithm

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## Asymptotic Limits:

### 1. Emission Approach

$$I(\tau_1, \mu) = B[1 - (1 - \varepsilon)e^{-2\tau_1/\mu}] - [B(T_s) - B(T)](1 - e^{-\tau_1/\mu})[1 + (1 - \varepsilon)e^{-\tau_1/\mu}]$$

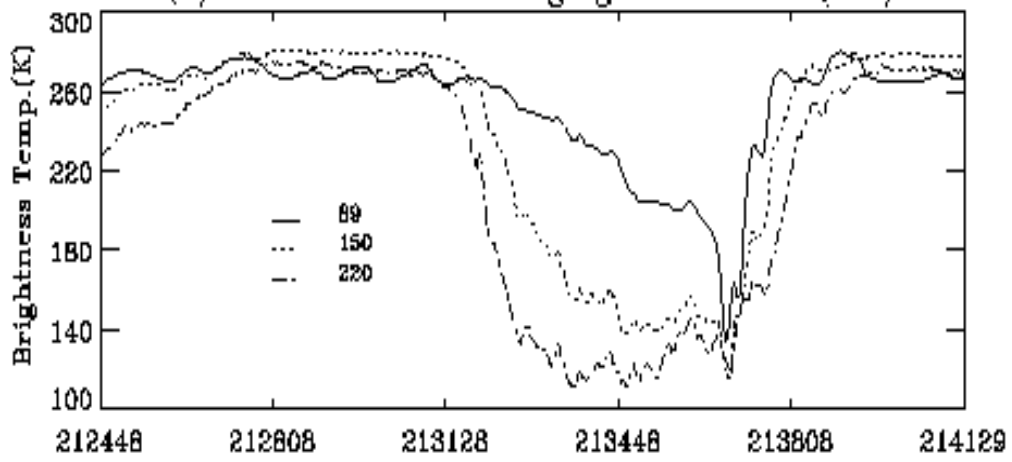
### 2. Scattering Approach:

$$I(\tau_0, \mu) = \frac{I(\tau_1, \mu)}{1 + \Omega(\mu)} \quad \Omega(\mu) = \frac{IWP}{\mu \rho_i D_e} \Omega_N(x_e, m)$$

References: Weng and Grody (2000, JAS), Zhao and Weng (2002, JAM)

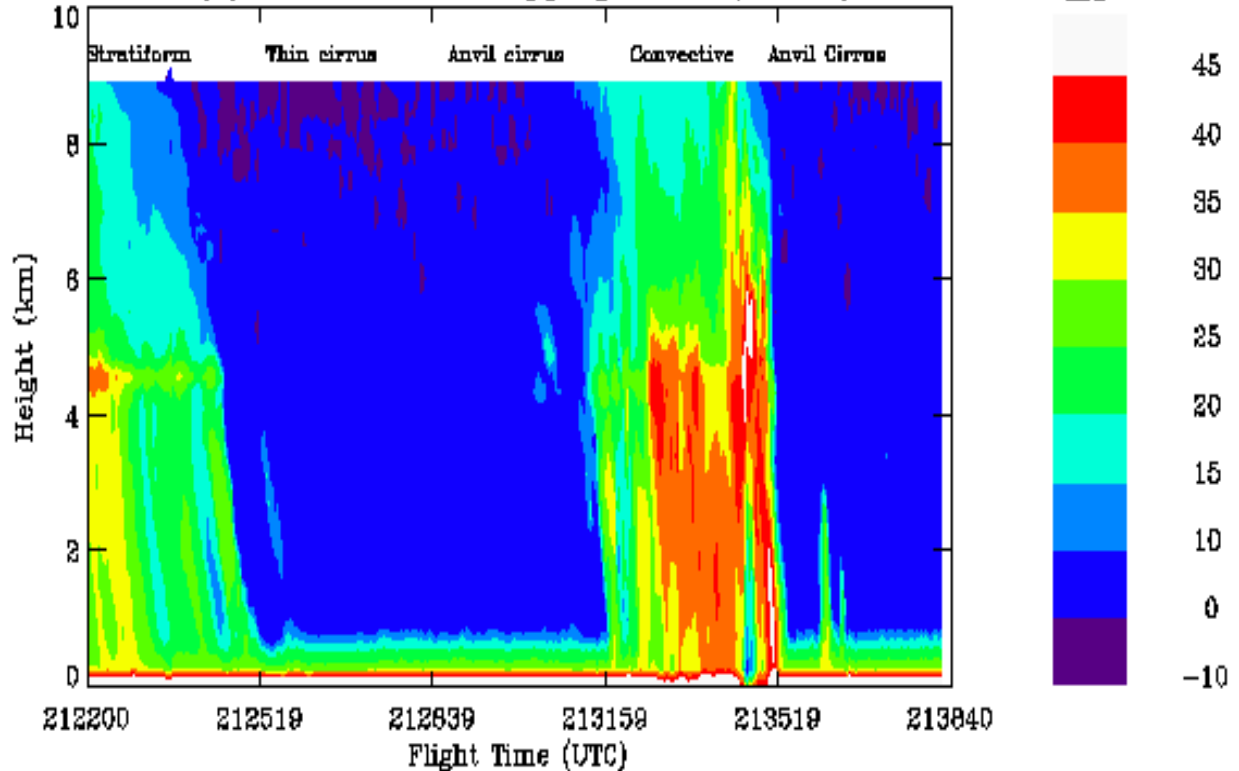


(a) Millimeter-wave Imaging Radiometer (MIR)



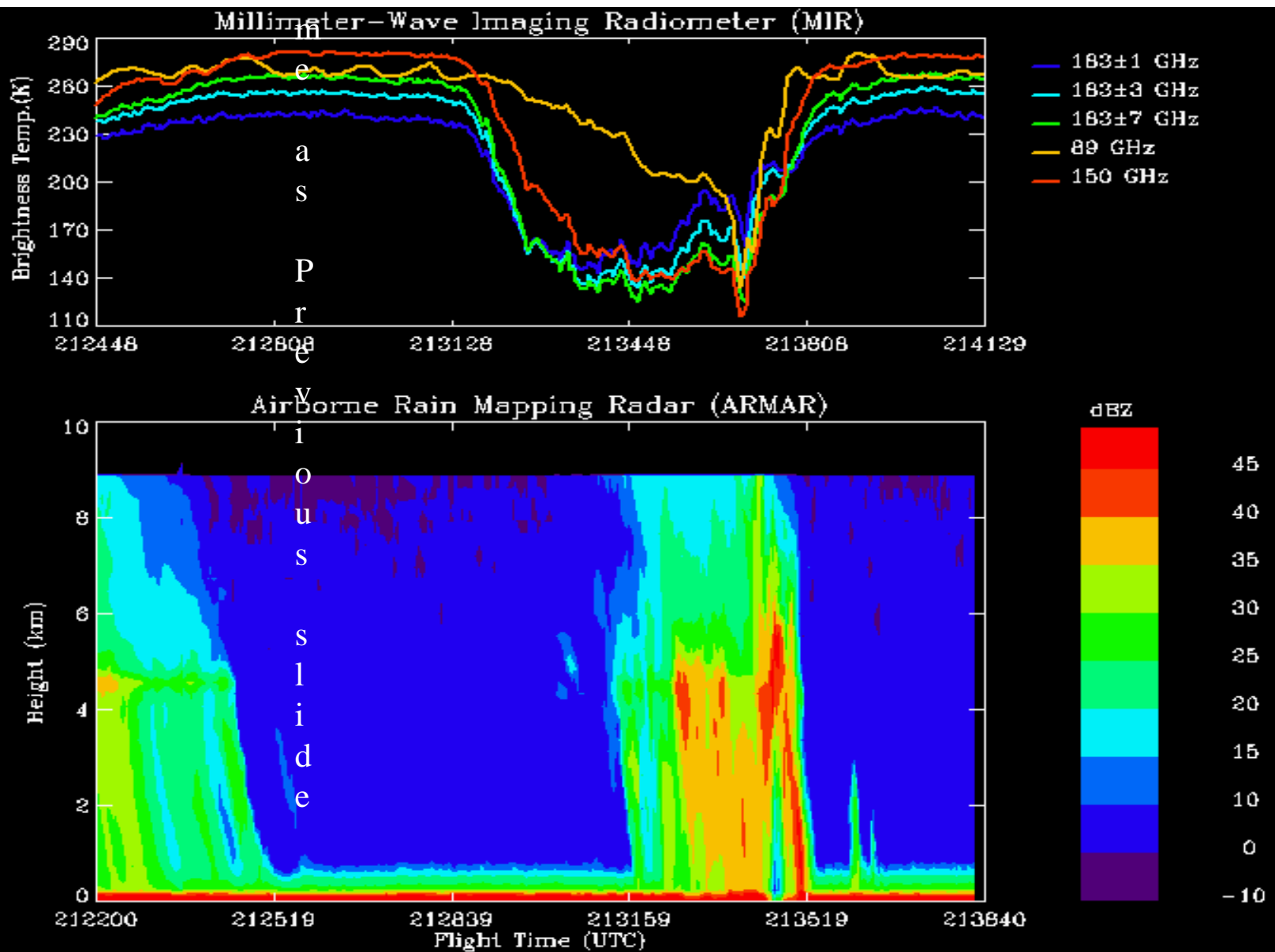
# ER-2 MIR, DC-8 ARMAR, MODIS Simulator Measurements

(b) Airborne Rain Mapping Radar (ARMAR)



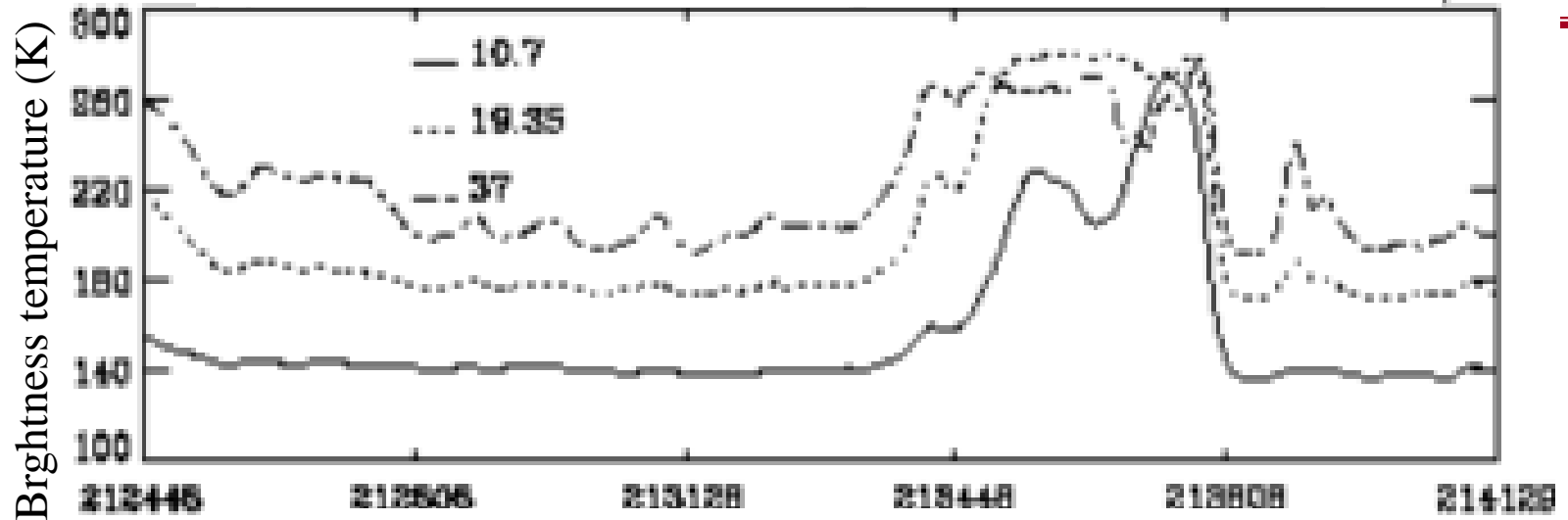
Three millimeter wavelength channels provide the overall needed sensitivity for cloud ice microphysics which can be uniquely used for precipitation mapping.

Same figures as those on the previous slide, but colored.

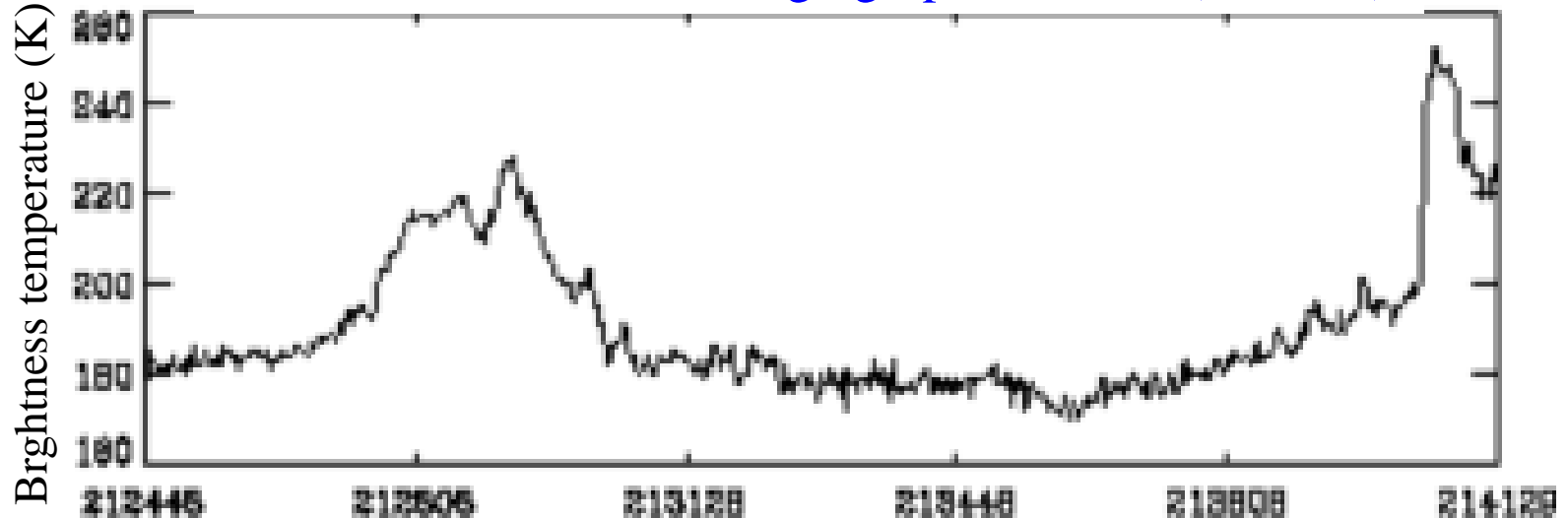


# ER-2 MIR, DC-8 ARMAR, MODIS Simulator Measurements (cont.)

Advanced Microwave Precipitation Radiometer (AMPR)



Moderate-resolution Imaging Spectrometer (MODIS)



# Definitions of Cloud Ice Water Path

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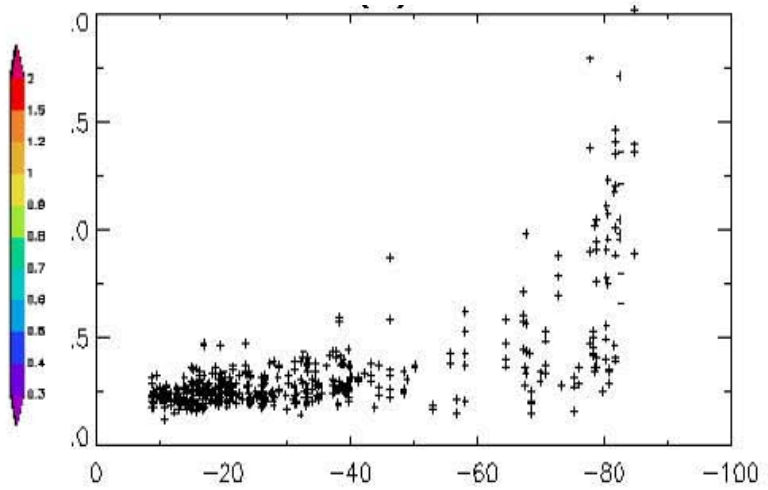
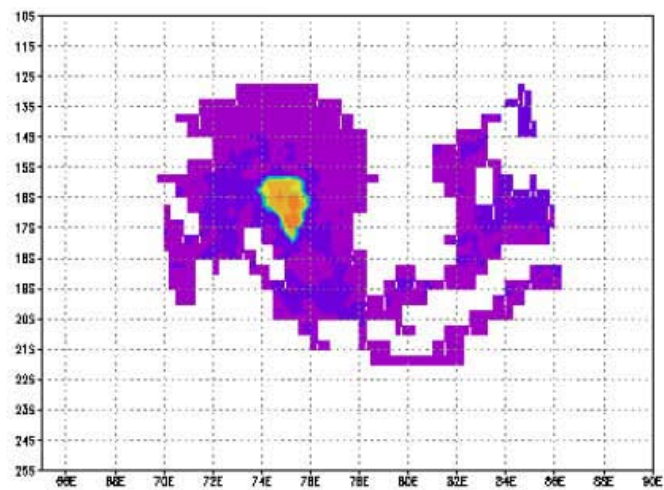
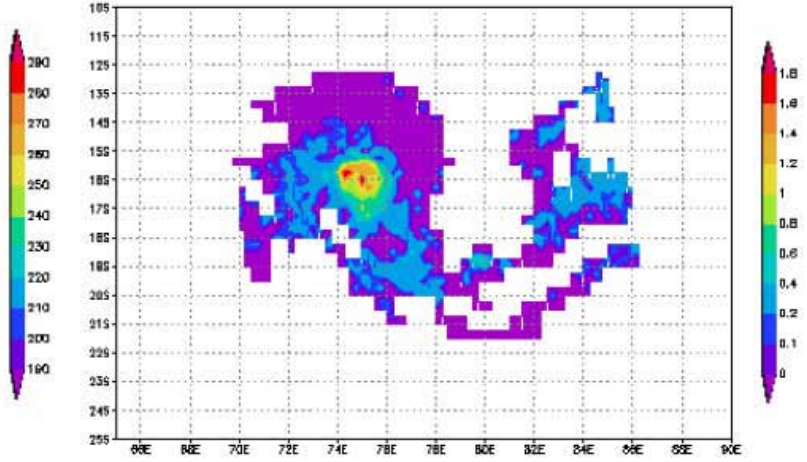
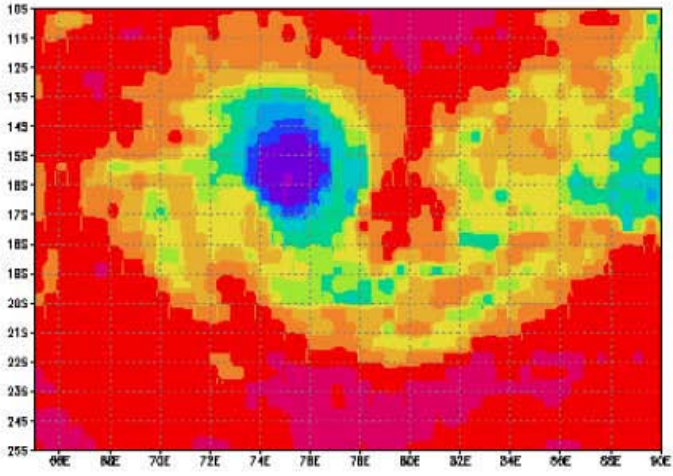
$$\tau = \int_{z_b}^{z_t} dz \int_0^{\infty} \frac{\pi}{4} D^2 \Omega_e(x, m) N(D) dD$$

$$IWP = \int_{z_b}^{z_t} dz \int_0^{\infty} \frac{\pi}{6} D^3 N(D) dD$$

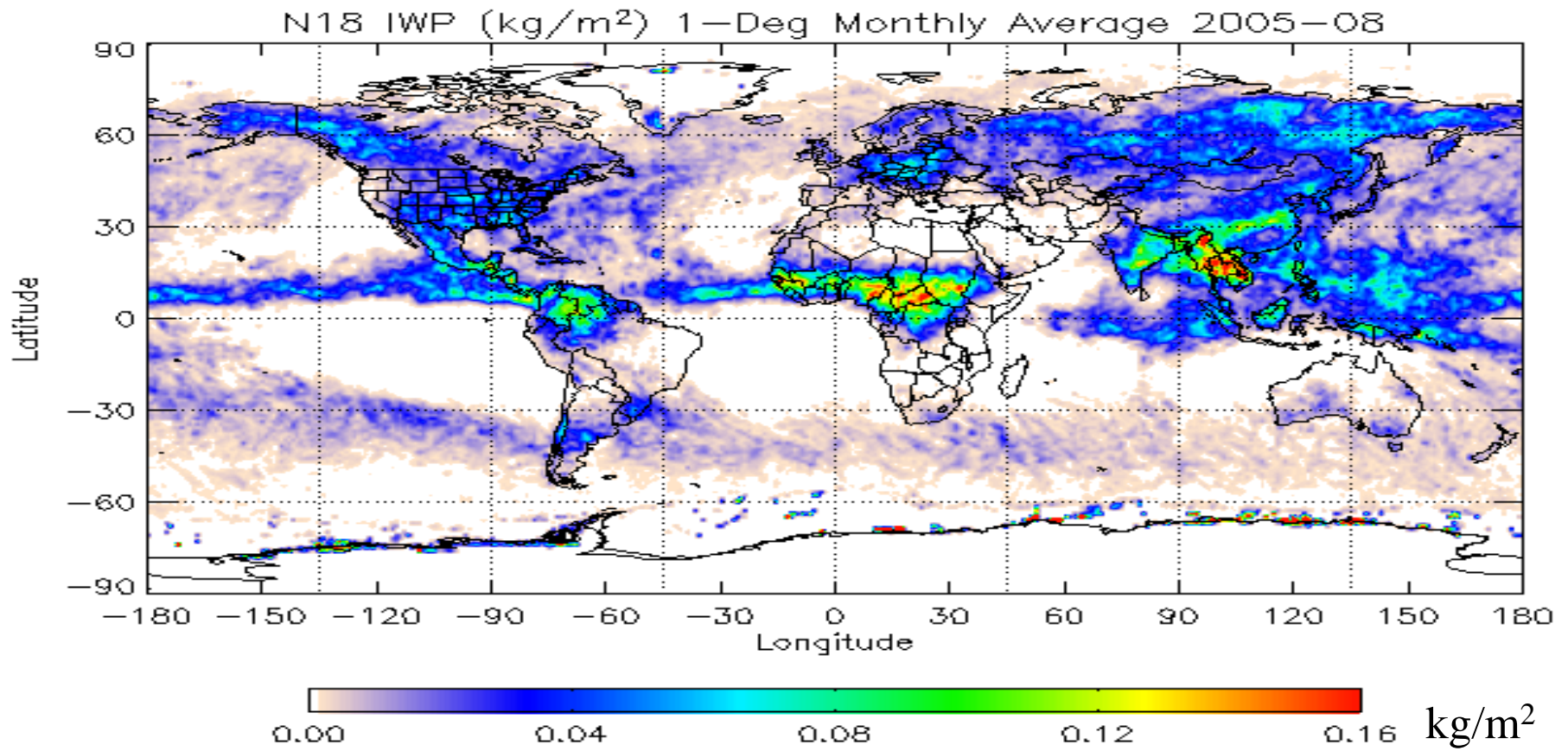
$$\Omega(\mu) = \frac{IWP}{\mu \rho_i D_e} \Omega_N(x, m)$$

$$\Omega_N = \exp(b_0 + b_1 \ln(D_e) + b_2 (\ln D_e)^2)$$

# Cloud Ice Water Path



# N18 IWP Monthly Average 2005-2008



# N18 IWP Monthly Average 2005-2008

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- Brightness temperatures from AMSU-B 89 and 150 GHz are two primary channels for IWP and De
- Retrieval algorithm was published in Journal of Atmos Sci (Weng and Gody, 2000) and J. Appli. Meteor (Zhao and Weng, 2002)
- AMSU-A window channels are used for surface screening
- The algorithm works for opaque ice clouds having IWP greater than  $0.05 \text{ kg/m}^2$

# Atmospheric Sounding from MW

$$T_b = \int_{\Upsilon_s}^1 B(T) d\Upsilon$$

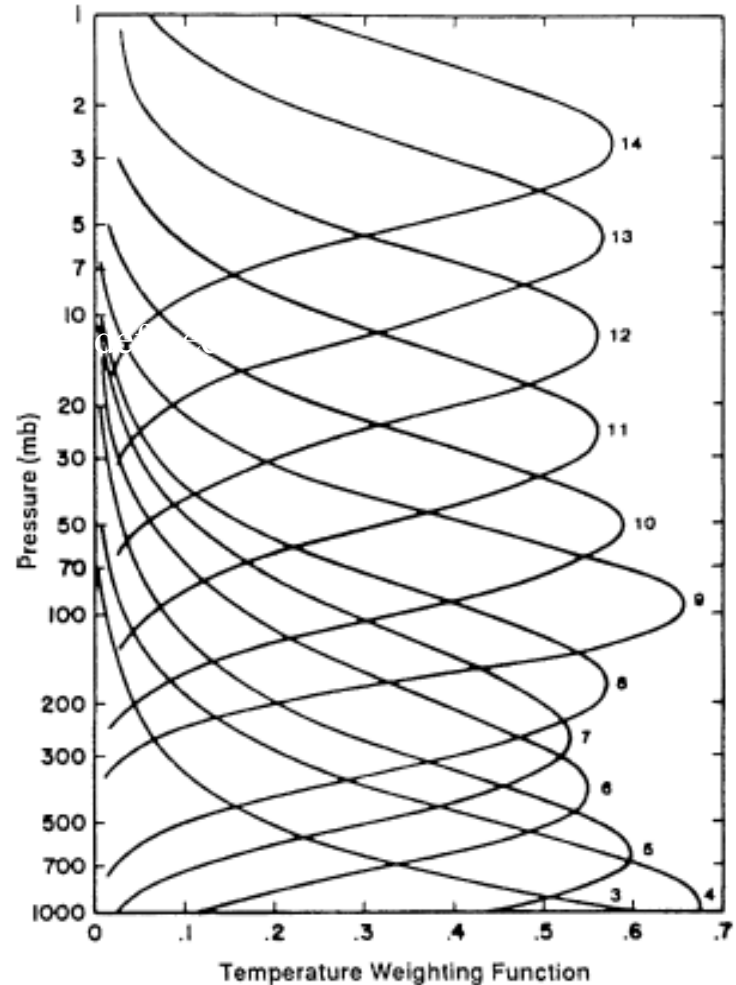
$$d\Upsilon = \exp\left(-\frac{(\tau_s - \tau)}{\mu}\right) d\tau / \mu$$

Weighting function:

$$W = \frac{\partial \Upsilon}{\partial \ln p}$$

$$T_{b,i} = \int_{P_s}^0 B(T) W_i d \ln p$$

$$T_{b,i} = \sum_{j=1}^L c_i T_j W_{i,j}$$





# Temperature Retrieval from Linear Regression Algorithm

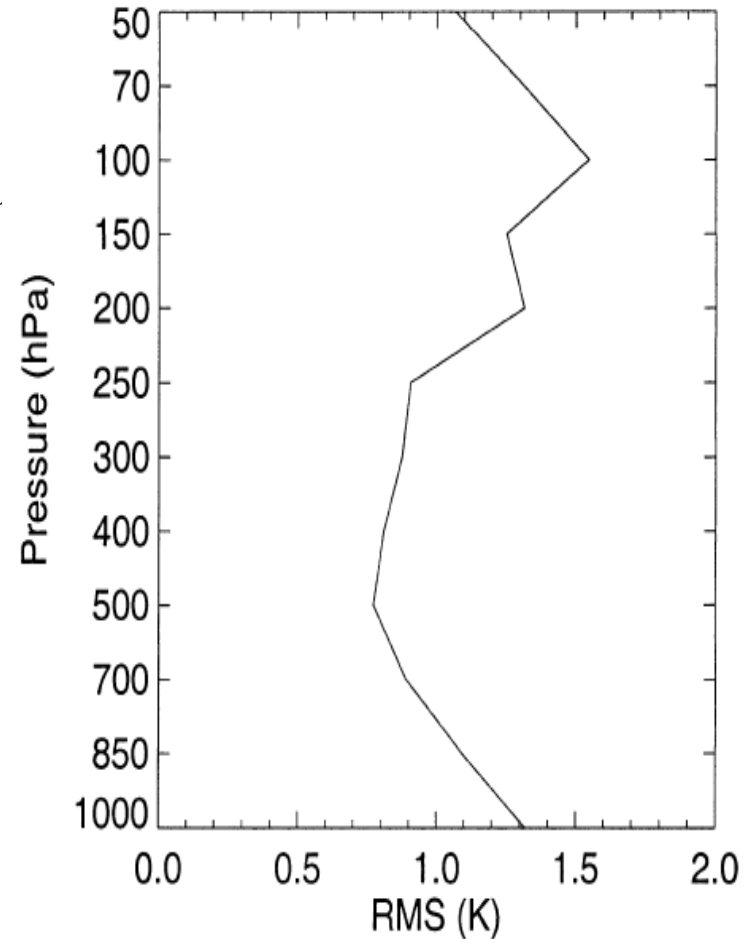
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$$T(p) = C_0(p, \mu) + \sum_{j=1}^L C_j(p, \mu) T_b,$$

$T_b$  is brightness temperature

$\mu$  is the cosine of local zenith angle

$p$ : pressure



# 1D-VAR Retrieval

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- In cloudy and precipitation conditions, the radiance become a non-linear function of temperature
- Also, we have more variables than channel measurements (an under-deterministic problem)
- A prior or background information can help to formulate an optical estimation

# 1D-VAR Retrieval Algorithm

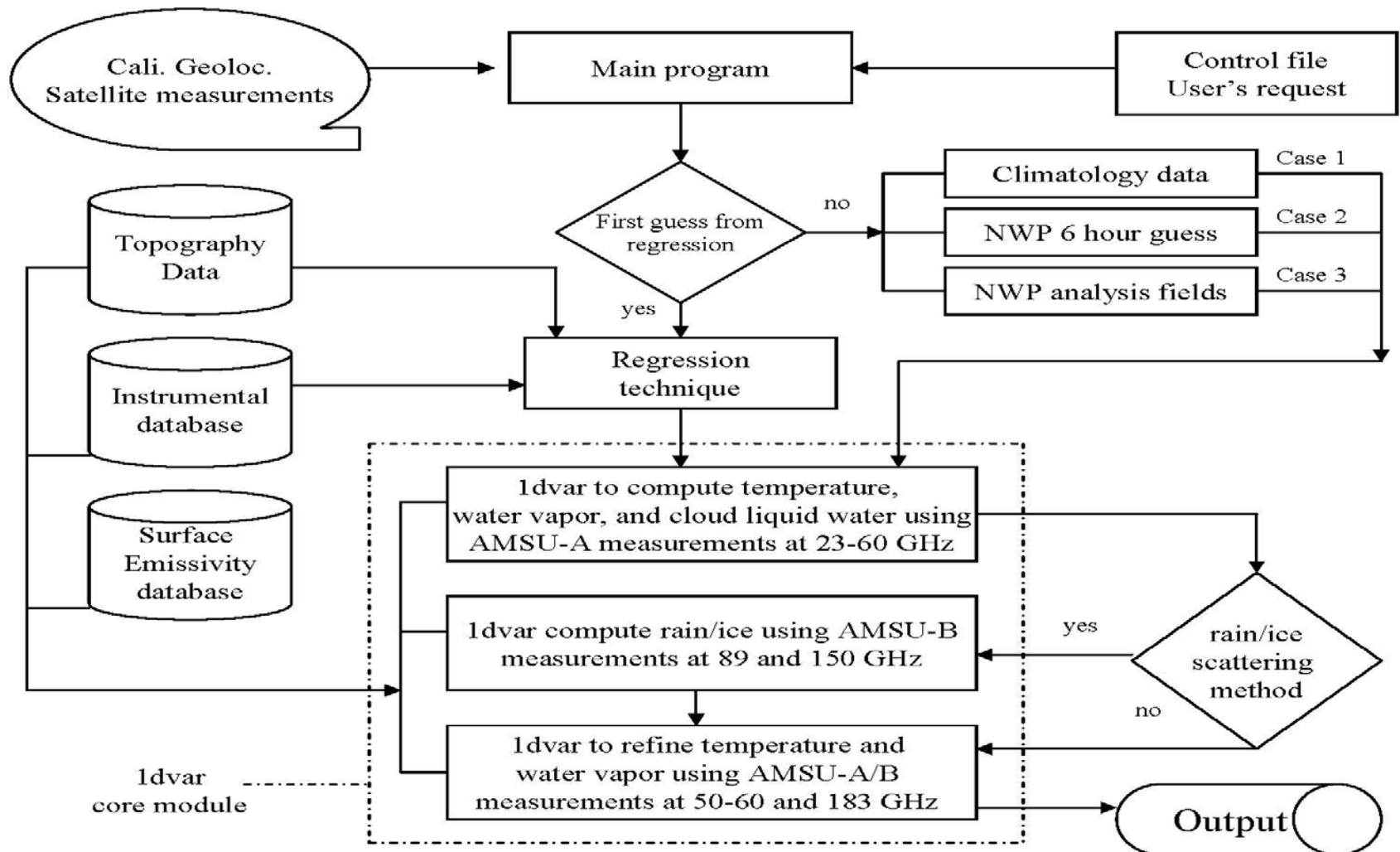
$$J(\mathbf{X}) = \left[ \frac{1}{2} (\mathbf{X} - \mathbf{X}_0)^T \mathbf{B}^{-1} (\mathbf{X} - \mathbf{X}_0) \right] + \left[ \frac{1}{2} (\mathbf{Y}^m - \mathbf{Y}(\mathbf{X}))^T \mathbf{E}^{-1} (\mathbf{Y}^m - \mathbf{Y}(\mathbf{X})) \right]$$

$$\frac{\partial J(\mathbf{X})}{\partial \mathbf{X}} = \mathbf{J}'(\mathbf{X}) = 0$$

$$\Delta \mathbf{X}_{n+1} = \left\{ \left( \mathbf{B}^{-1} + \mathbf{K}_n^T \mathbf{E}^{-1} \mathbf{K}_n \right)^{-1} \mathbf{K}_n^T \mathbf{E}^{-1} \right\} \left[ \left( \mathbf{Y}^m - \mathbf{Y}(\mathbf{X}_n) \right) + \mathbf{K}_n \Delta \mathbf{X}_n \right]$$

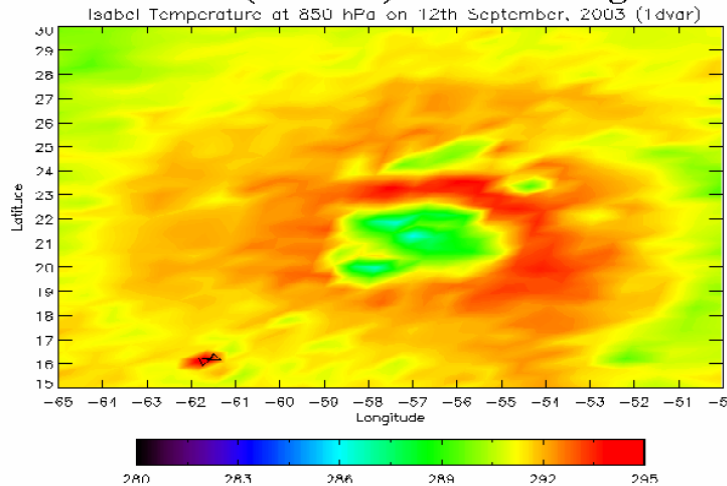
$$\mathbf{X}_{n+1} = \left\{ \mathbf{B} \mathbf{K}_n^T \left( \mathbf{K}_n \mathbf{B} \mathbf{K}_n^T + \mathbf{E} \right)^{-1} \right\} \left[ \left( \mathbf{Y}^m - \mathbf{Y}(\mathbf{X}_n) \right) + \mathbf{K}_n \mathbf{X}_n \right]$$

# MW 1D-VAR System for Atmospheric Sounding

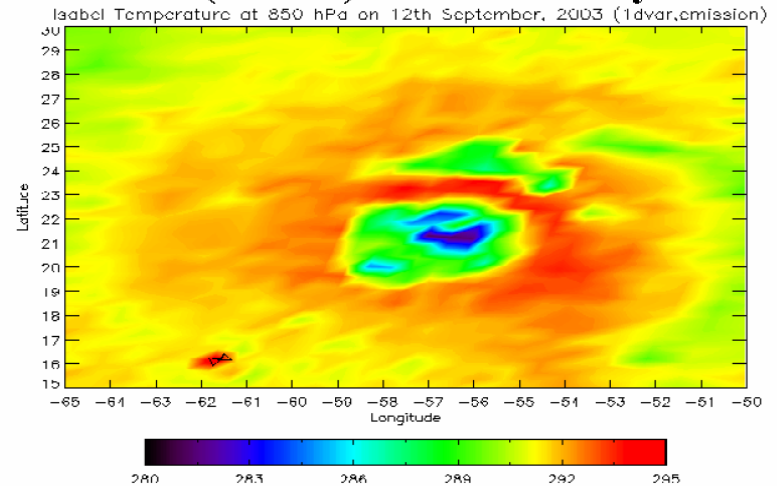


# Hurricane temperature Structure from Two RT models

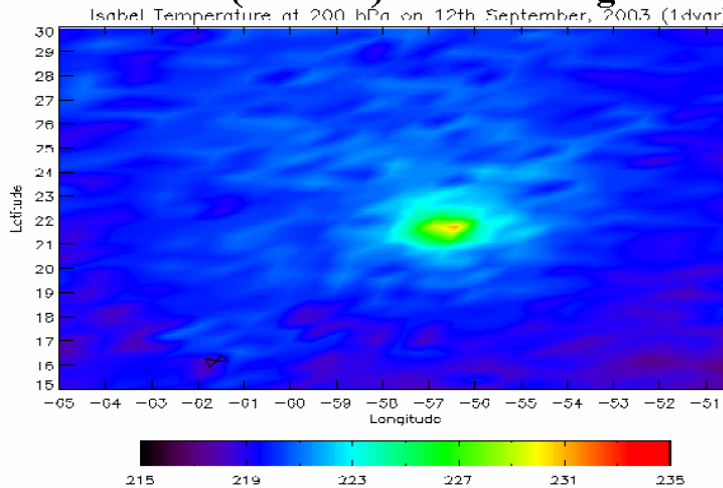
## T(850hPa) – Scattering



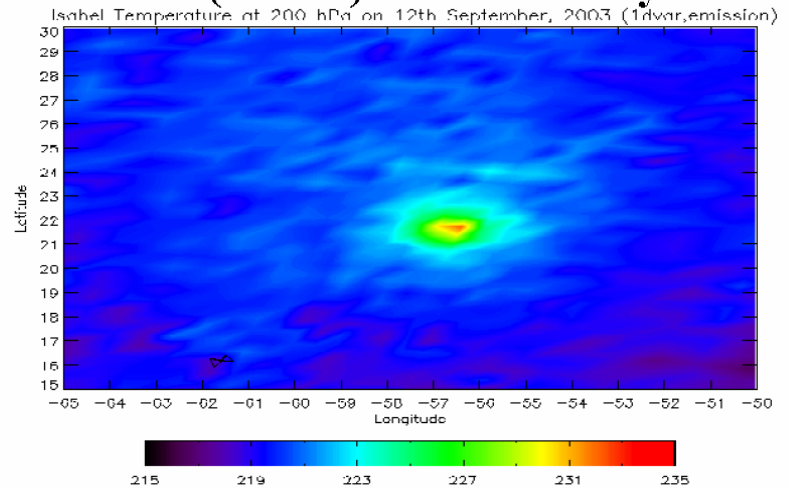
## T(850hPa) – Emission only



## T(200hPa) – Scattering

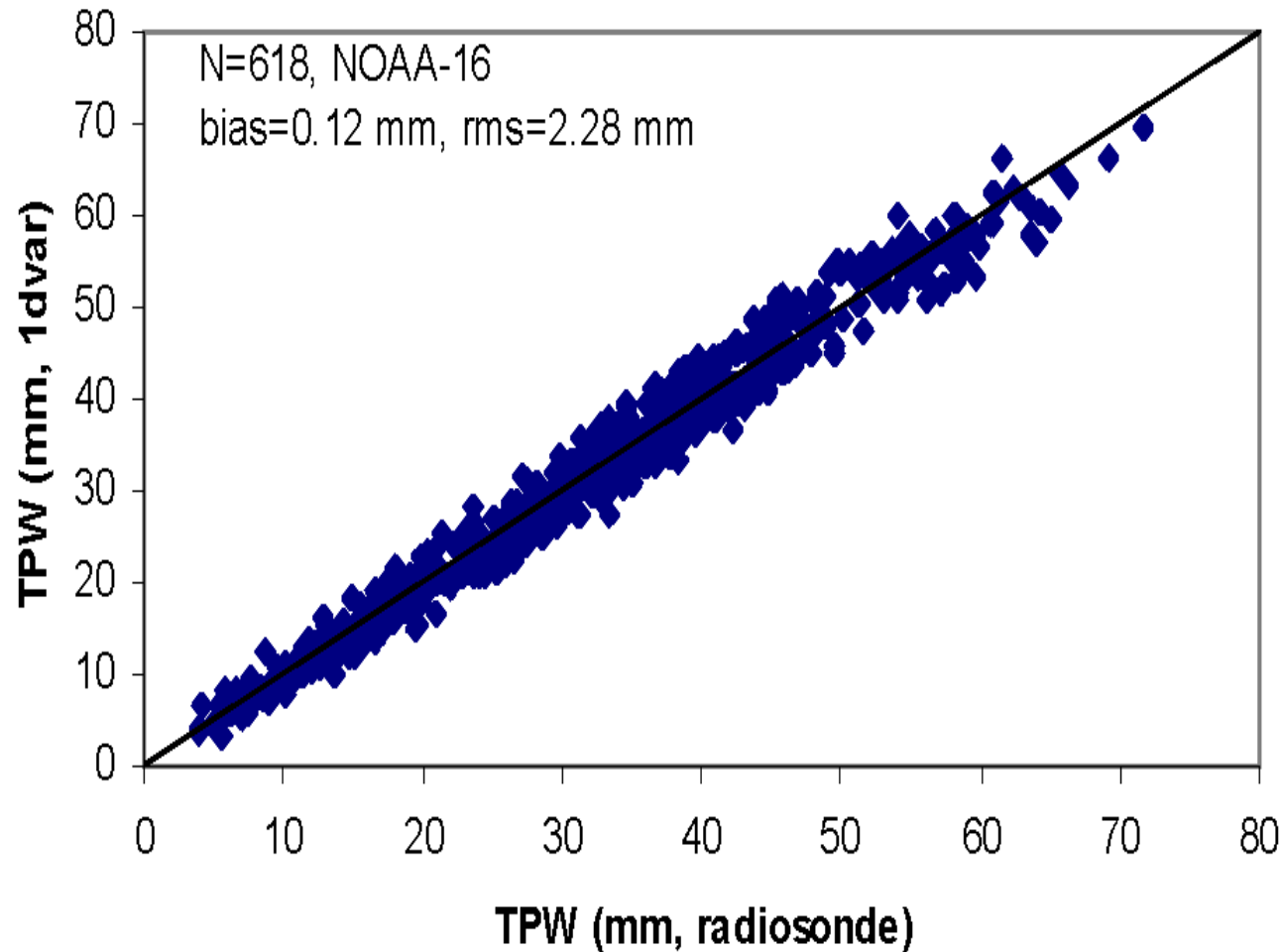


## T(200hPa) – Emission only



# Validation of TPW Retrieval Using Radiosondes

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# Summary of MW Remote Sensing of Atmosphere

## 1. Microwave Absorption Bands

- O<sub>2</sub> (50-60 GHz, 117-120 GHz),
- H<sub>2</sub>O (176-190 GHz)
- Used for sounding of temperature & humidity

## 2. Microwave Cloud Algorithms

- Emission: cloud liquid water/total precipitable water
- Scattering: ice water path/ particle size

## 3. Microwave Sounding Algorithms:

- simultaneous retrievals from 1dvar
- All weather profiling requires scattering rt model
- Accurate surface emissivity model

## 4. Main Applications:

- NWP data assimilations
- Hurricane monitoring

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